

RUHR-UNIVERSITÄT BOCHUM

## Selective Opening Security from Simulatable Data Encapsulation

Asiacrypt 2016, Hanoi, 5th of December 2016

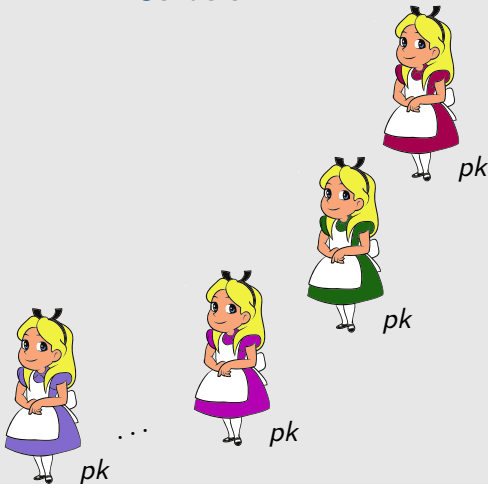
**Felix Heuer**, Bertram Poettering  
Horst Görtz Institute for IT Security  
Ruhr University Bochum

# Selective Opening Attacks

Receiver



Senders

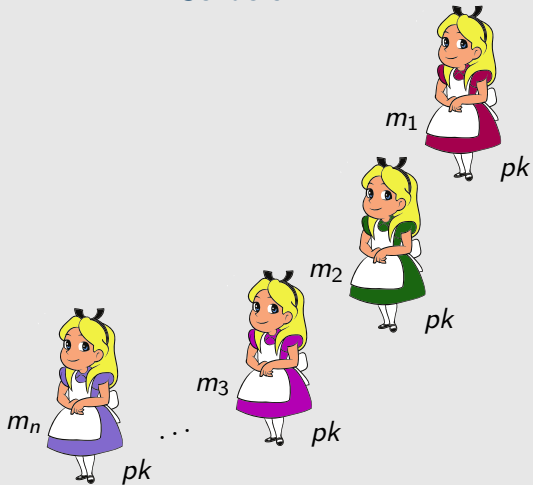


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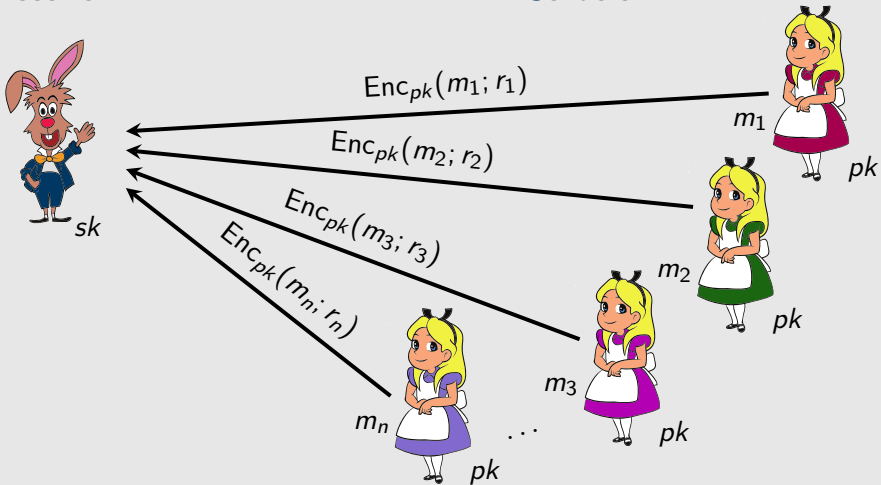
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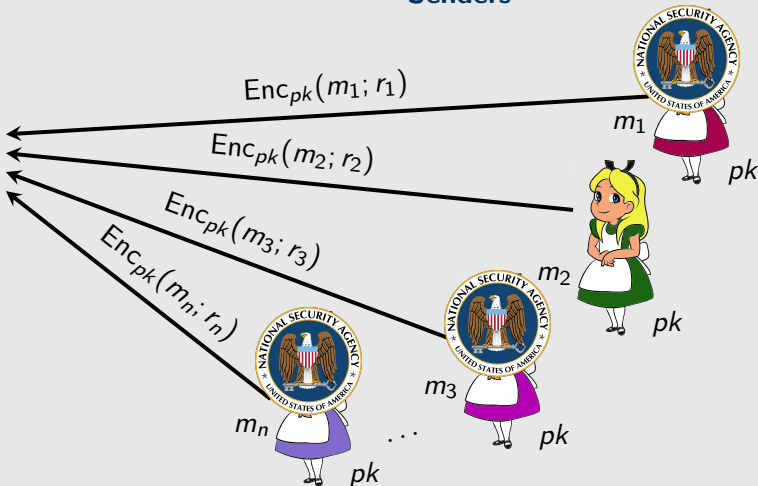
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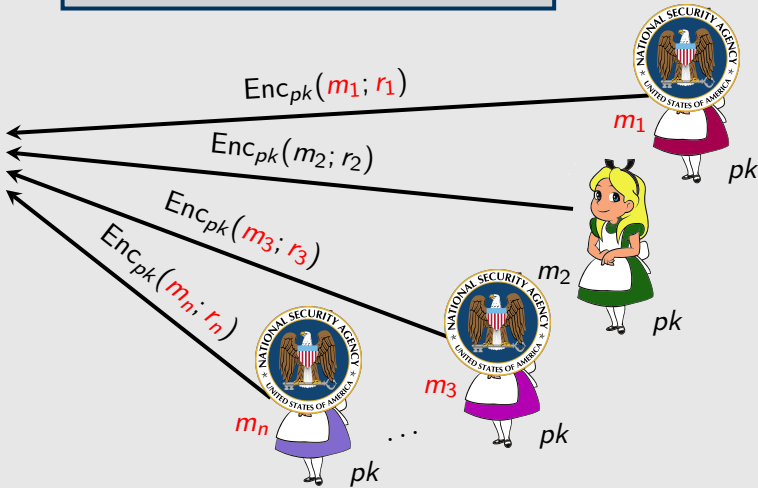
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**Corrupting senders reveals  $m$  and  $r$ .**

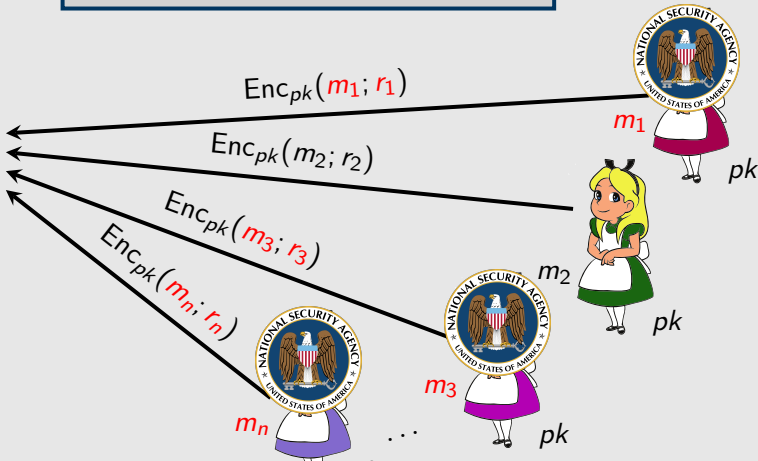
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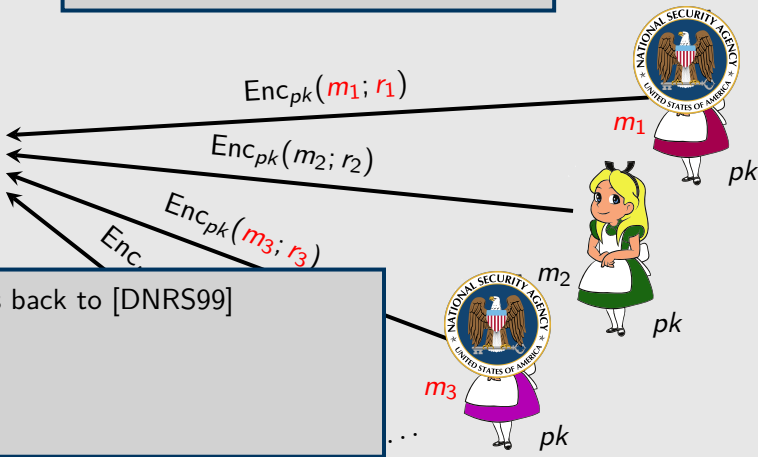


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- Dates back to [DNRS99]

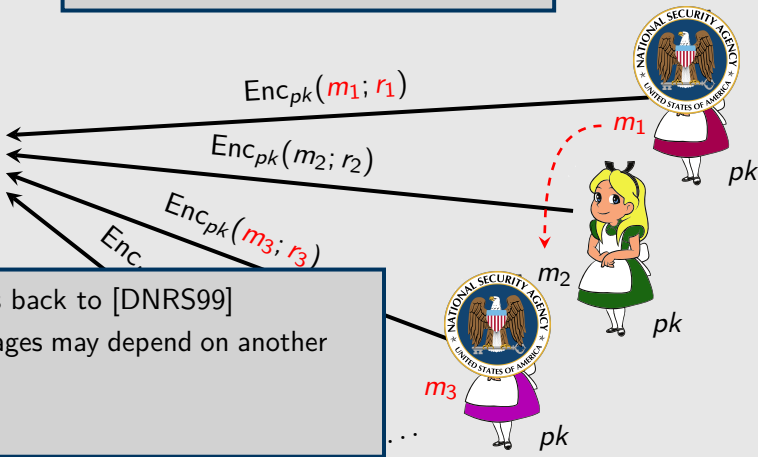
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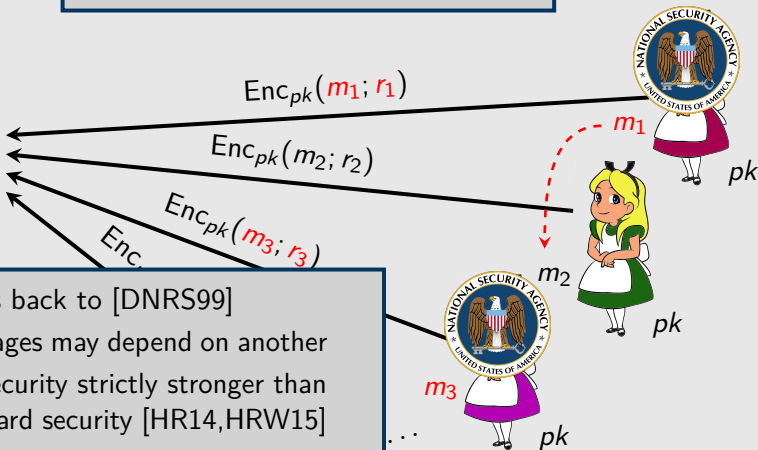
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- Dates back to [DNRS99]
- Messages may depend on another
- SO security strictly stronger than standard security [HR14,HRW15]

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# Defining SIM-SO-CCA Security [BHK12]

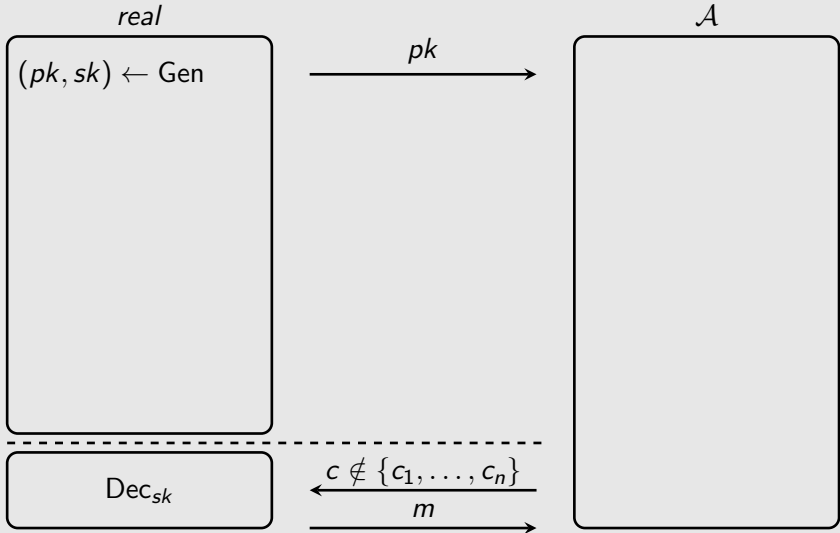
*real*



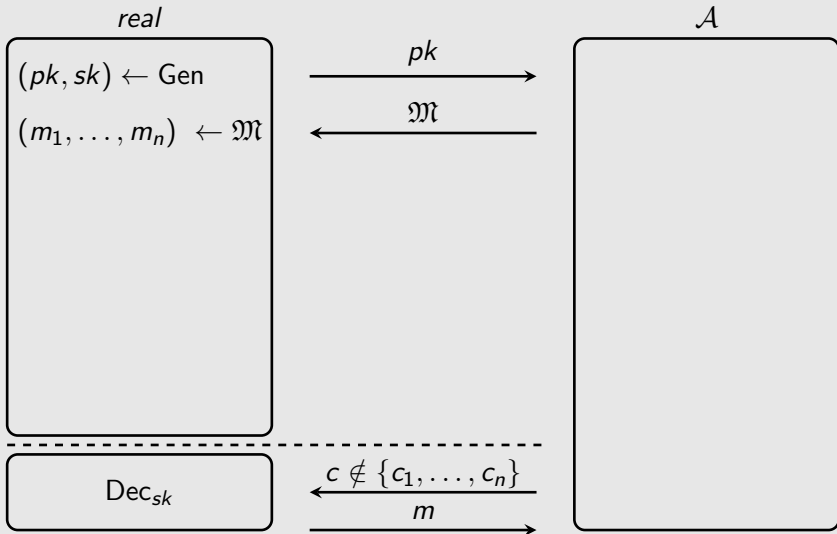
$\mathcal{A}$



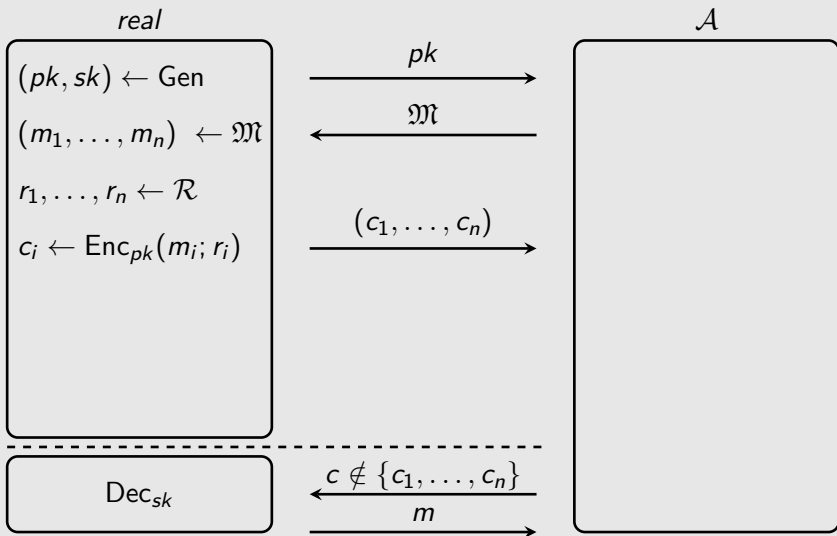
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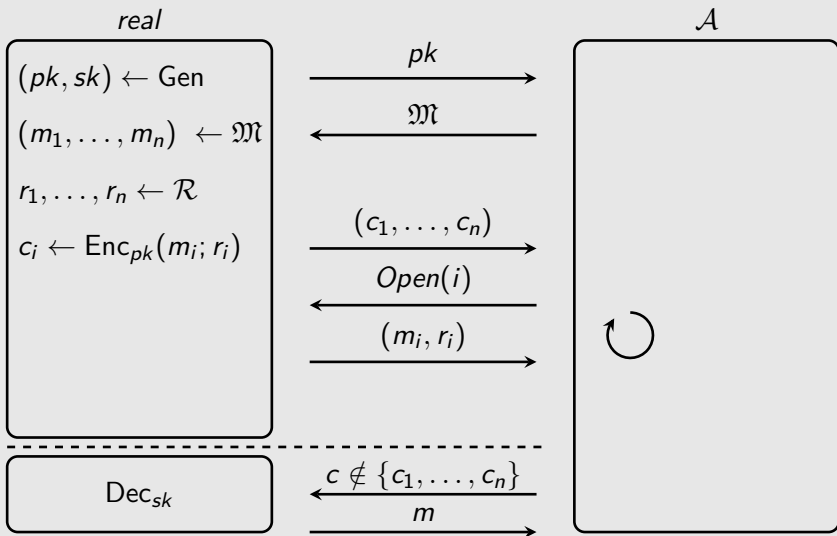
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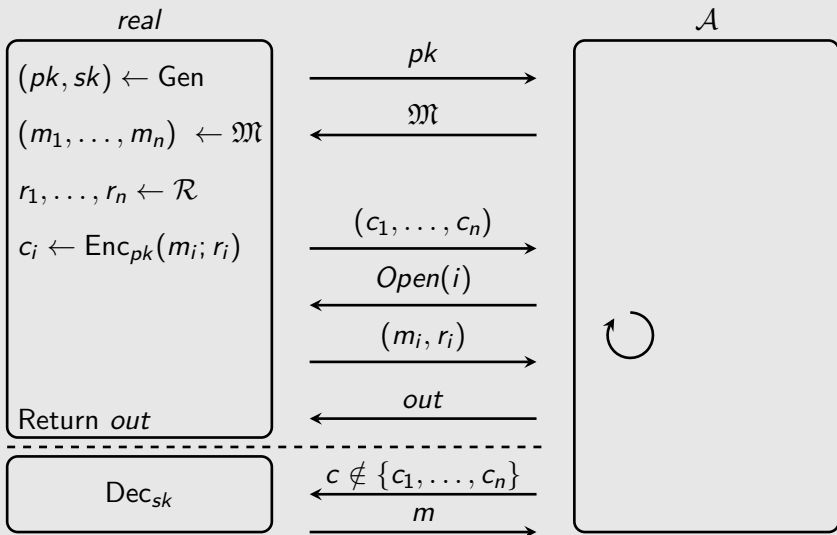
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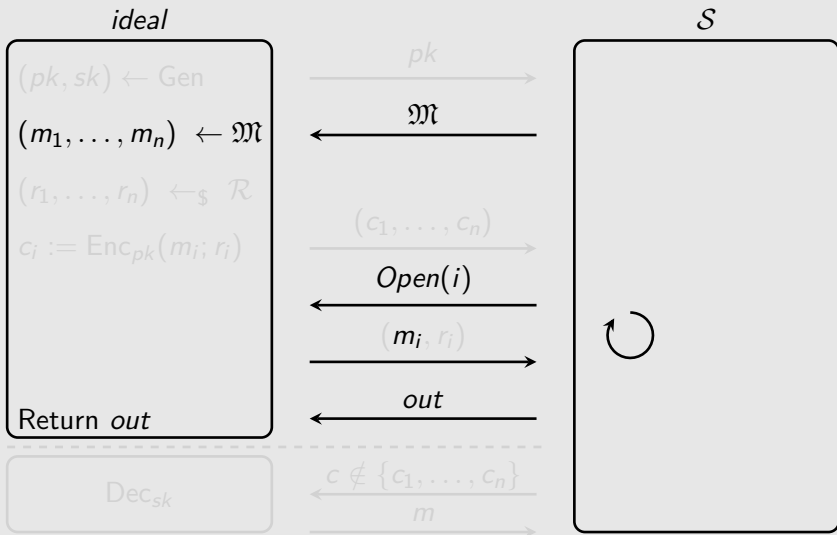


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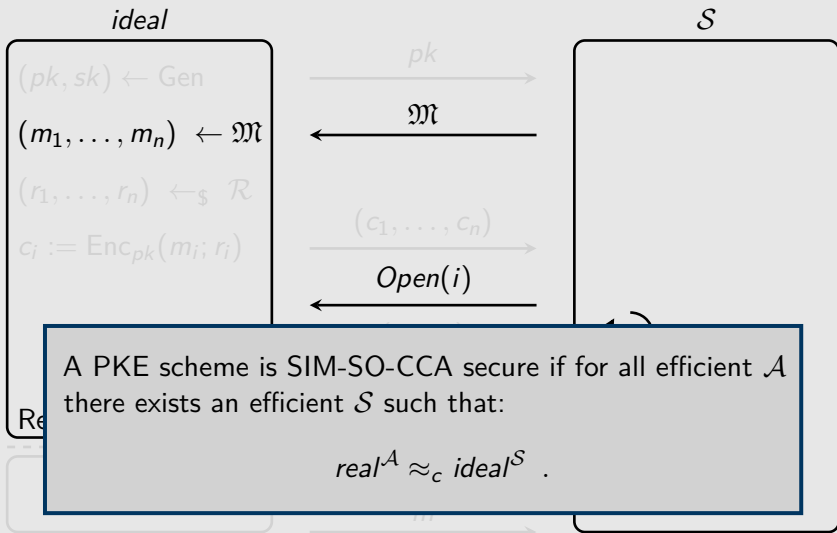




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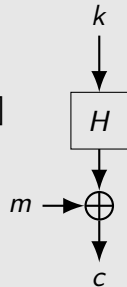
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## Previous Results

- DHIES, RSA-OAEP are SIM-SO-CCA secure [HJKS15]
- DEM: xor with the output of a random oracle



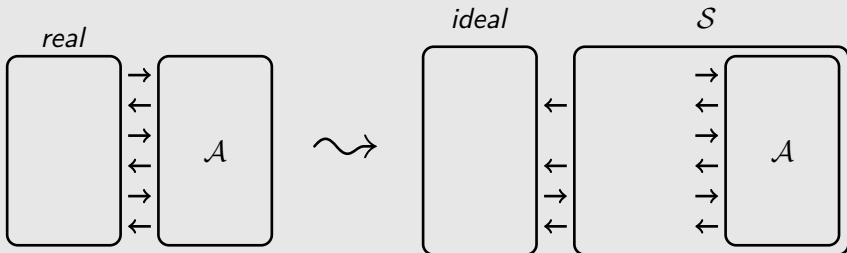
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$\mathcal{S}$  (internally) runs  $\mathcal{A}$  to draw the same conclusions as  $\mathcal{A}$ .



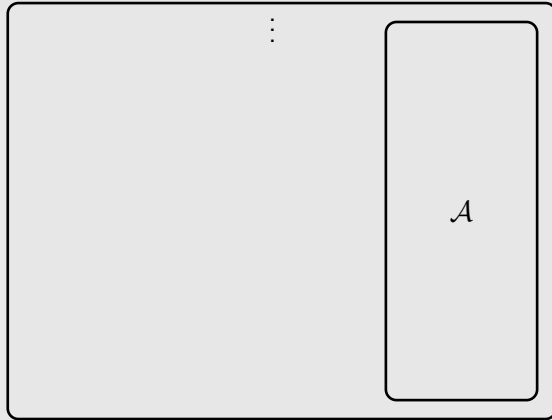


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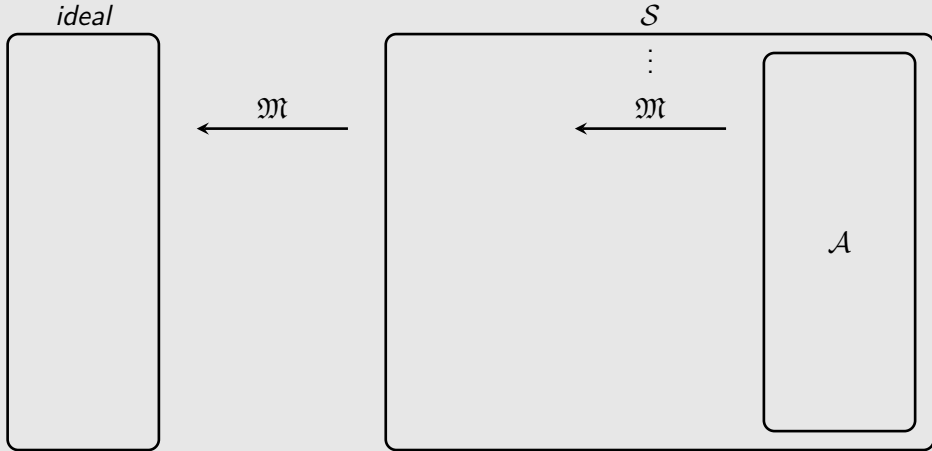
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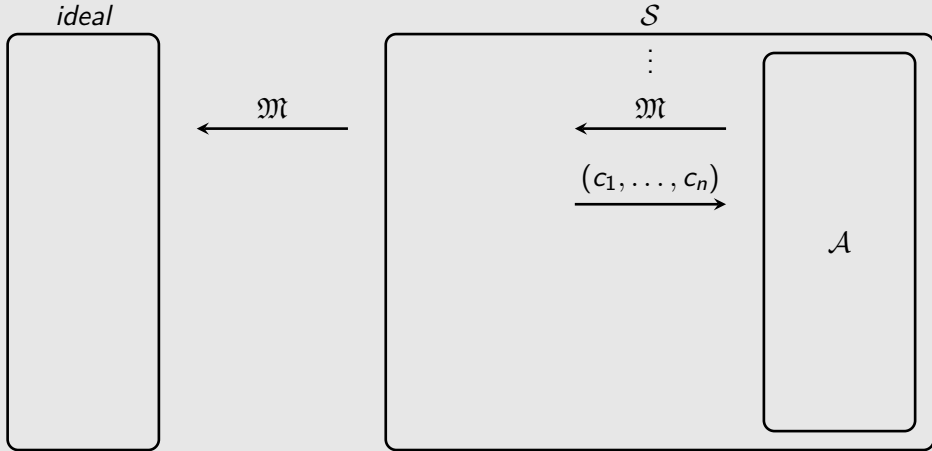
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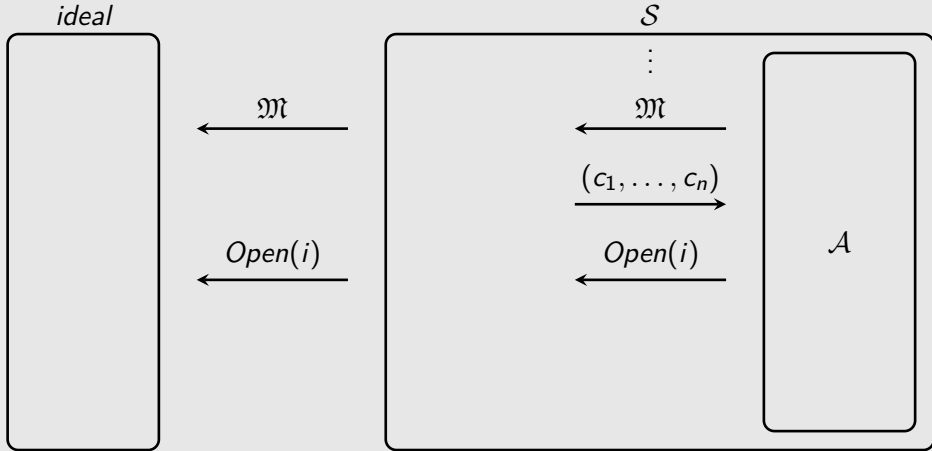
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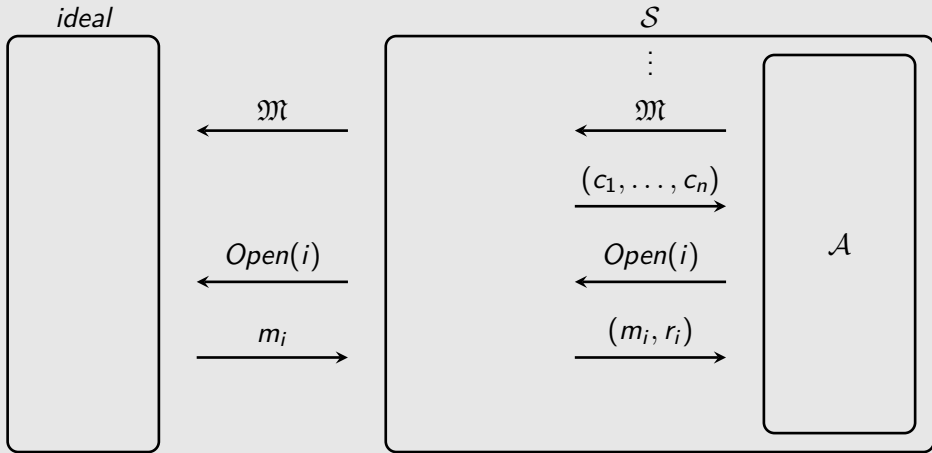
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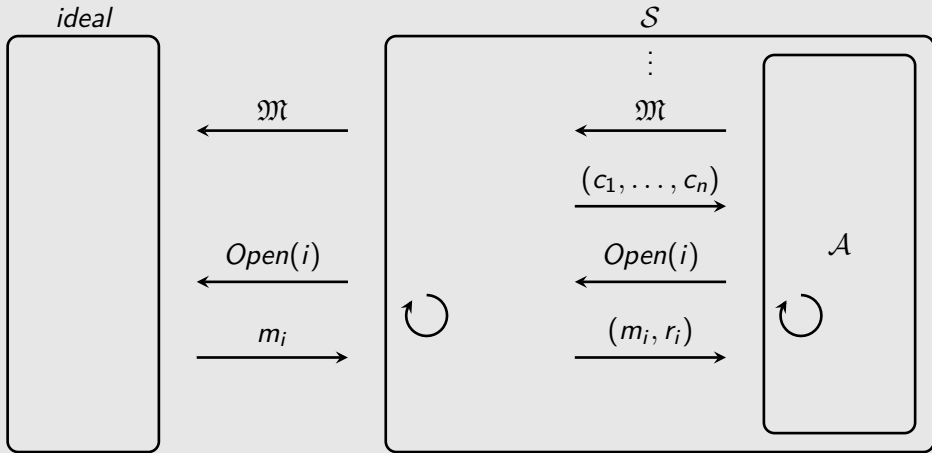
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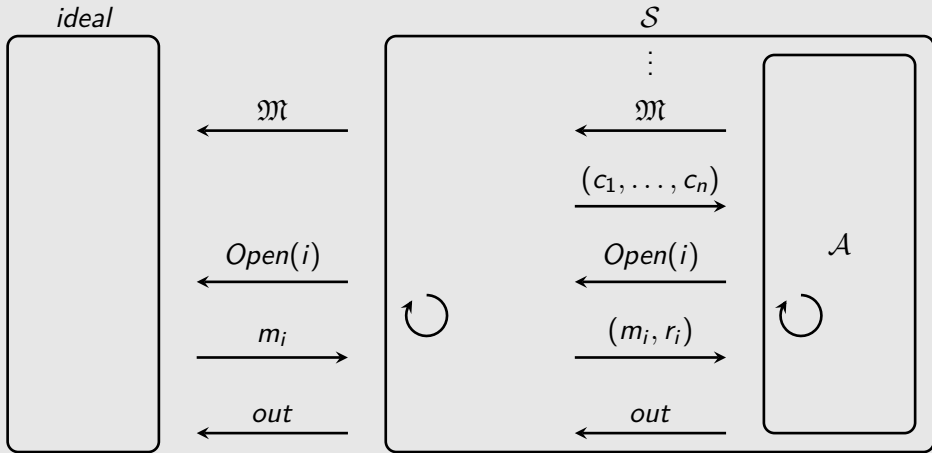
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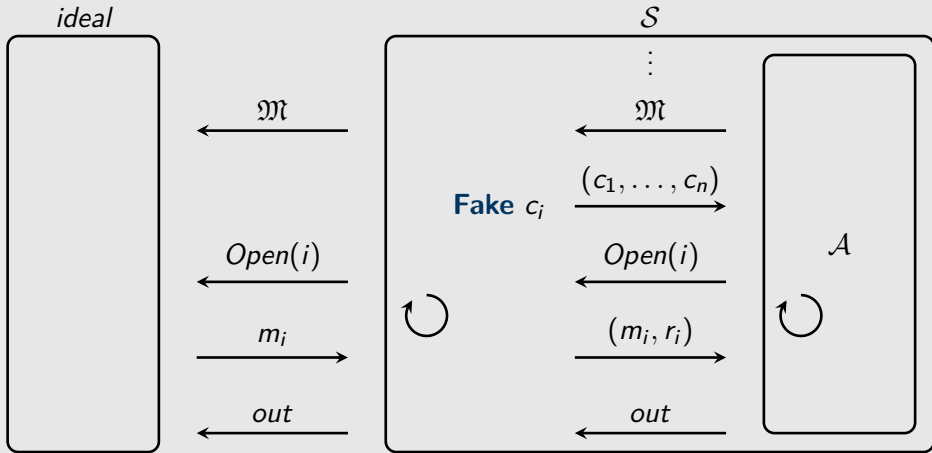
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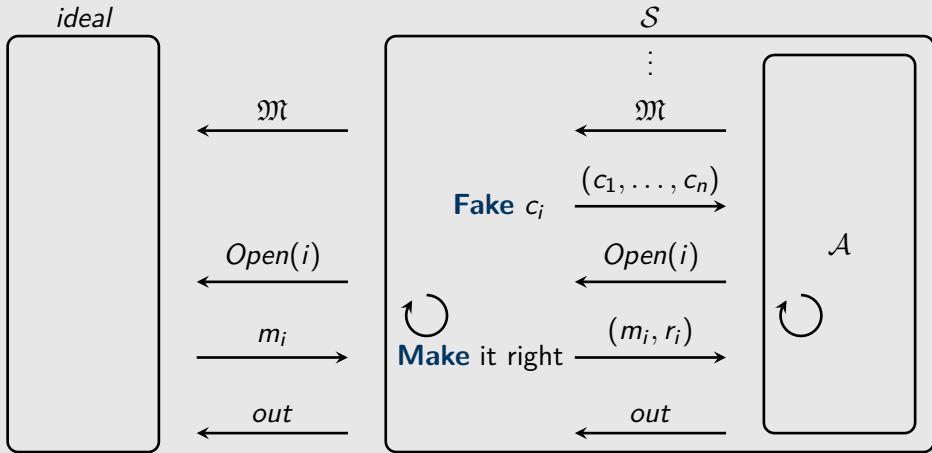


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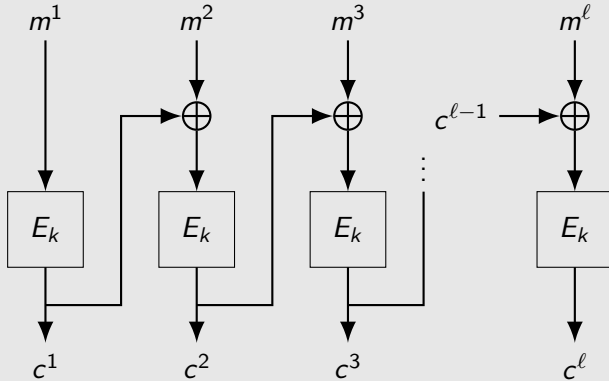




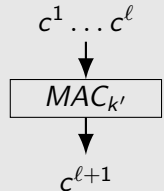
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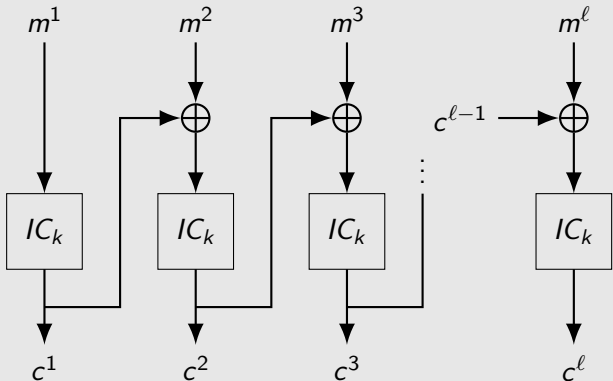
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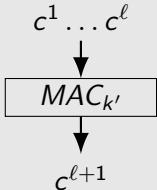
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2. Running **(Fake, Make)** yields a uniform permutation.

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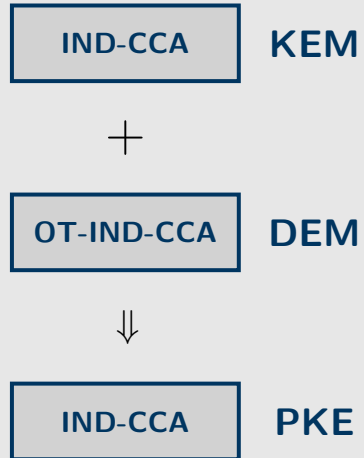
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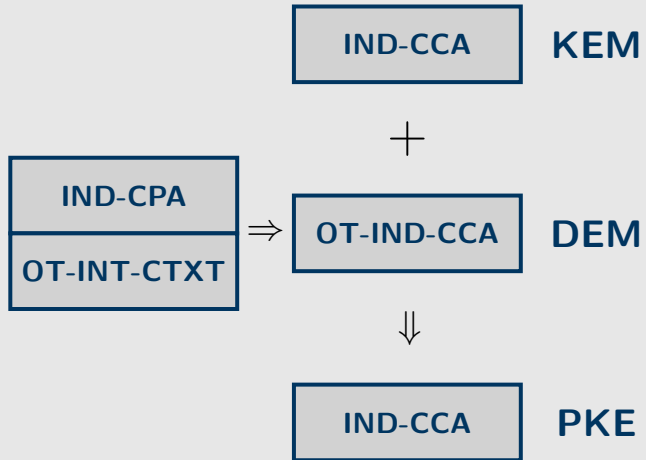
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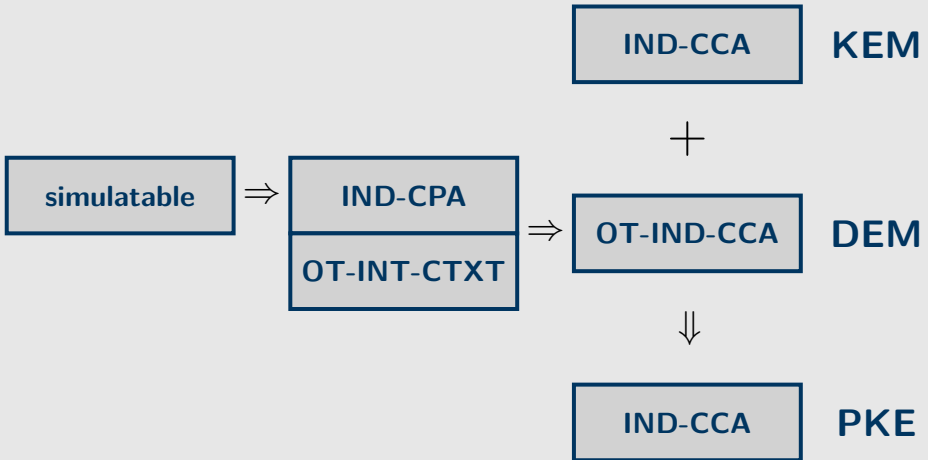
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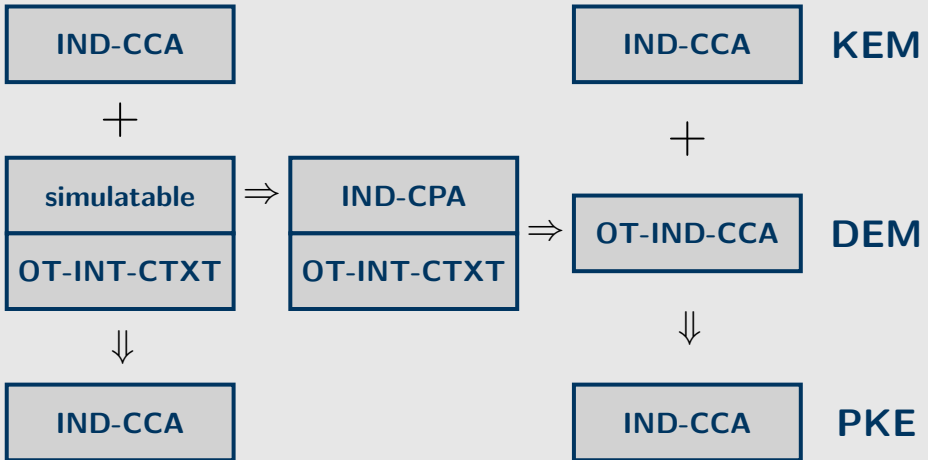
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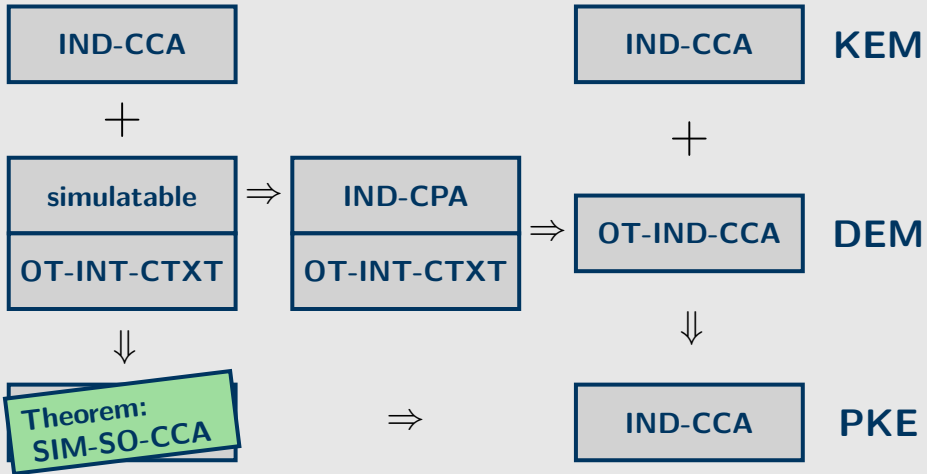
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+

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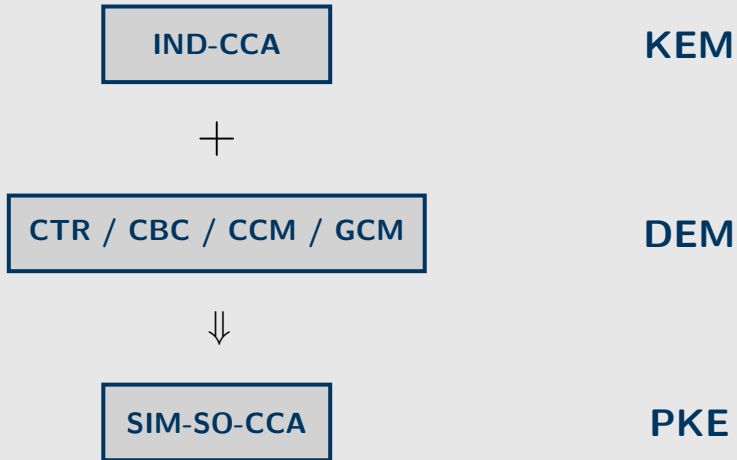
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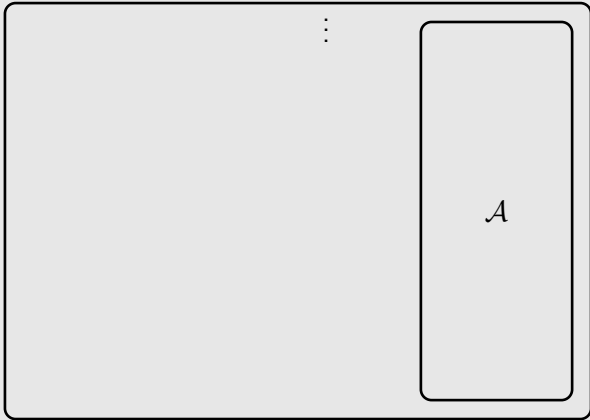


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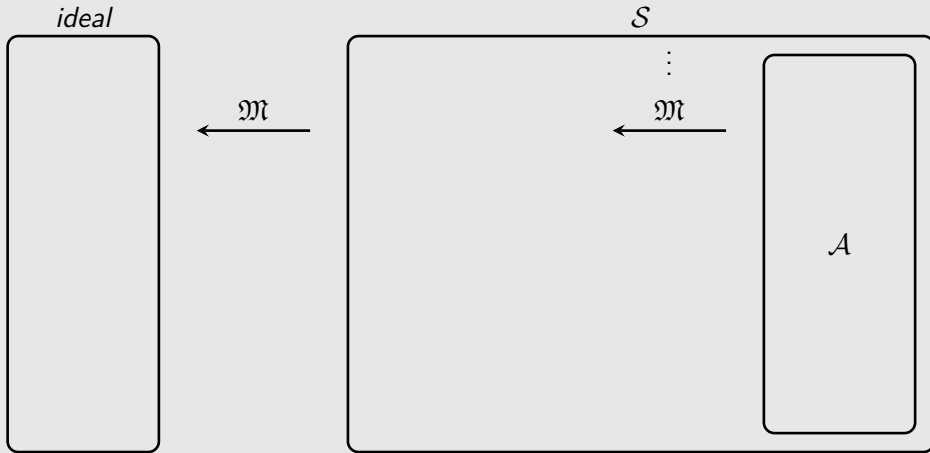


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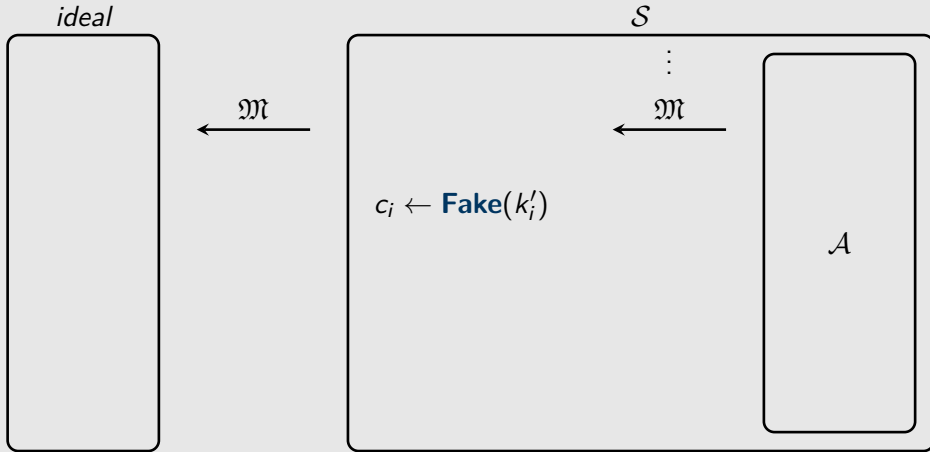


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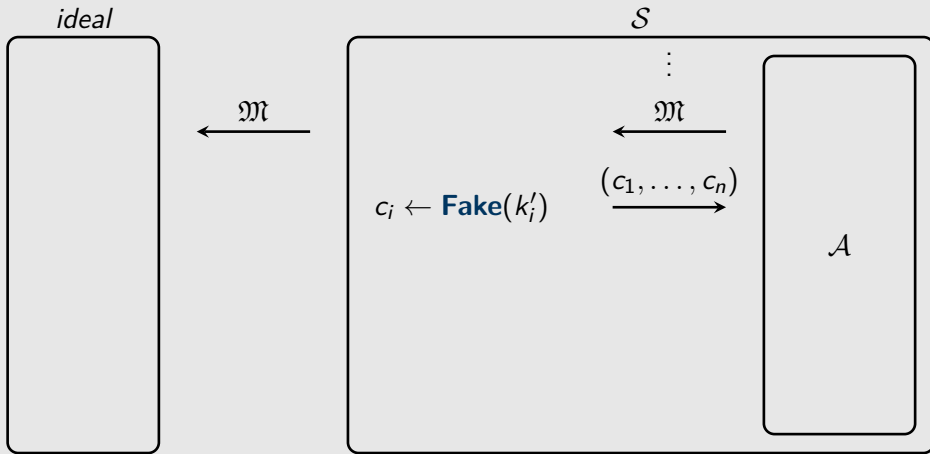
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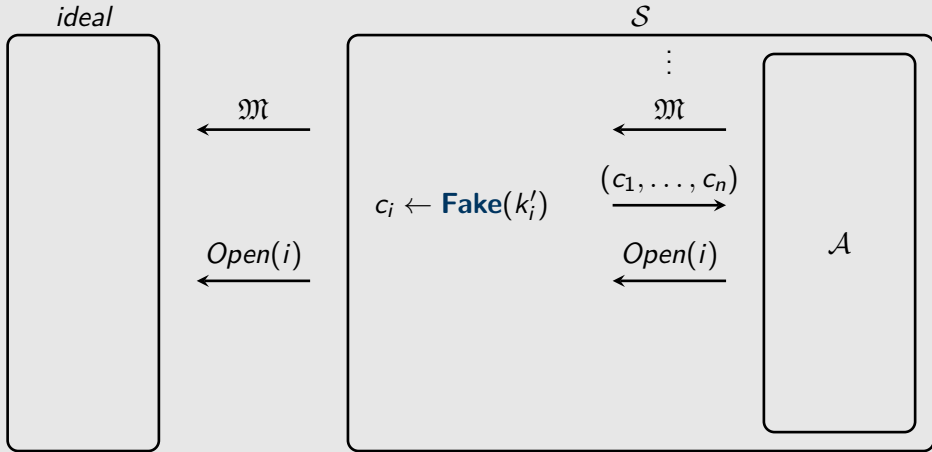
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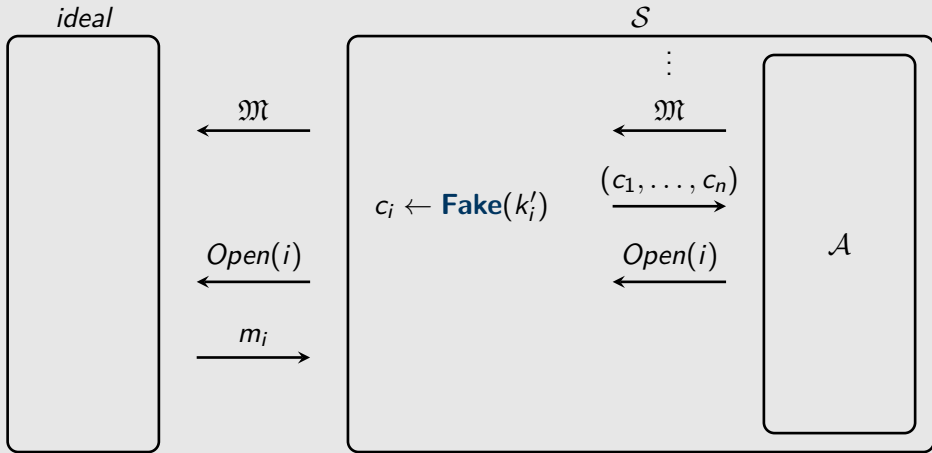
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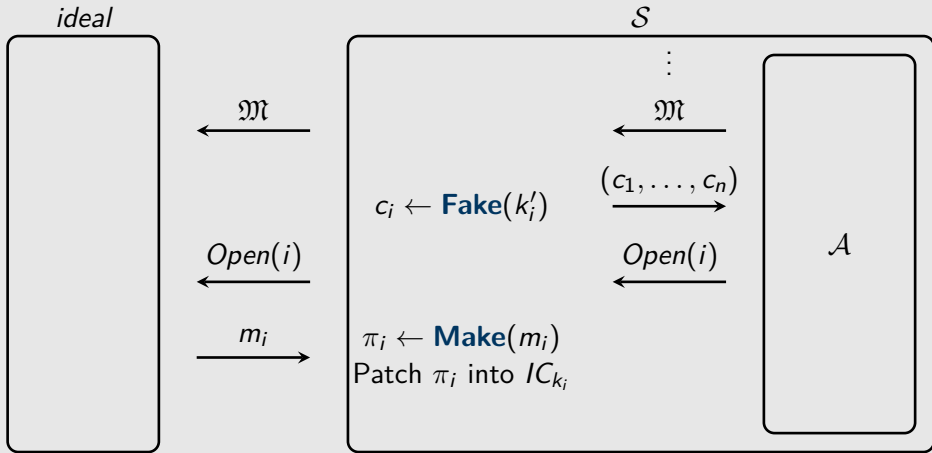
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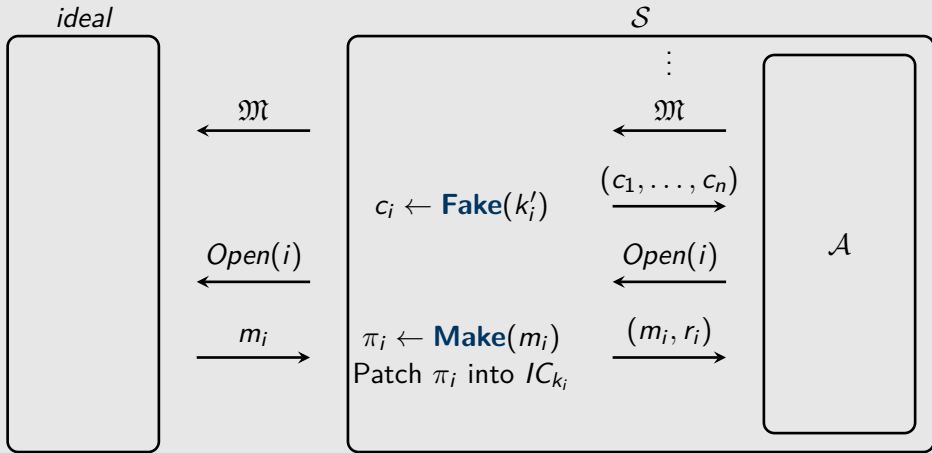
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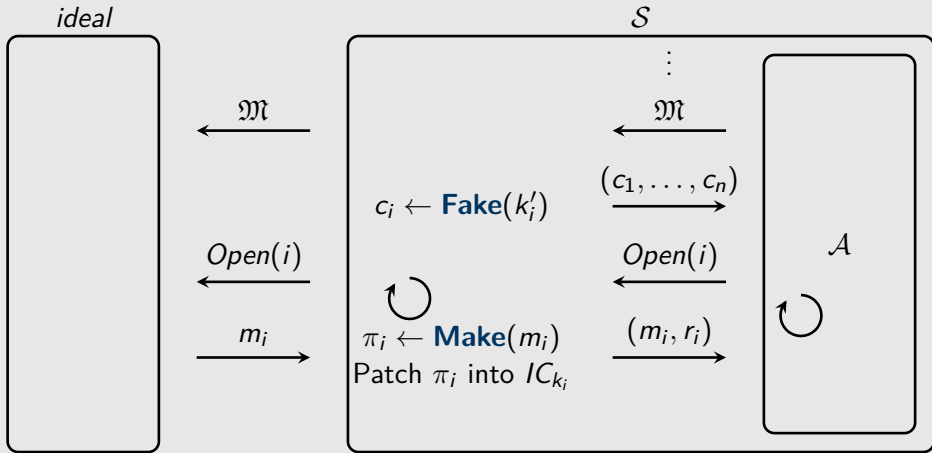


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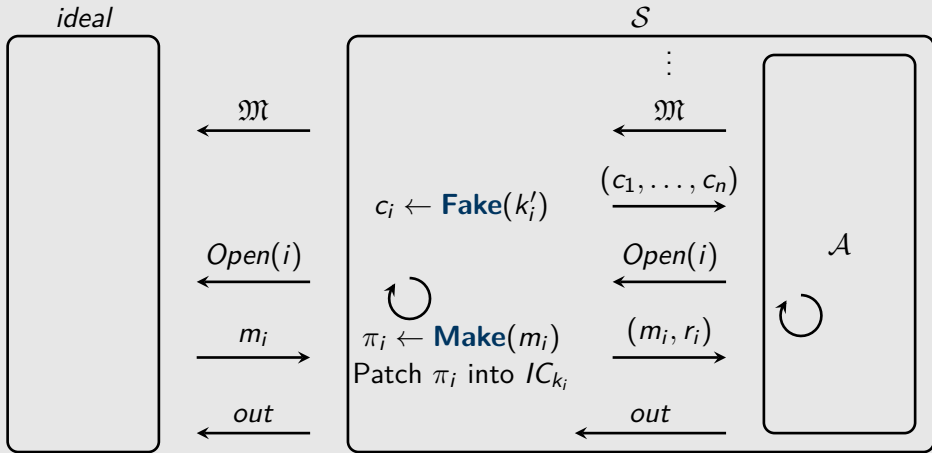




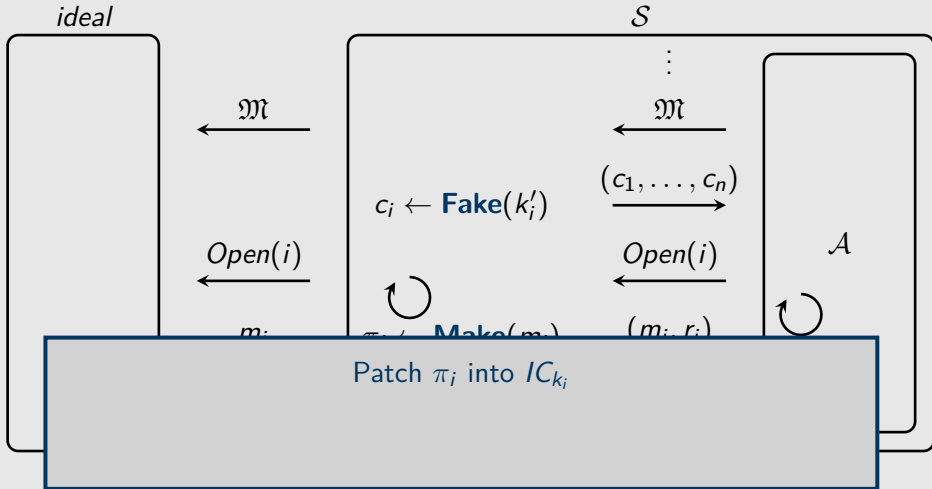
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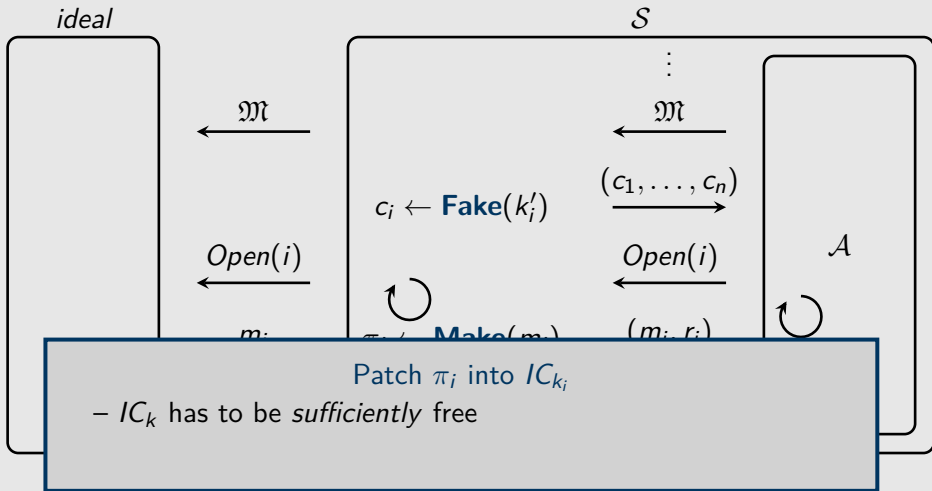
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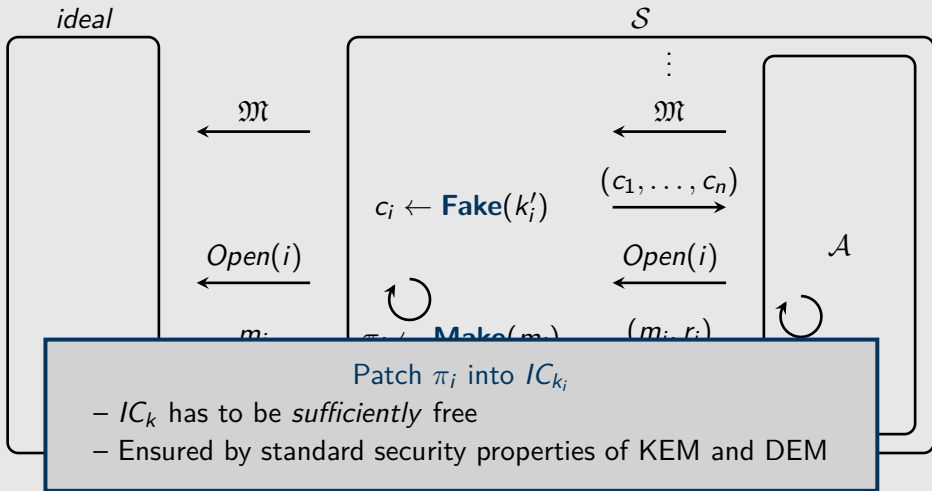
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2016/845

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