Balloon Hashing

A Memory-Hard Function with Provable Protection Against Sequential Attacks

Dan Boneh, Stanford *Henry Corrigan-Gibbs, Stanford Stuart Schechter, Microsoft Research

Balloon Hashing

A new password hashing function that:

- 1. Is proven memory-hard (in the sequential setting)
- 2. Uses a password-independent data access pattern
- 3. Matches the performance of the best heuristically secure memory-hard functions































The Attacker's Job

User	Salt	H(passwd, salt)
alice	0x65ff0162	0x526642d8
bob	0x37ceb328	0x5a325ad2
carol	0xec967ec1	0xf4441a71
dave	0xfb791a9a	0x1dbd71f3

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If the authentication server can compute...X hashesper\$ of energythen an attacker with custom hardware shouldonly be able to compute...(1+ε)X hashesper\$ of energy

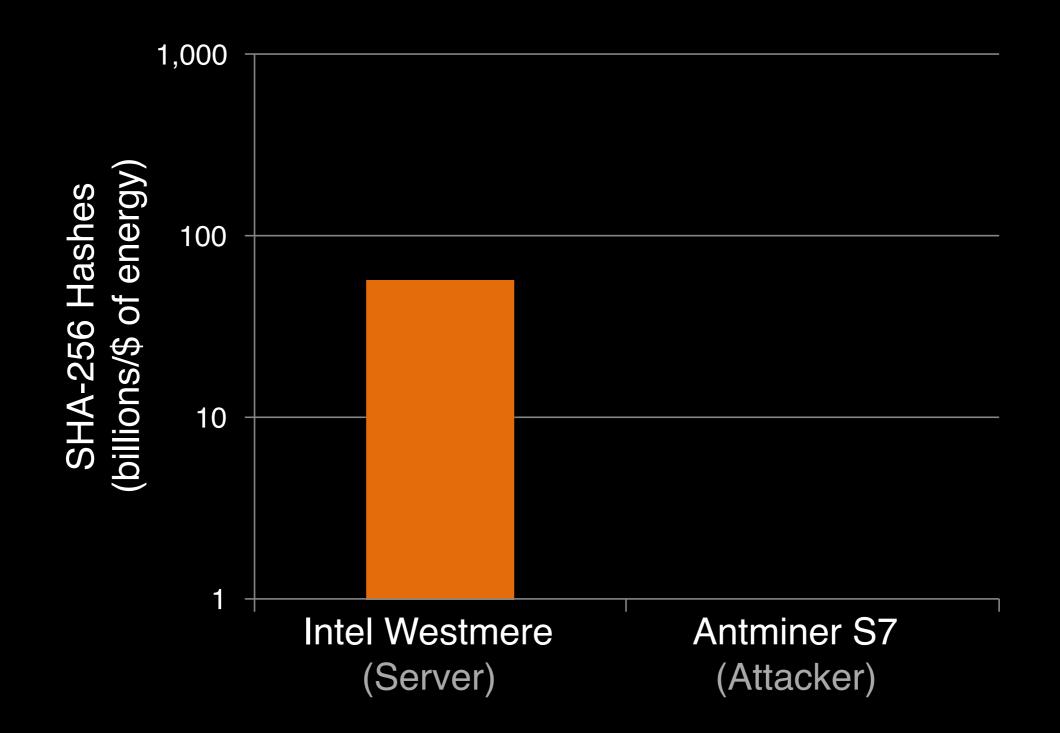
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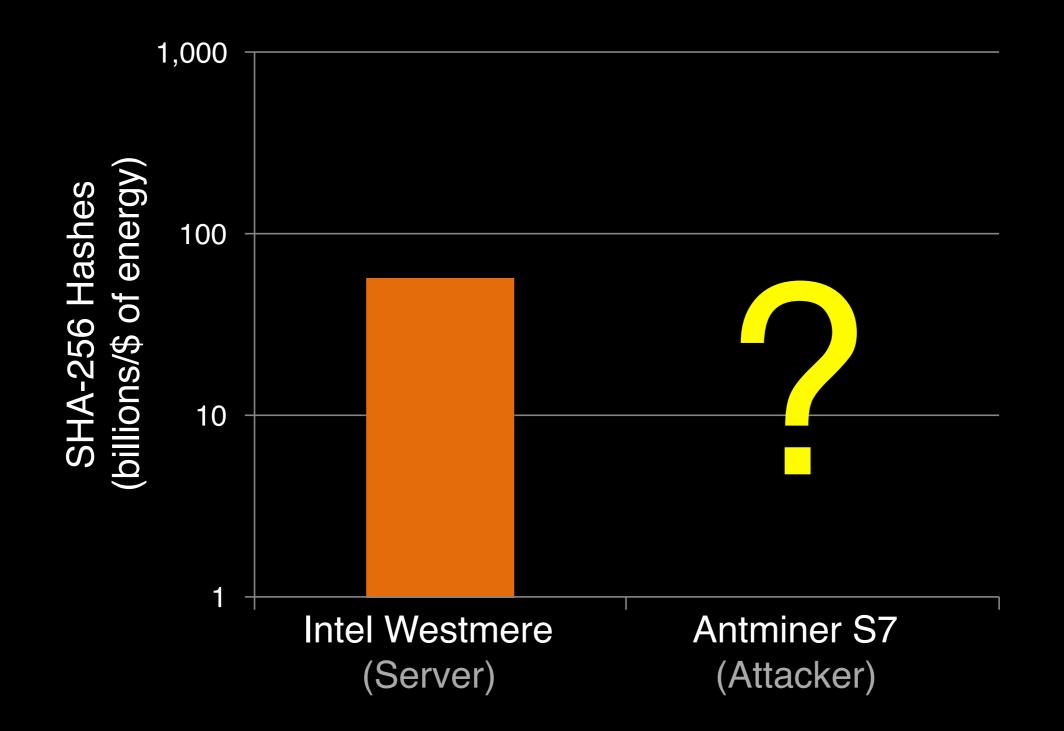
If the authentication server can compute... X hashes per \$ of energy then an attacker *with custom hardware* should only be able to compute...

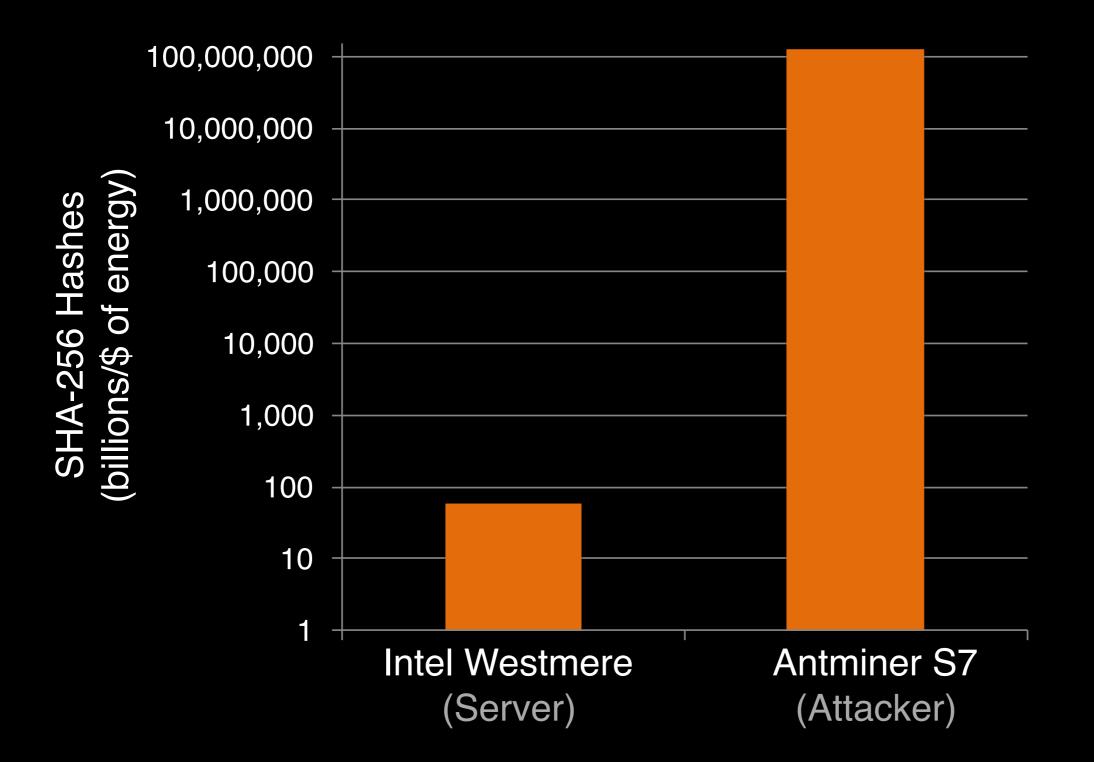
(1+ε)X hashes per

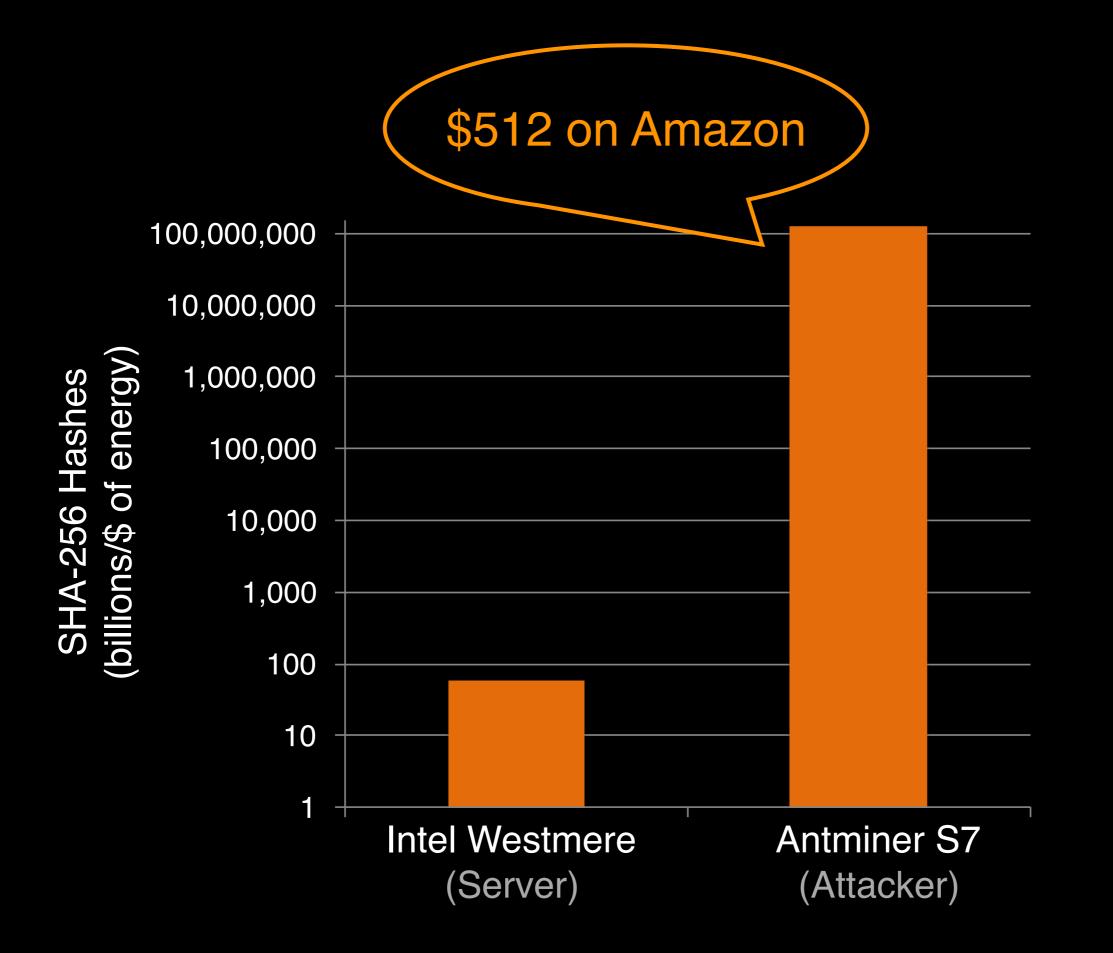
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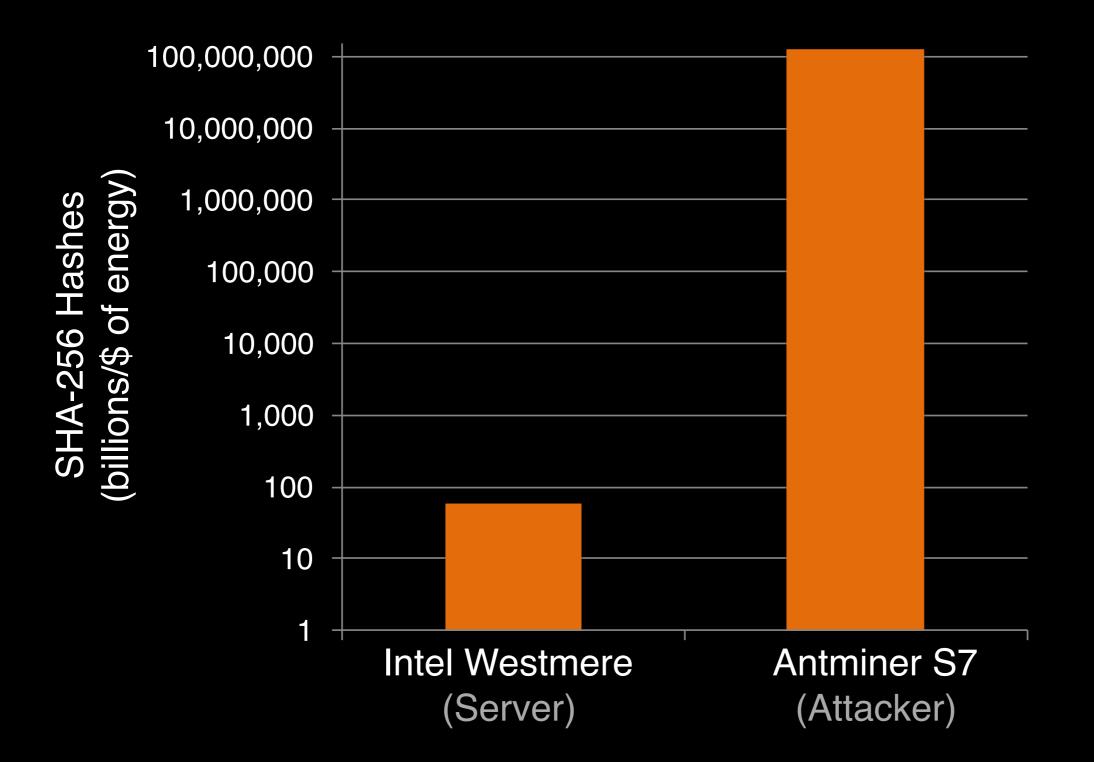
By this metric, conventional hash functions (e.g., SHA-256) are far from optimal!

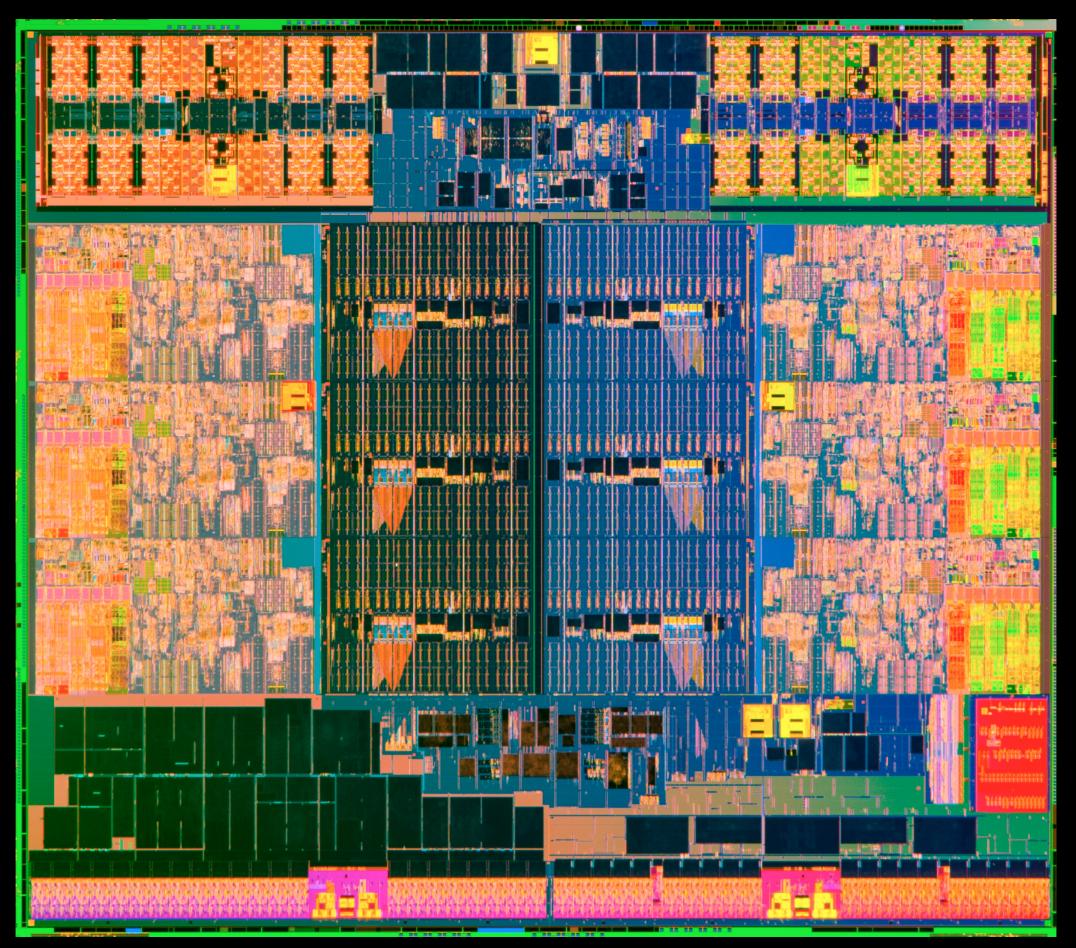




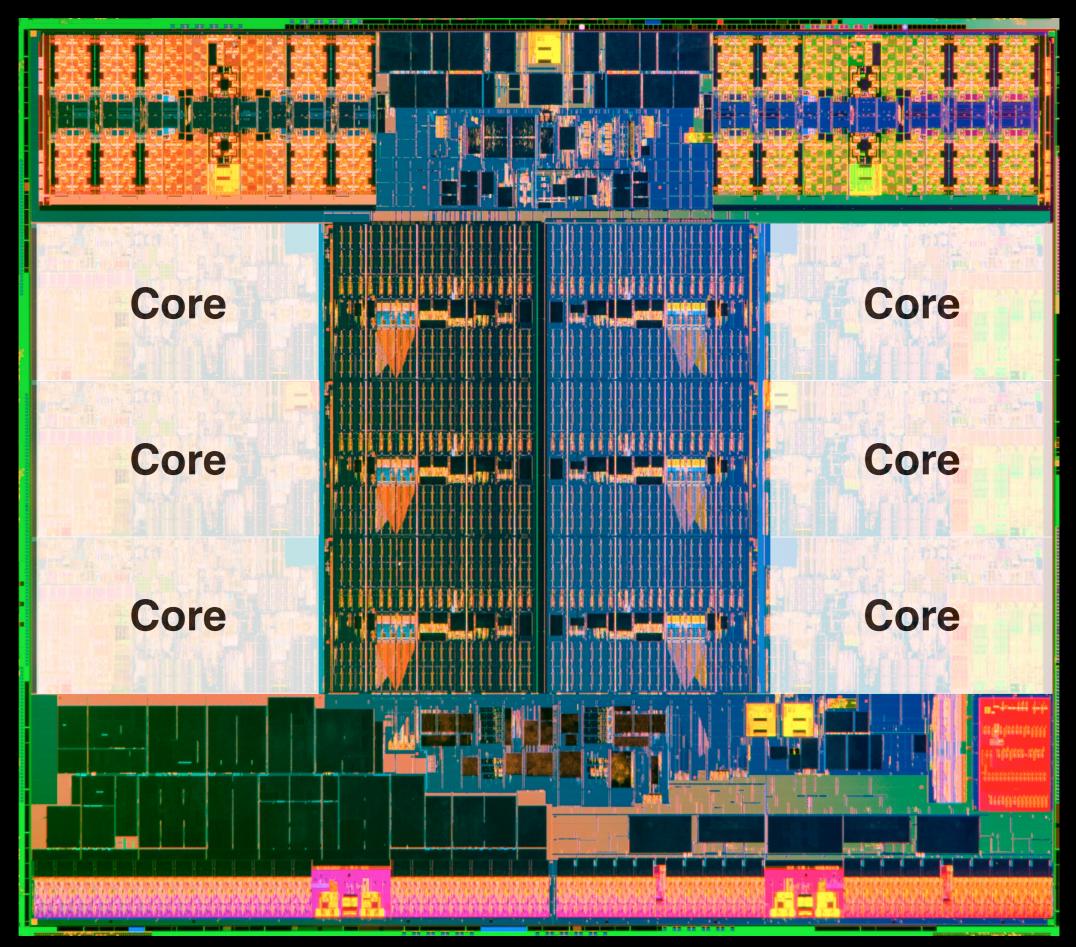


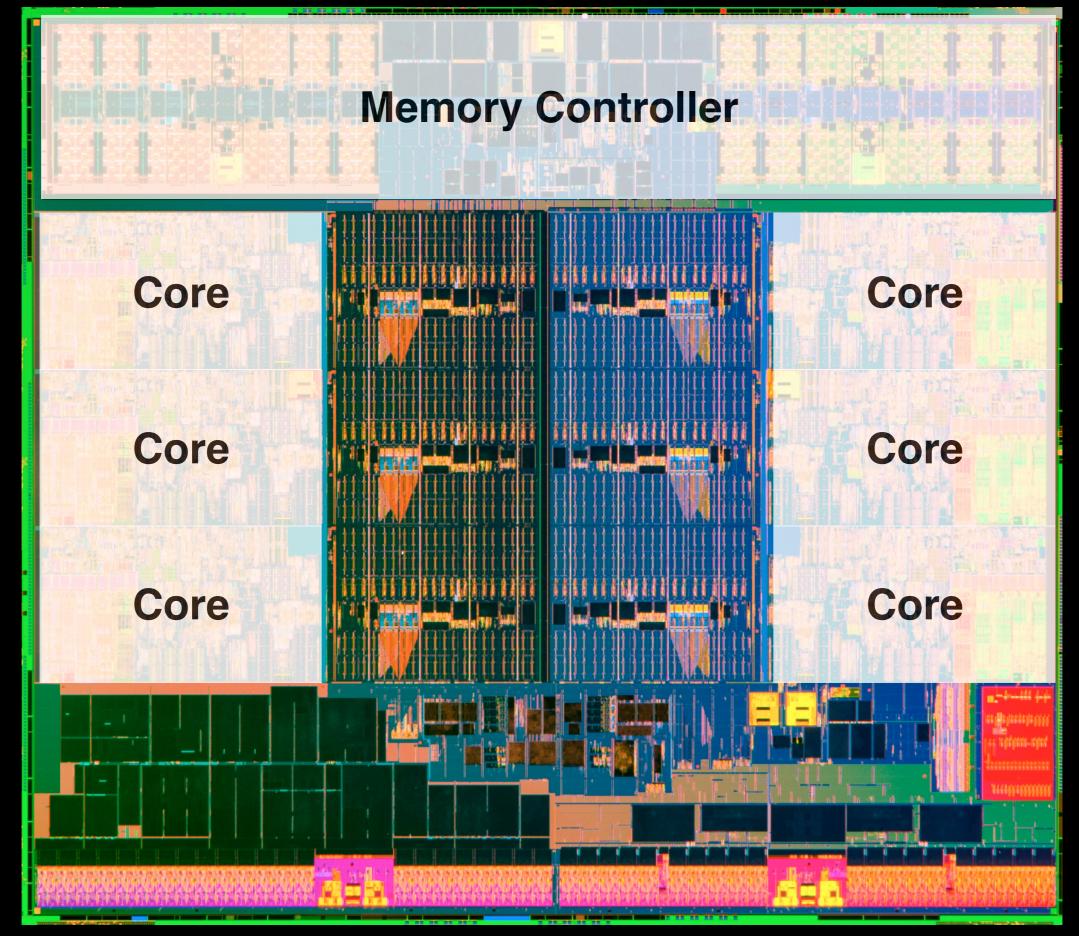


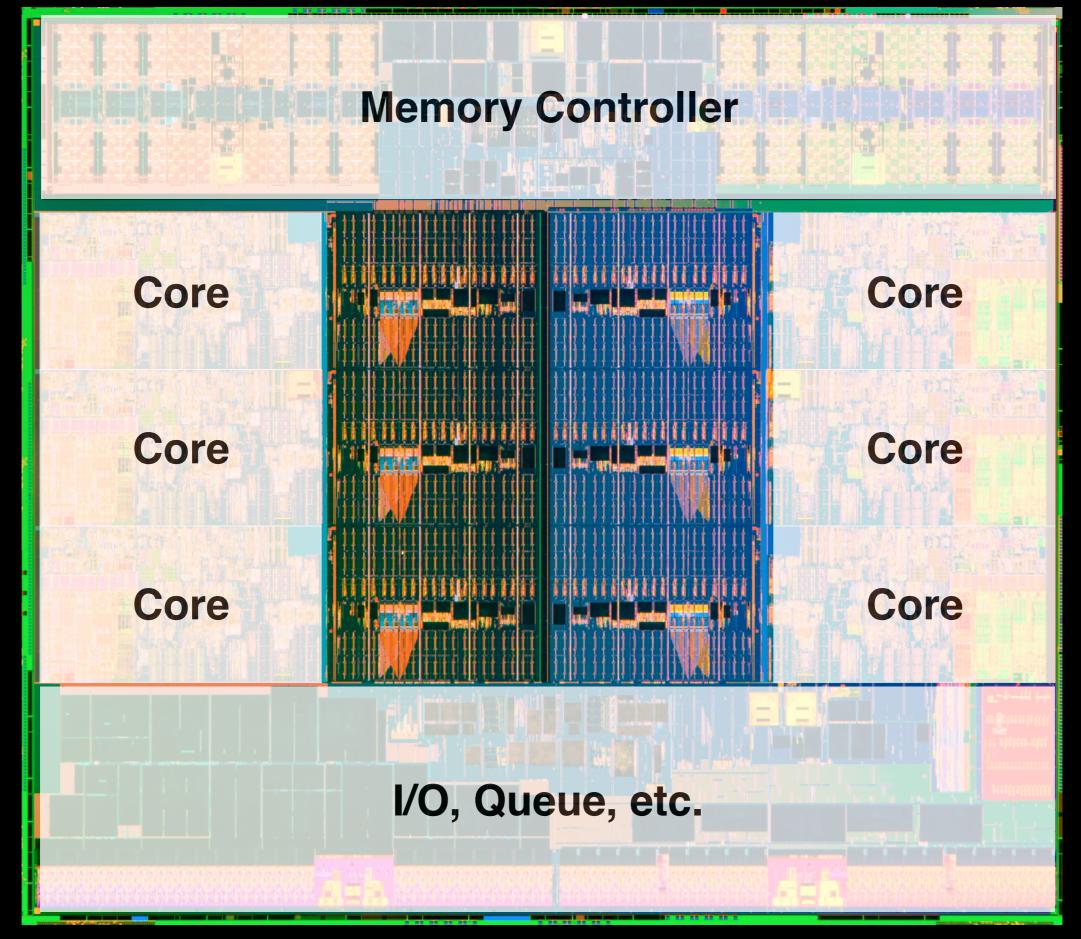


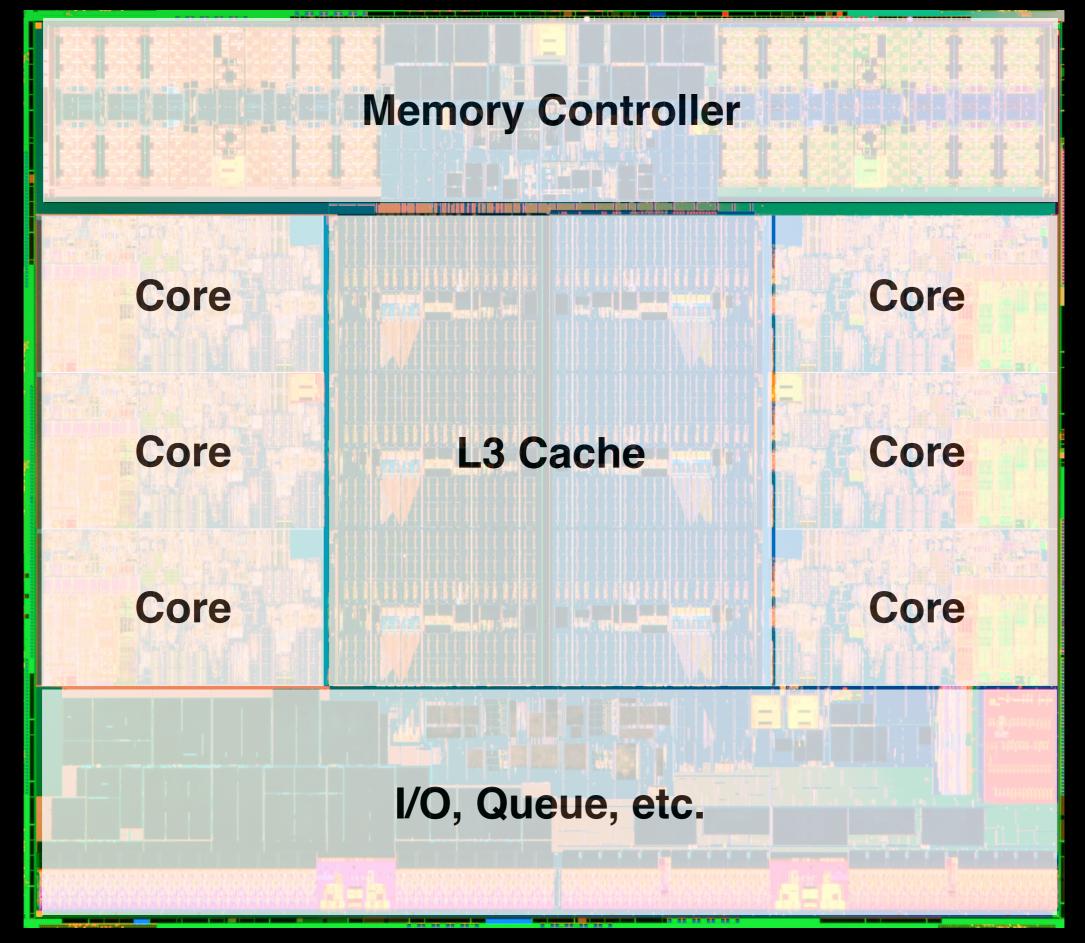


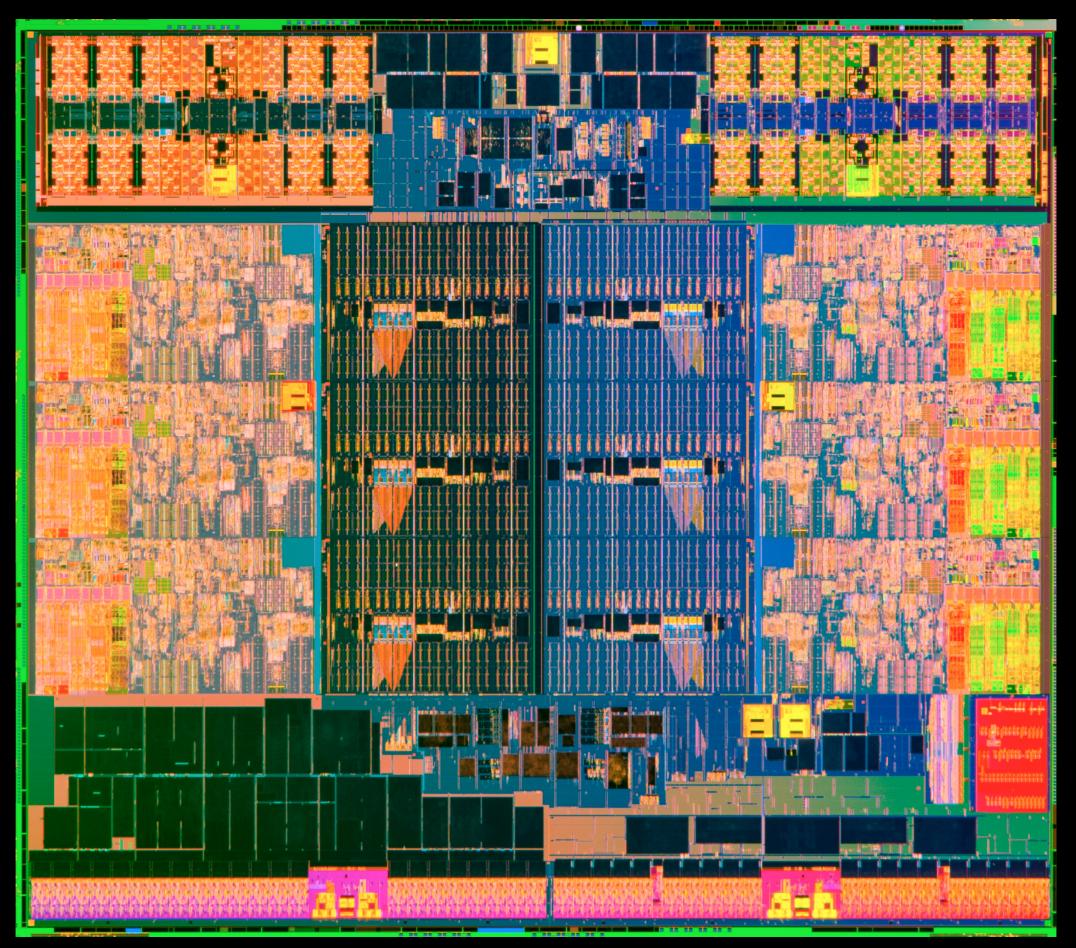
Intel Ivy Bridge-E Core i7-4960X http://kylebennett.com/files/hfpics/IVB-E_%28LCC%29_Die_Wafer_Shot-7837.jpg



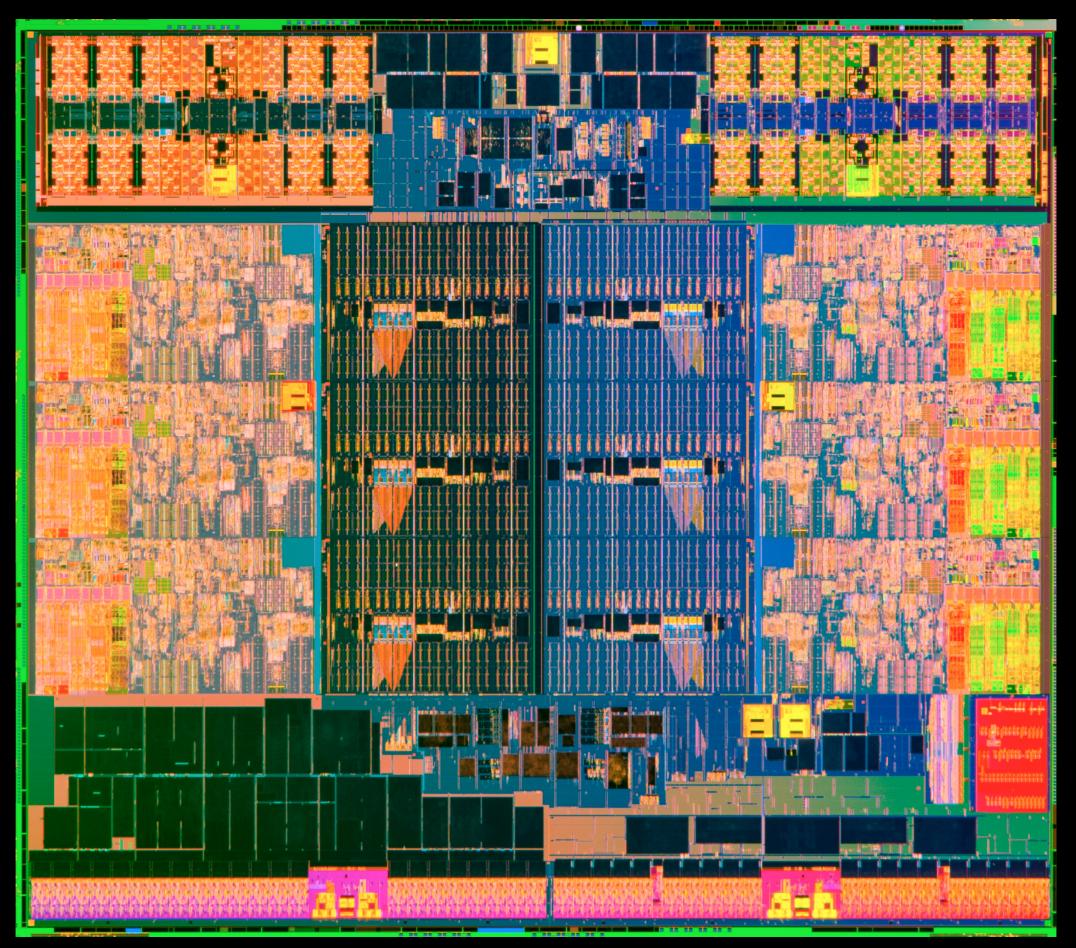




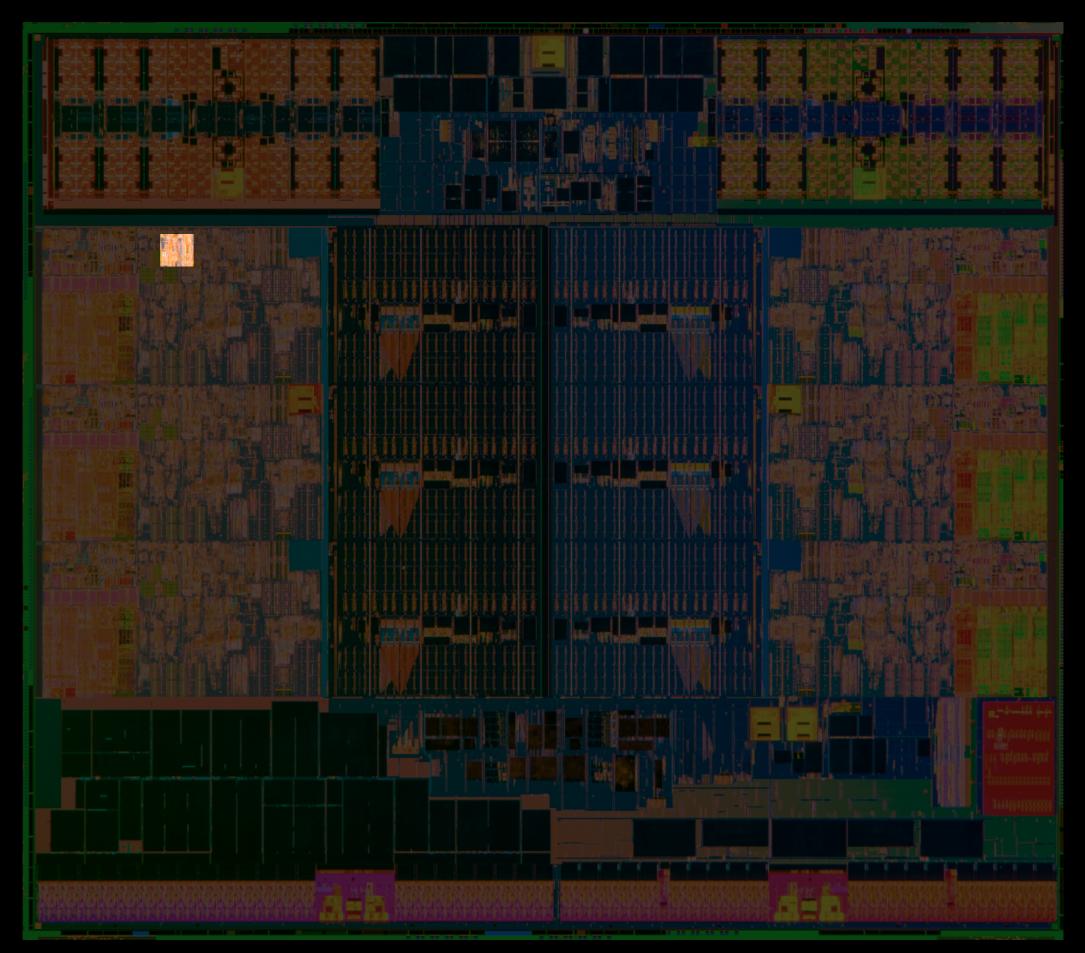




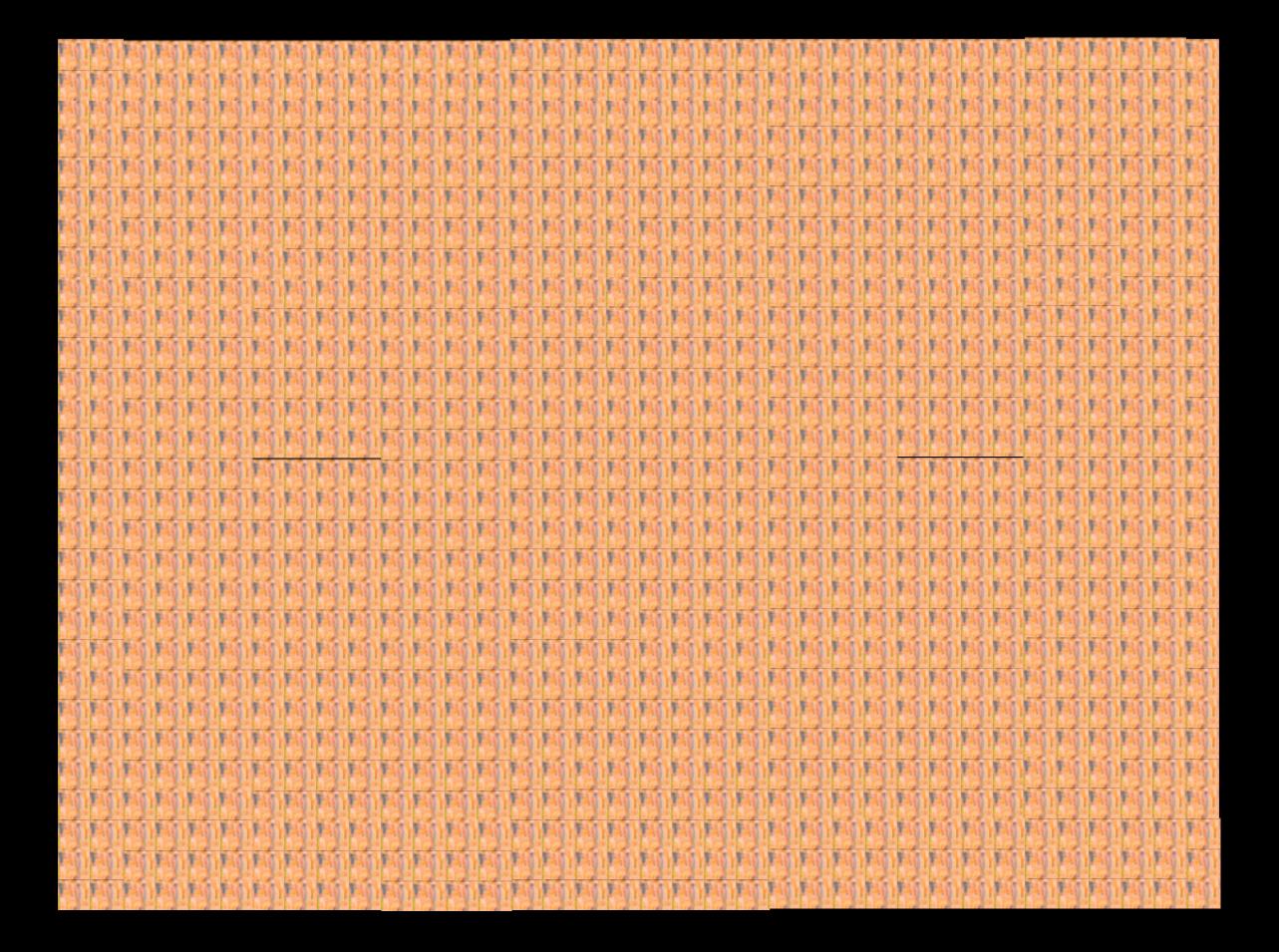
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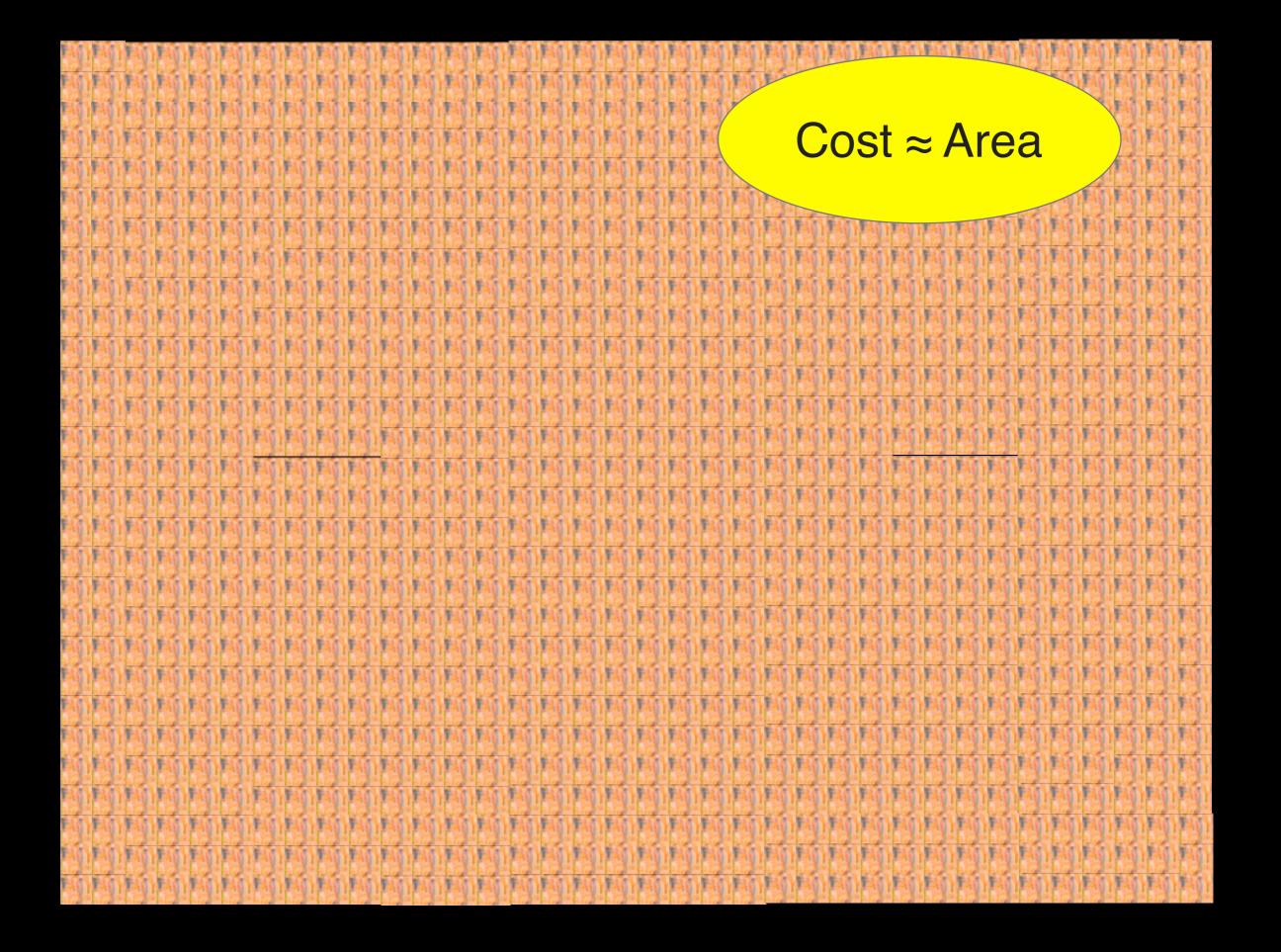


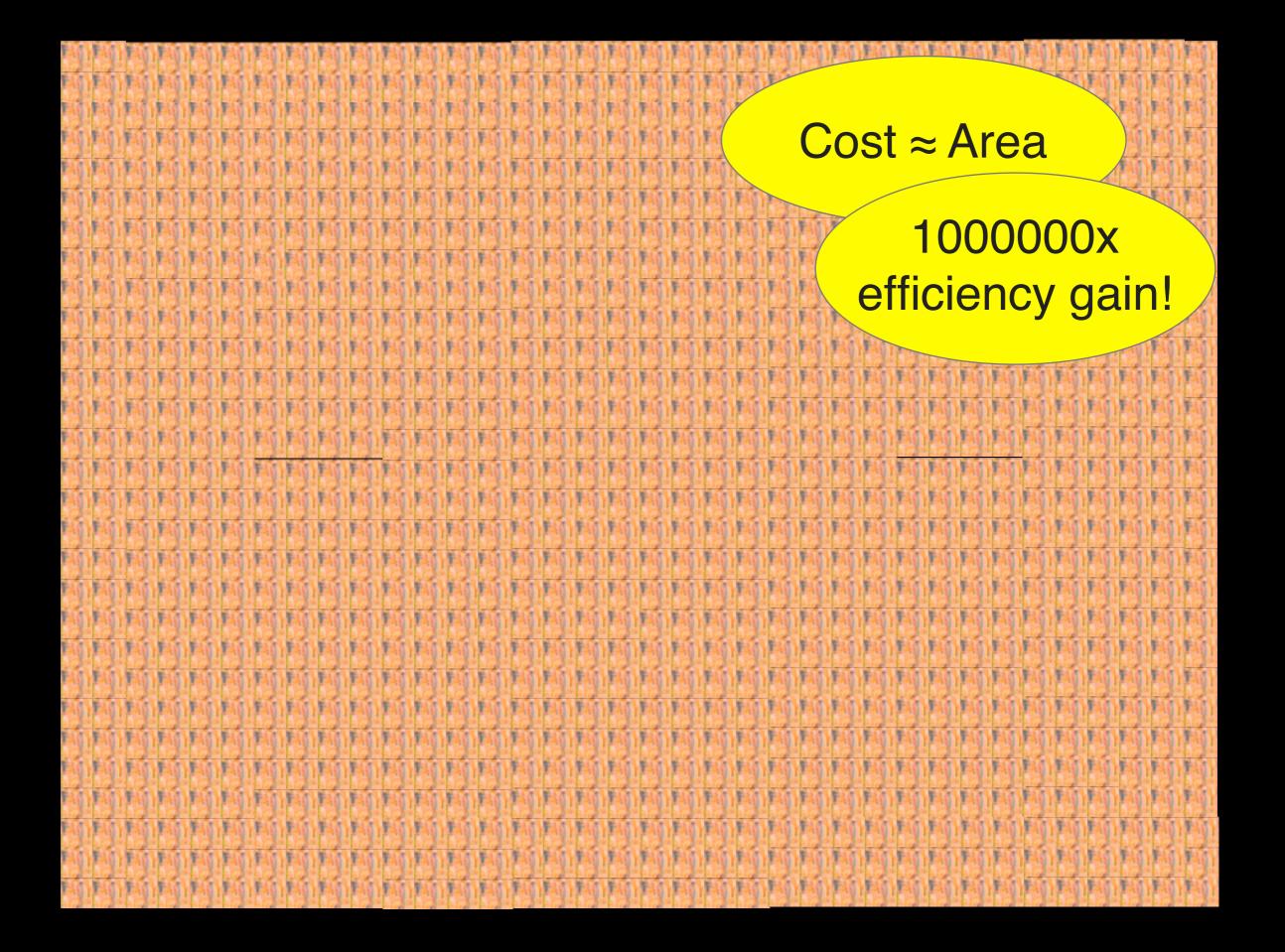
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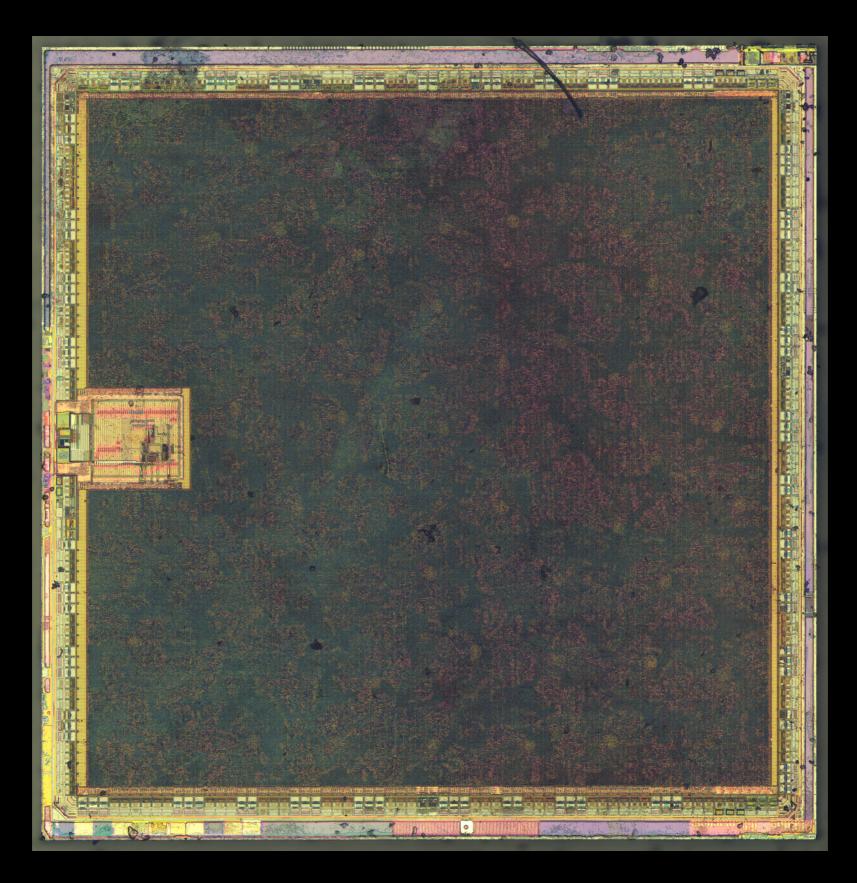


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Memory-hard functions use a large amount of working space during their computation

- → Attacker must keep caches on chip
- → Decreases the advantage of special-purpose HW

[Reinhold 1999], [Dwork, Goldberg, Naor 2003], [Abadi et al. 2005], [Percival 2009]

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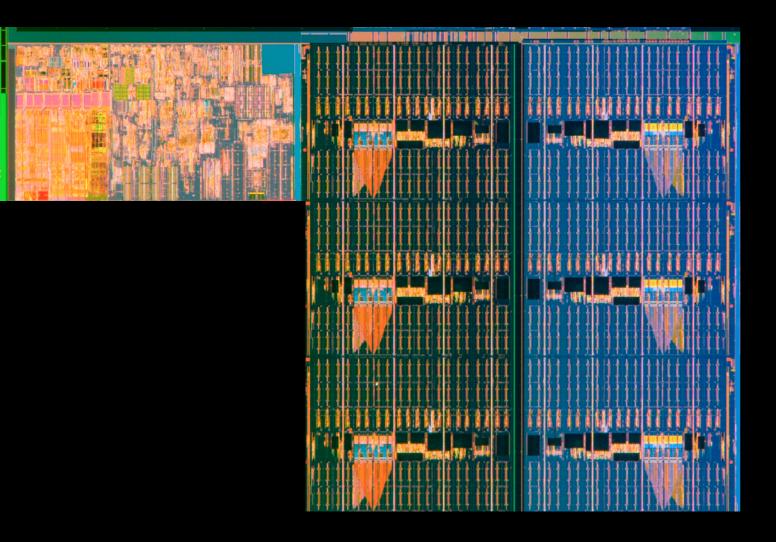
Typical technique:

- 1. Fill fill buffer with pseudo-random bytes
- 2. Mix read and write pseudo-random blocks in buffer
- 3. Extract extract function output from buffer contents

Without memory-hardness



Without memory-hardness



With memory-hardness

- I. Background on password hashing
- II. Goals
- III. The Balloon algorithm
- IV. Discussion

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Goal 1: Memory-Hardness

Random oracles: [Bellare & Rogaway 1993] Memory-hard functions: [Abadi et al. 2005] [Percival 2009]

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Informally, a memory-hard function, with hardness parameter N, requires space S and time T to compute, where

 $\mathbf{S} \cdot \mathbf{T} \in \Omega(\mathbb{N}^2)$

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Intuition: any adversary who tries to save space will pay a large penalty in computation time.

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Goal 3: Real-World Practical

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Goal 3: Real-World Practical

 The hash should be able to support hundreds of logins per second while filling L2 cache (or more)

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Balloon(password, salt, N = space_cost, R = num_rounds):

 $\delta \leftarrow 3$ // A security parameter.

var $B_1, ..., B_N$ // A buffer of N blocks.

```
// Step 1: Fill Buffer

B_1 \leftarrow Hash(password, salt)

for i = 2, ..., N:

B_i \leftarrow Hash(B_{i-1})
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// Step 3: Extract return B_N

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// Step 2: Mix Buffer for r = 1, ..., R: for i = 1,..., N: // Chosen pseudorandomly from salt $(v_1, ..., v_{\delta}) \leftarrow Hash(salt, r, i) \in Z_N^{\delta}$ $B_i \leftarrow Hash(B_{(i-1 \mod N)}, B_i, B_{v_1}, ..., B_{v_{\delta}})$

A conventional hash function (e.g., SHA-256)

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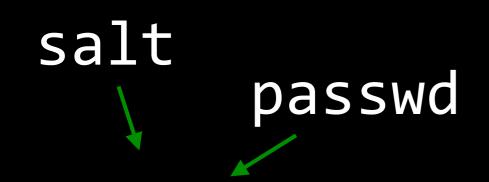
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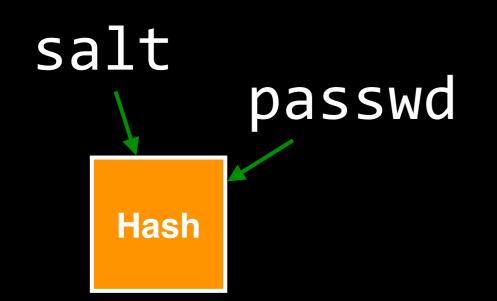
for i = 2, ..., N:

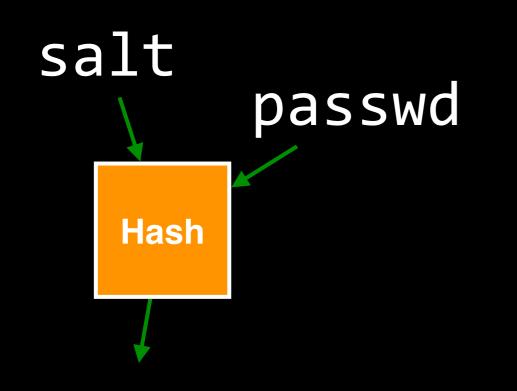
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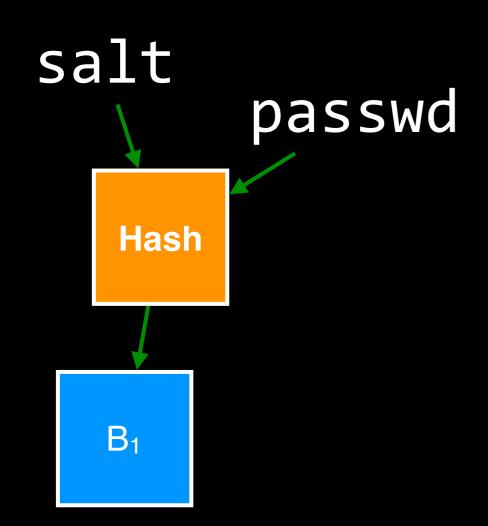
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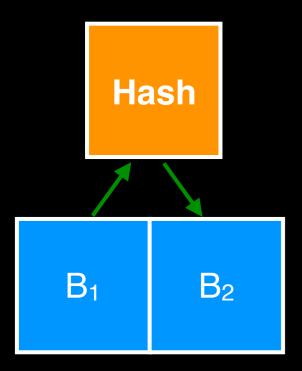
salt passwd

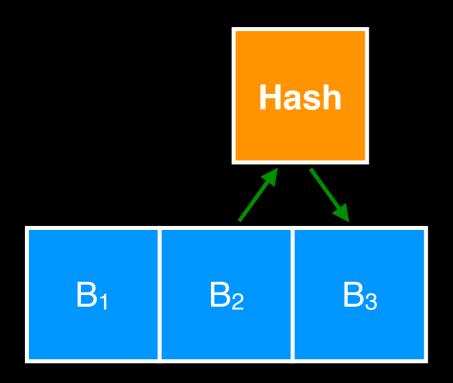


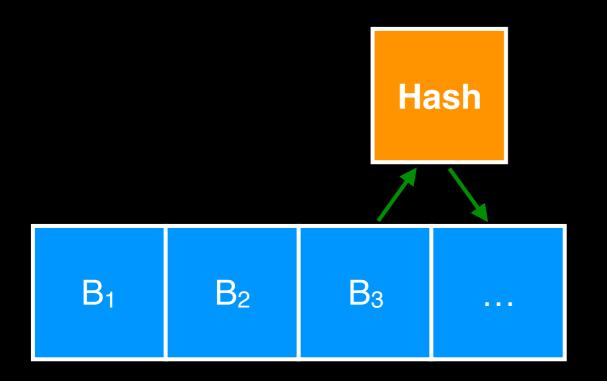




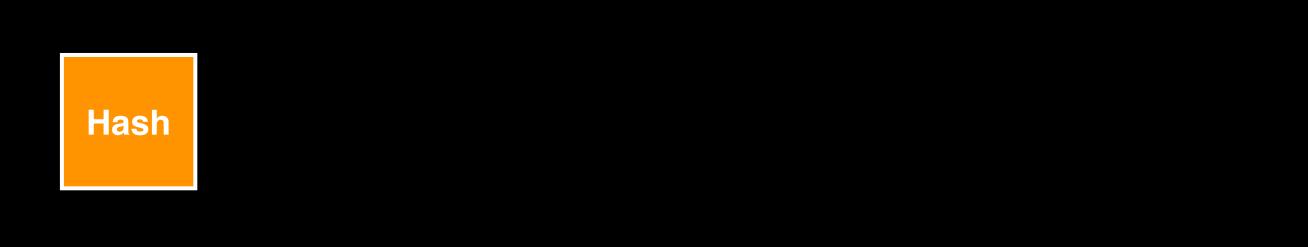




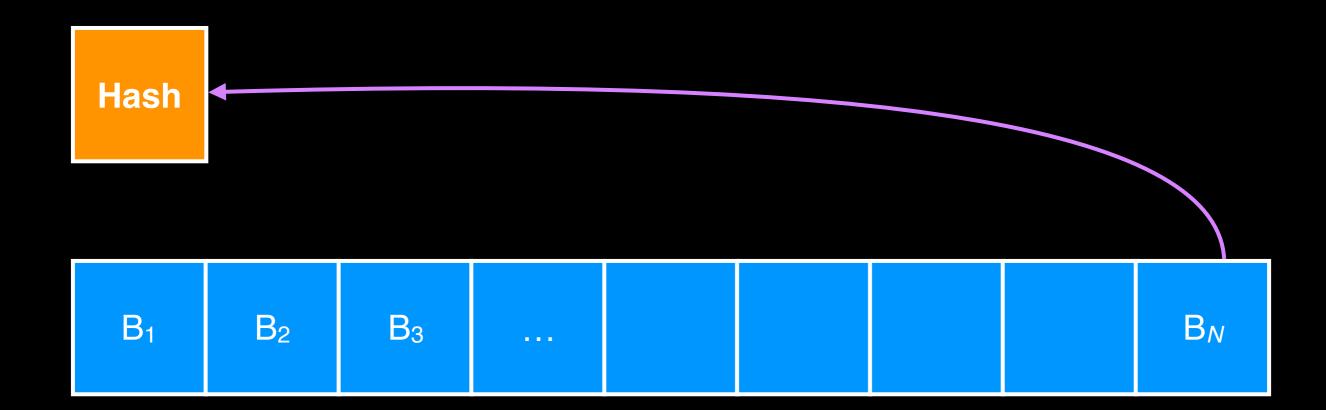


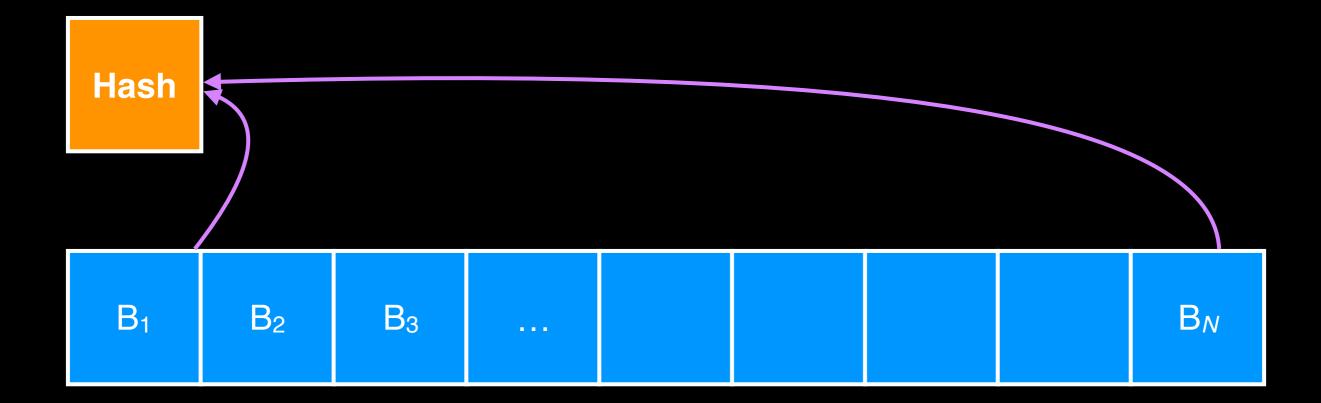


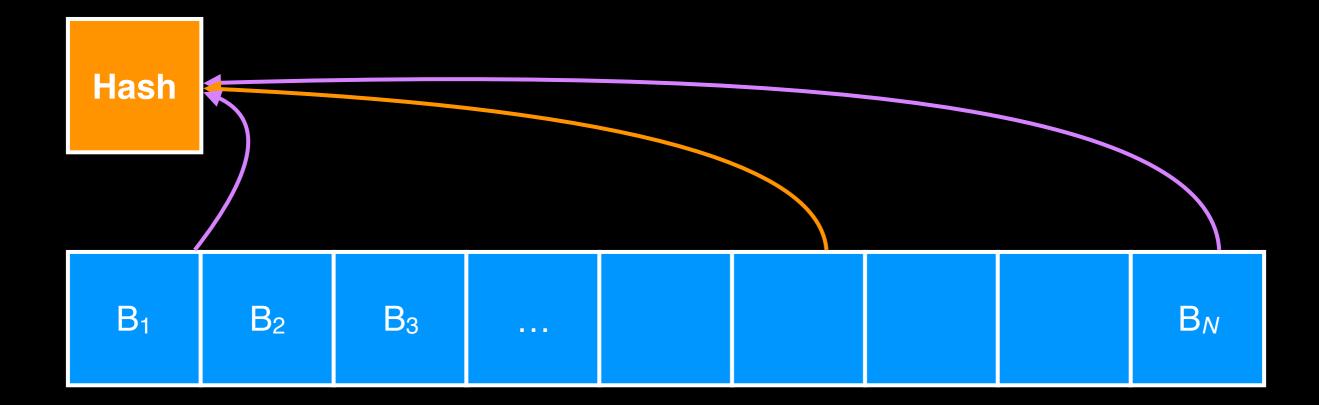


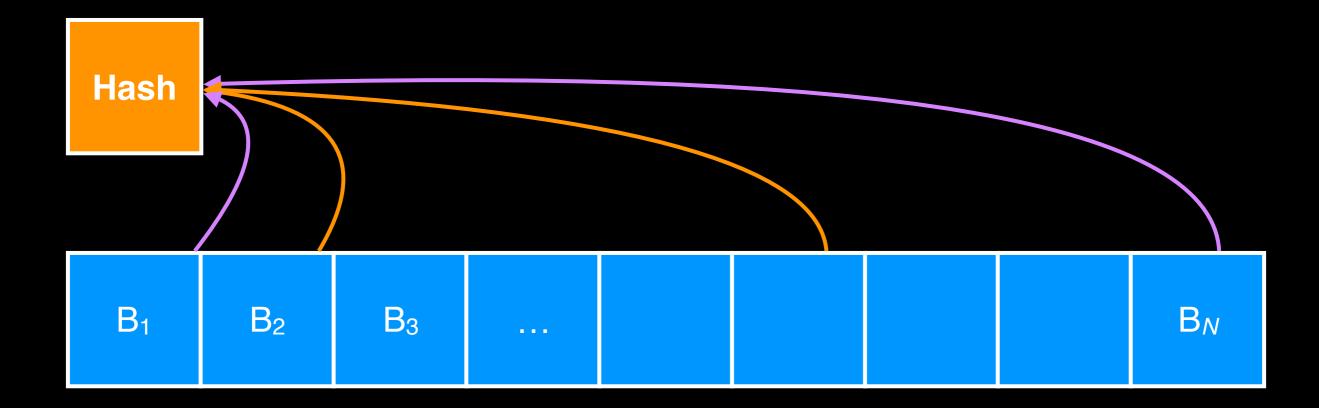


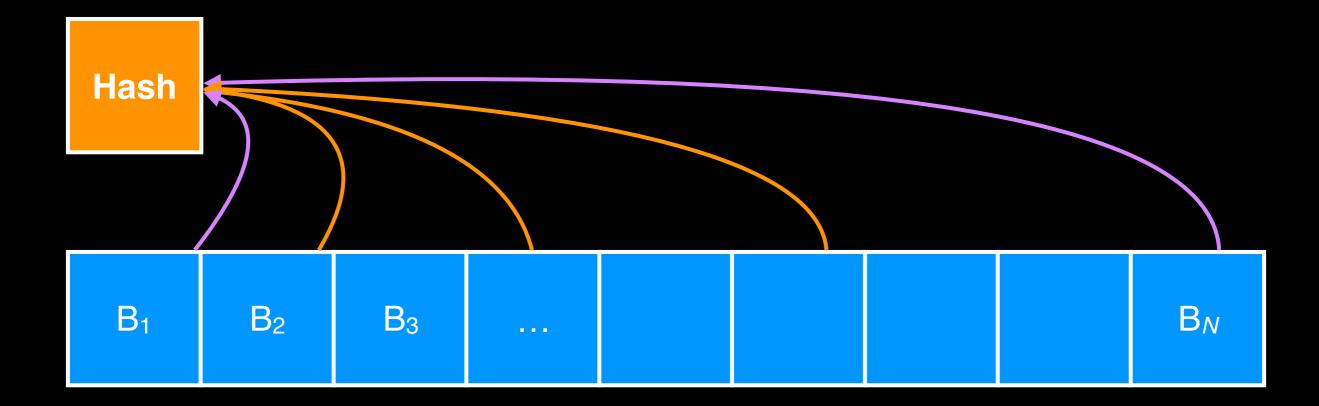
B ₁	B ₂	B ₃						B _N
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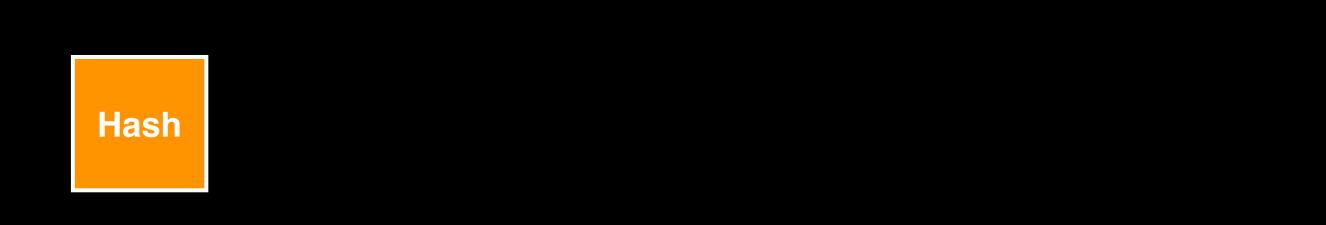




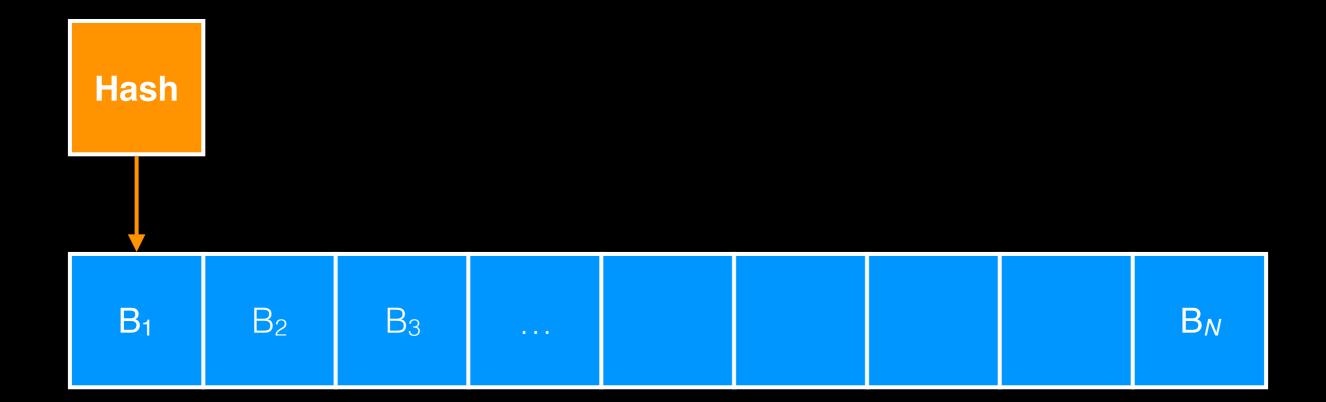


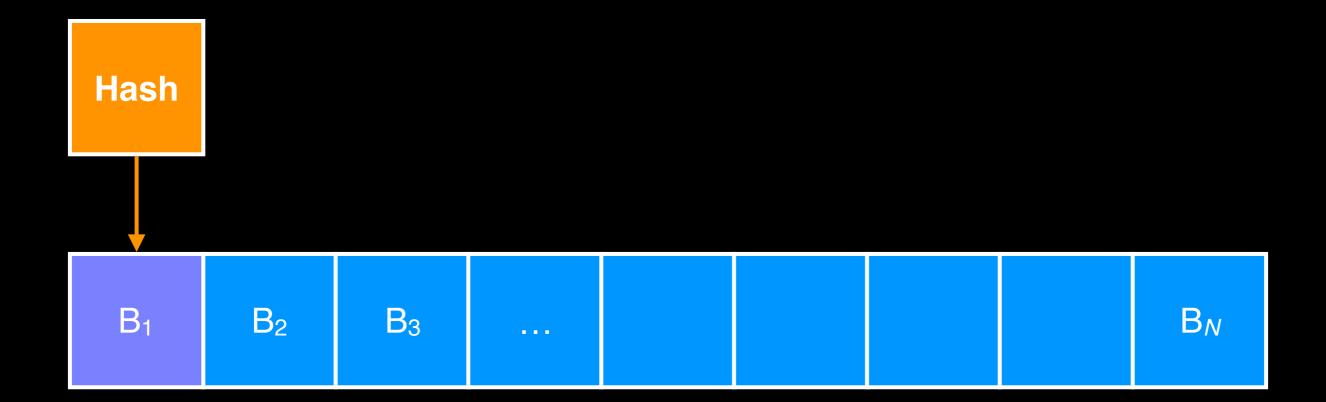






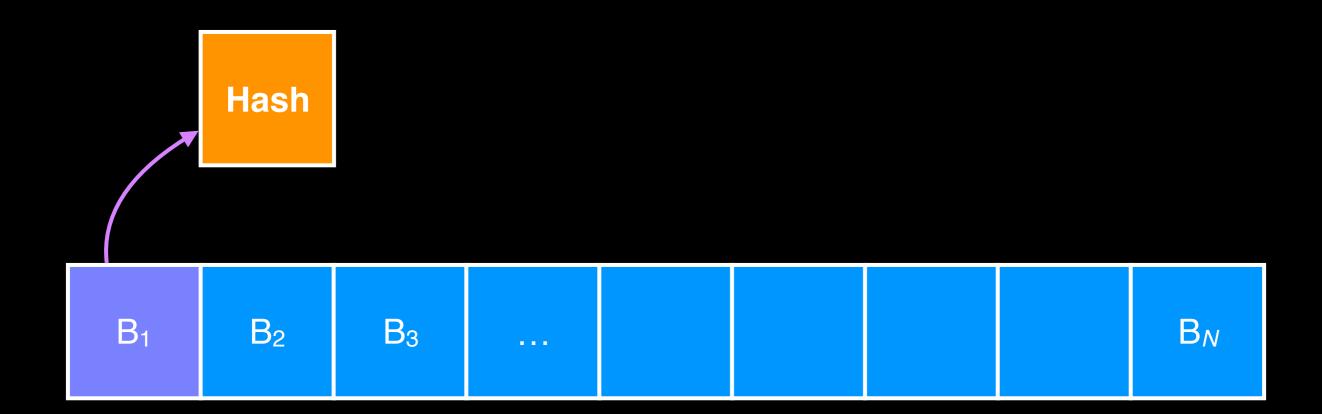
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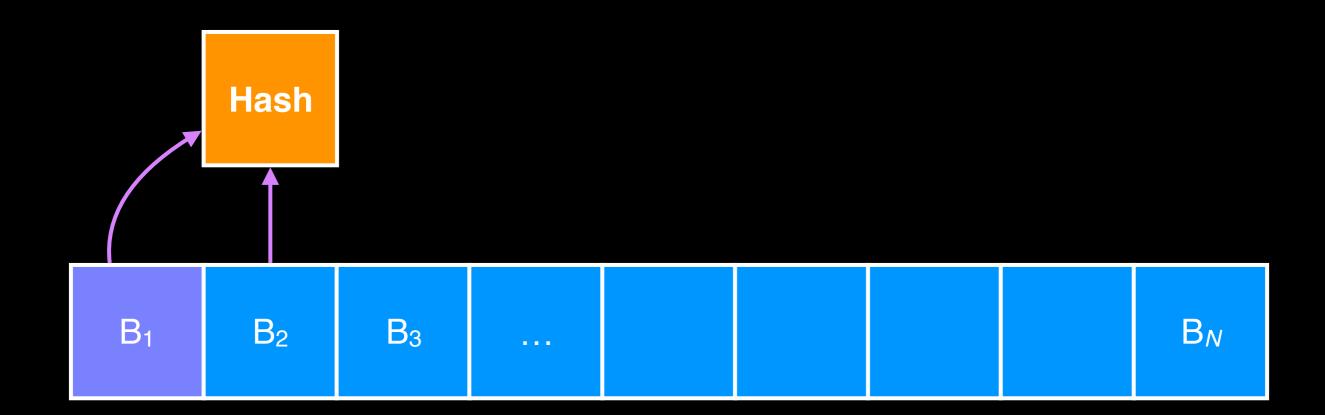


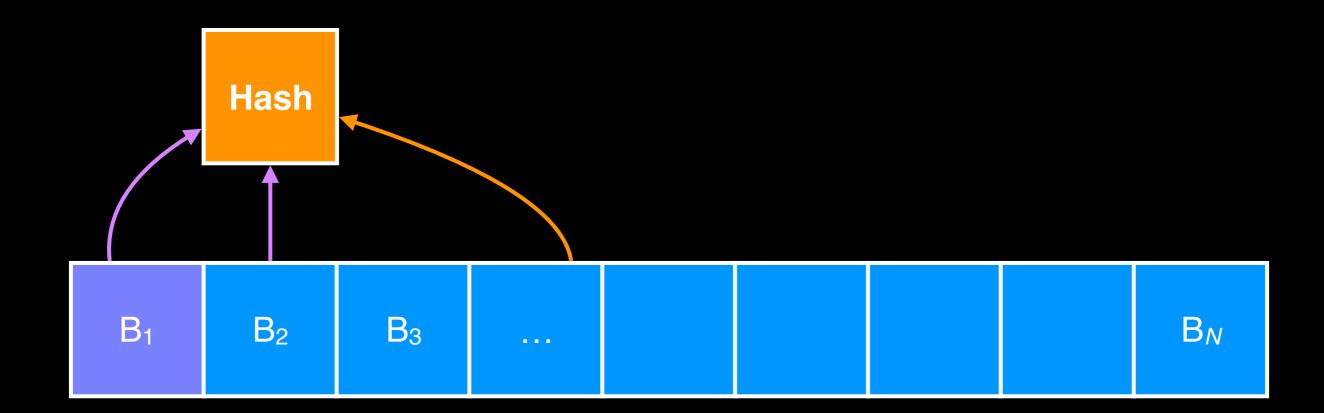


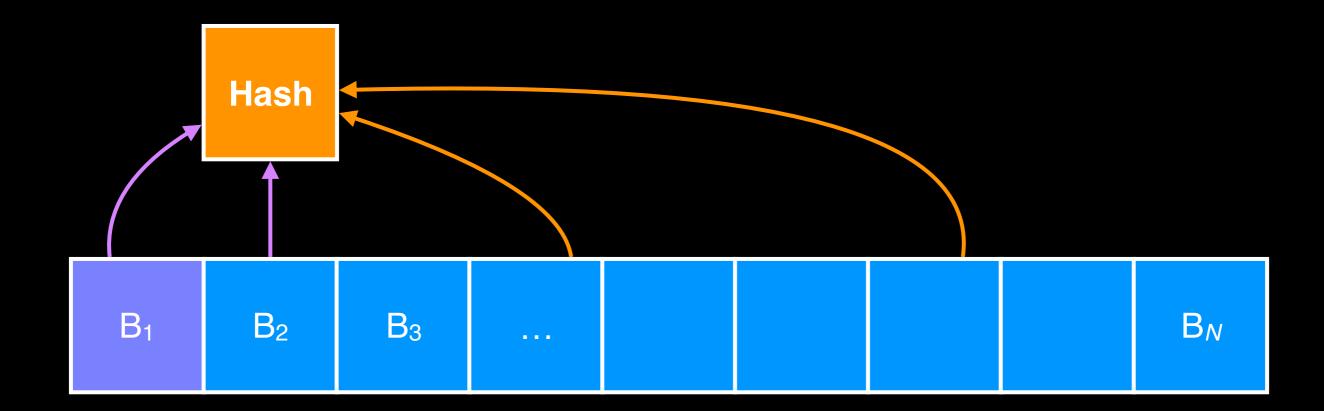


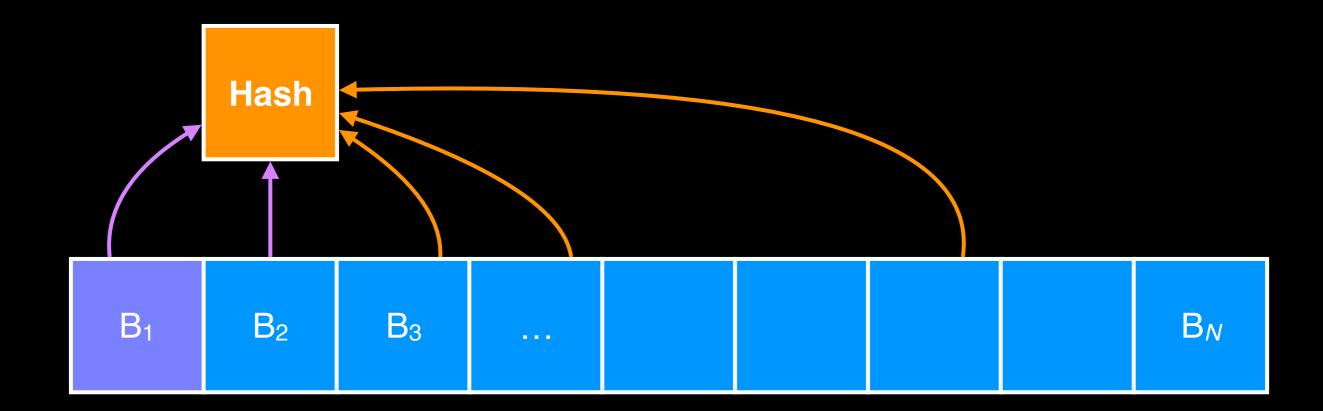
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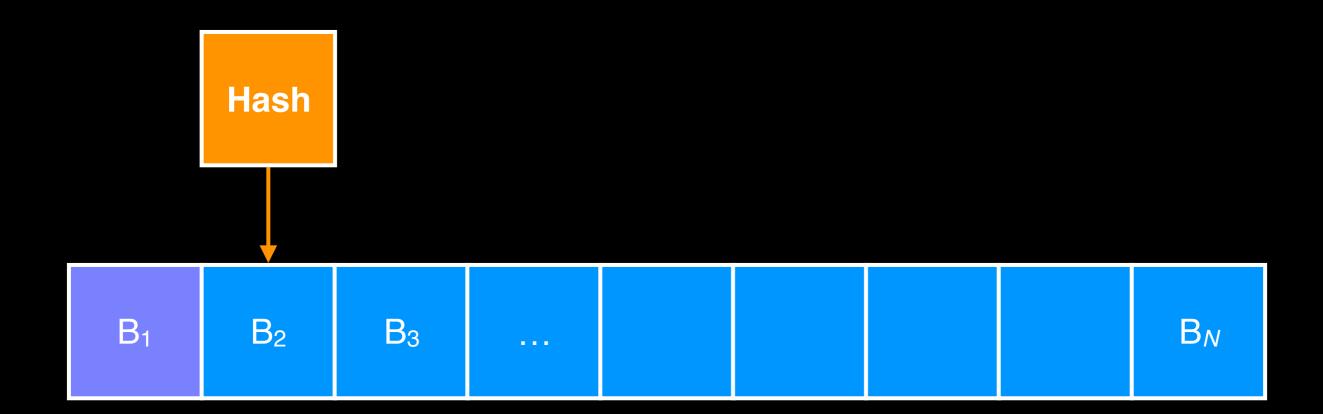


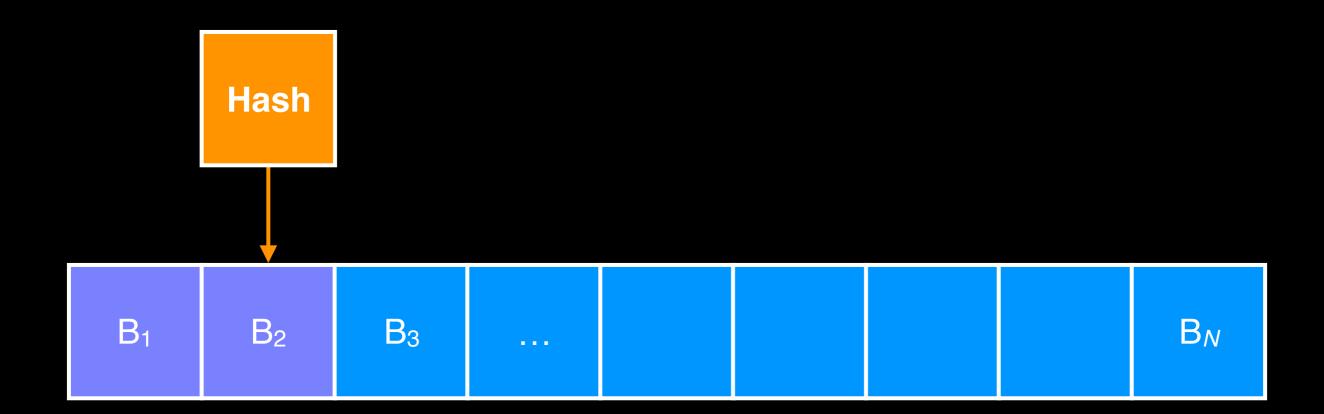






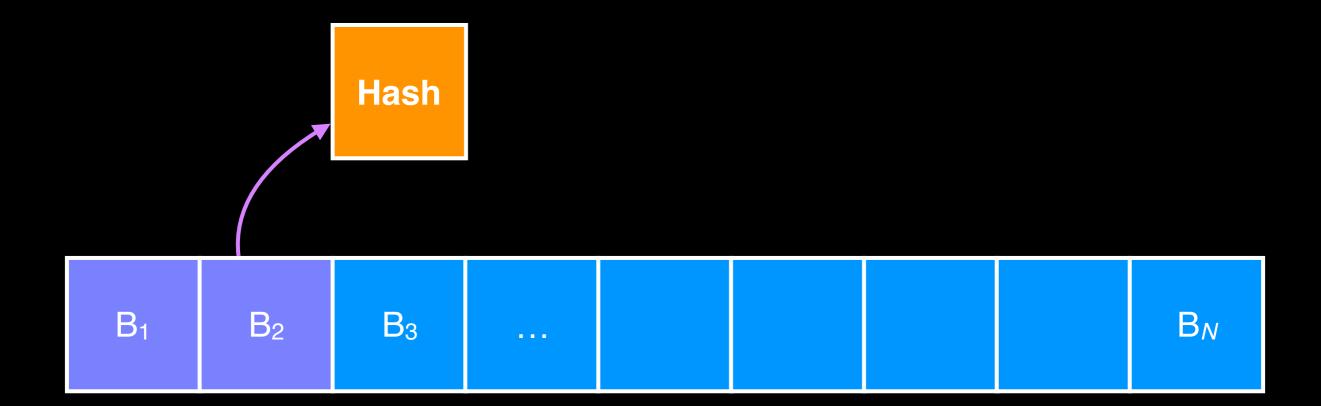
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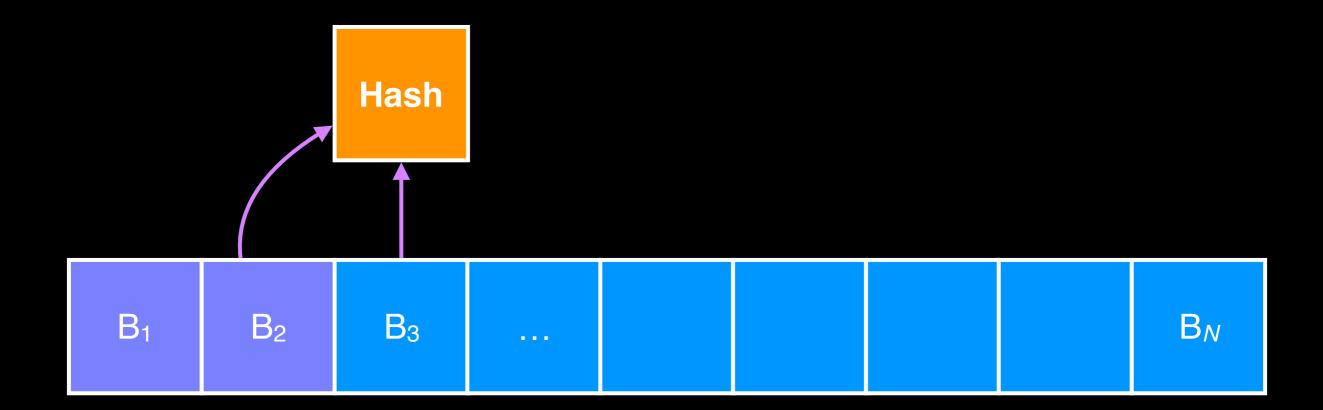


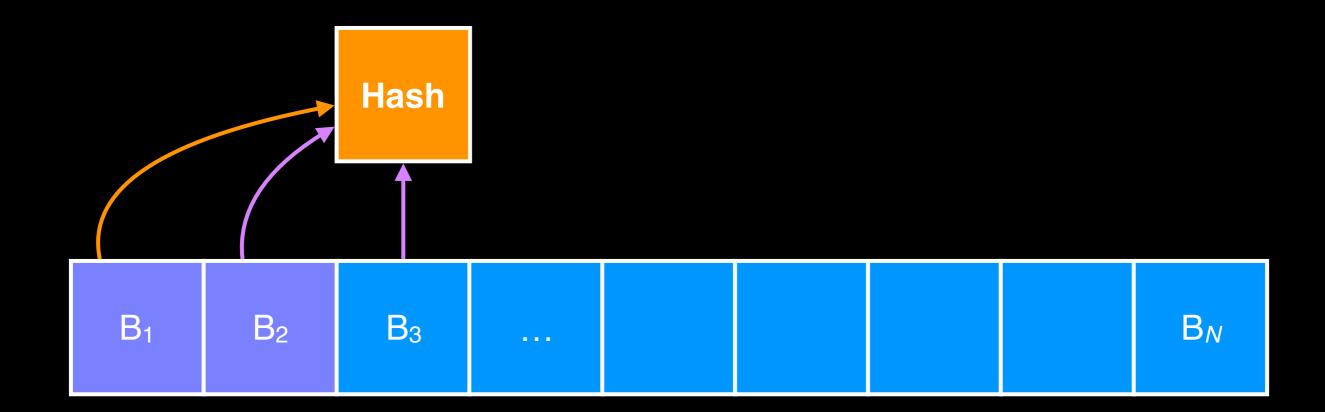


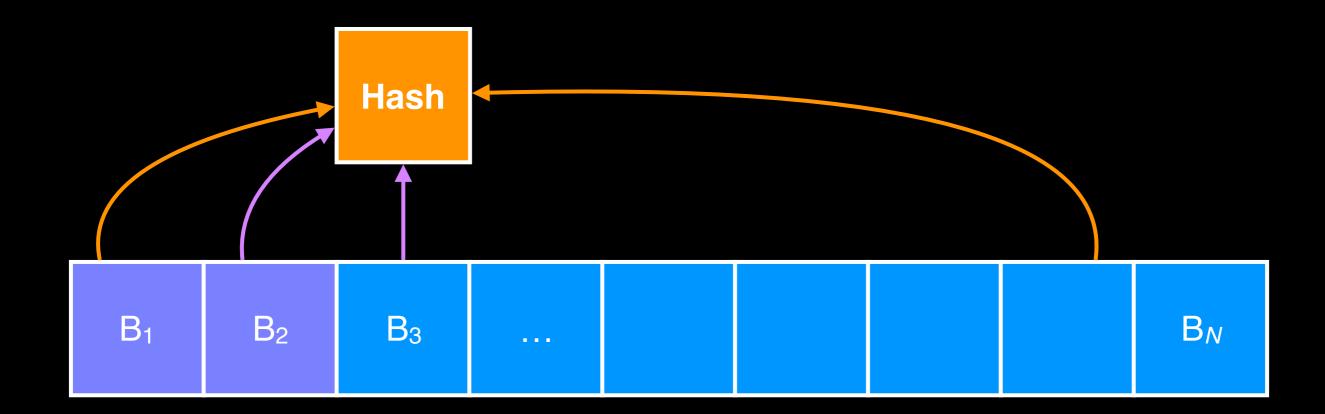


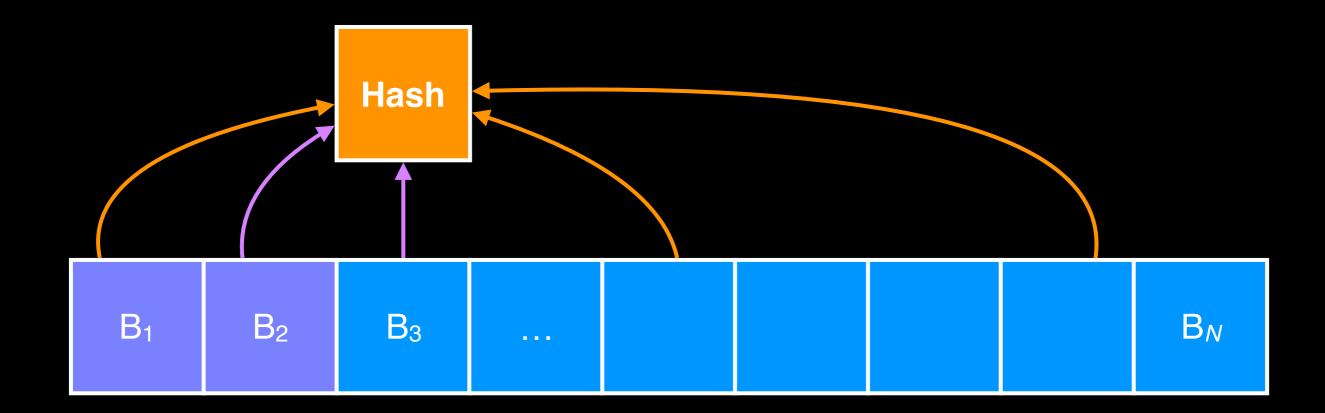
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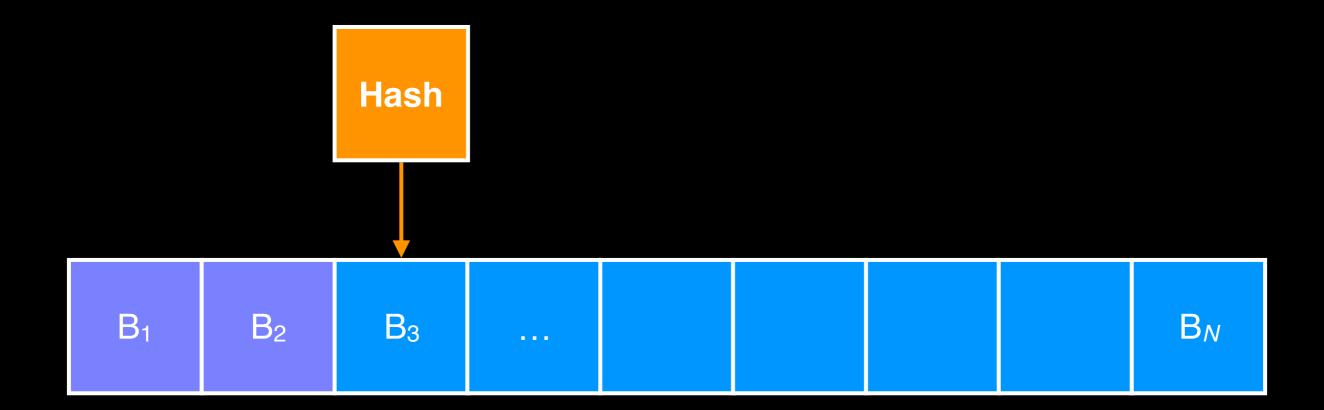


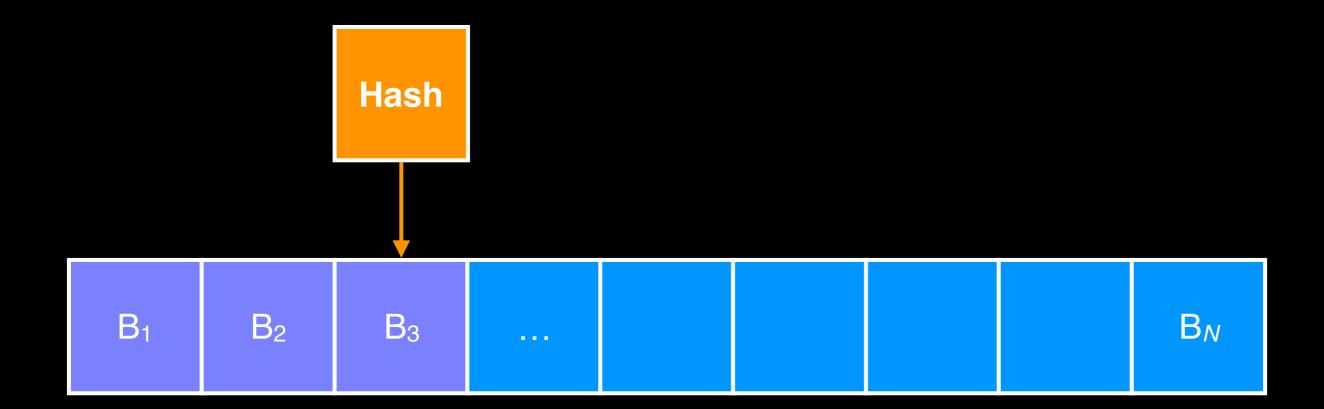


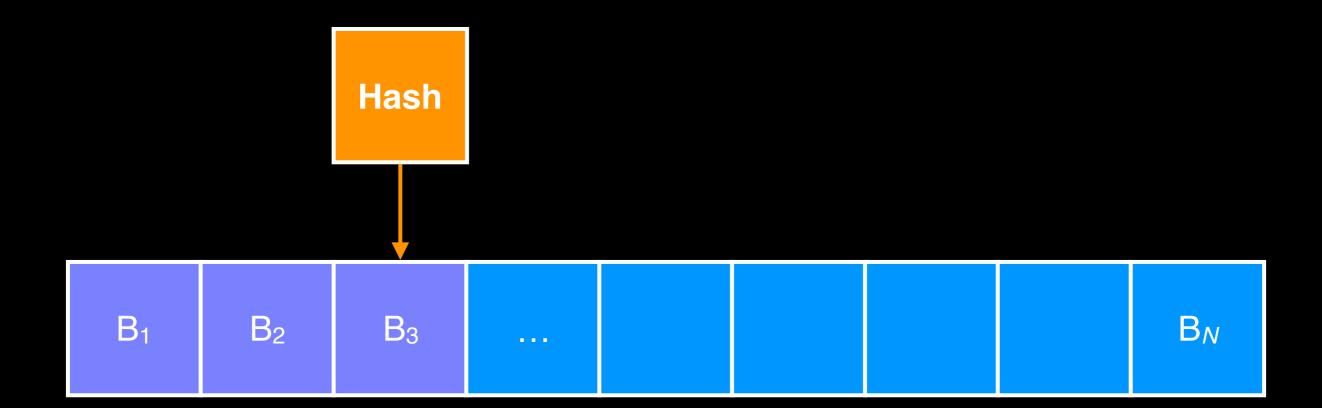




B ₁	B ₂	B ₃			B _N







A "mode of operation" for a cryptographic hash function

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A password hashing function the challenge

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<u>Theorem</u> [informal]: Computing the N-block R-round Balloon function w.h.p., when $\delta=7$, with space $S \leq N/8$ requires time T such that

 $S \cdot T \ge (2^R - 1) / 8 \cdot N^2$.

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Saving a factor of 8 in space causes a slowdown **exponential** in *#* rounds

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When R=20, using 8× less space requires using 60,000× more time

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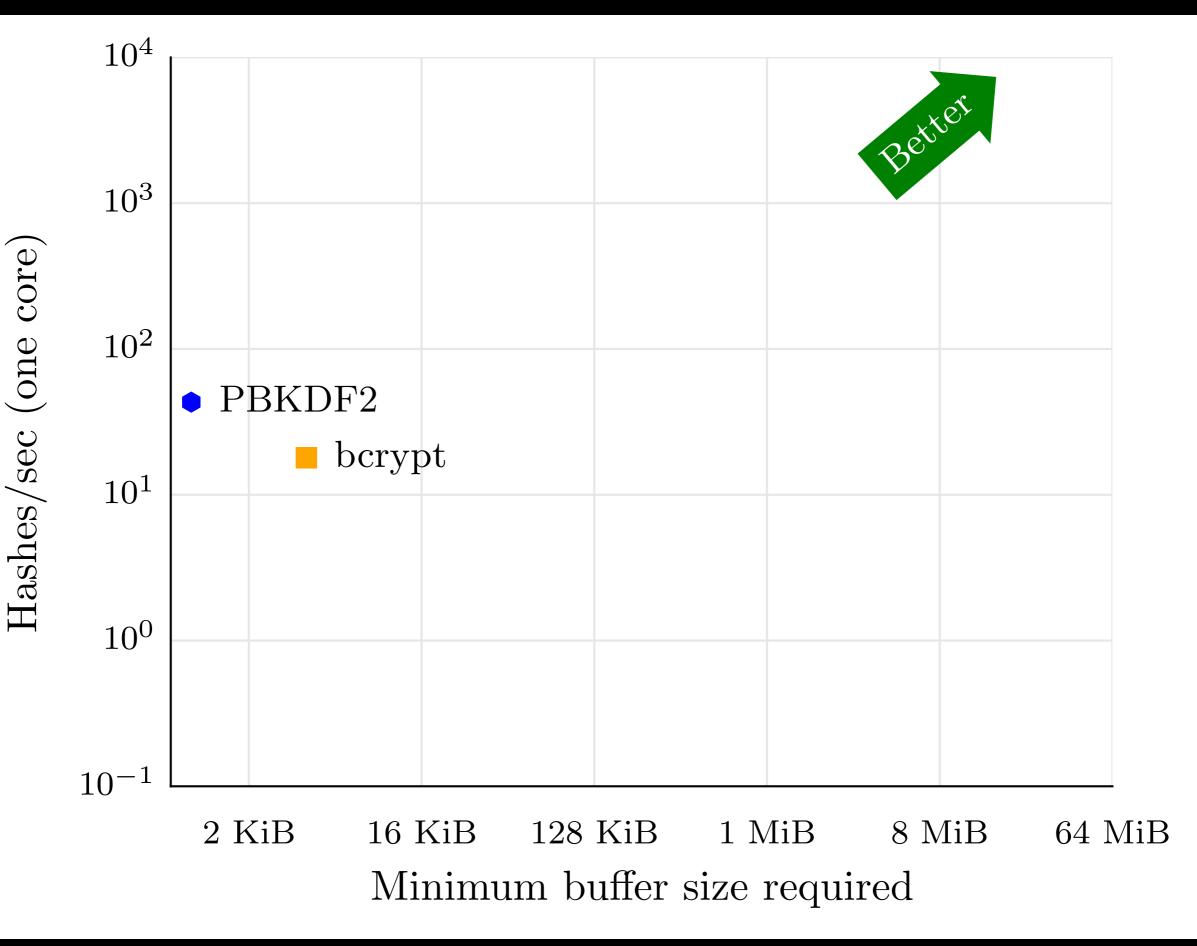
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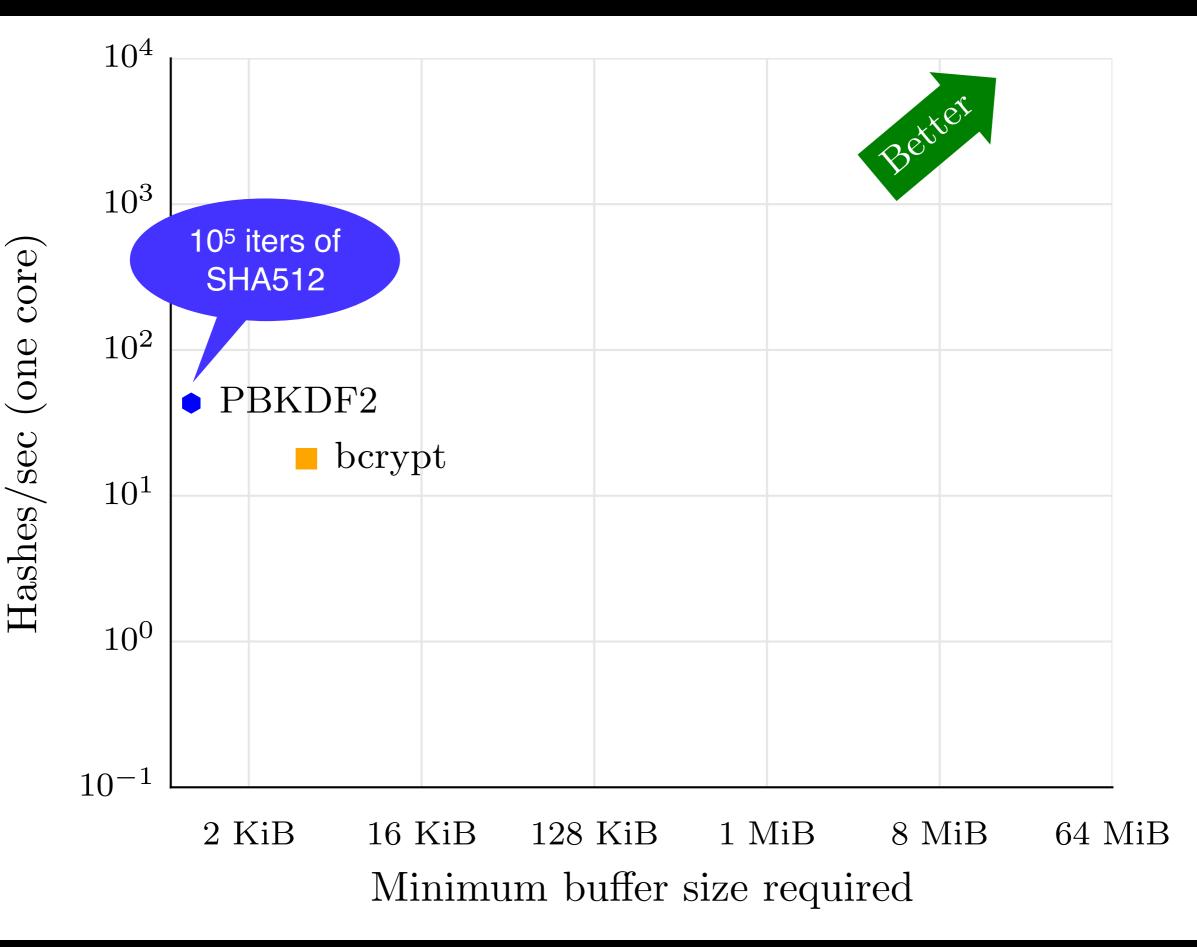
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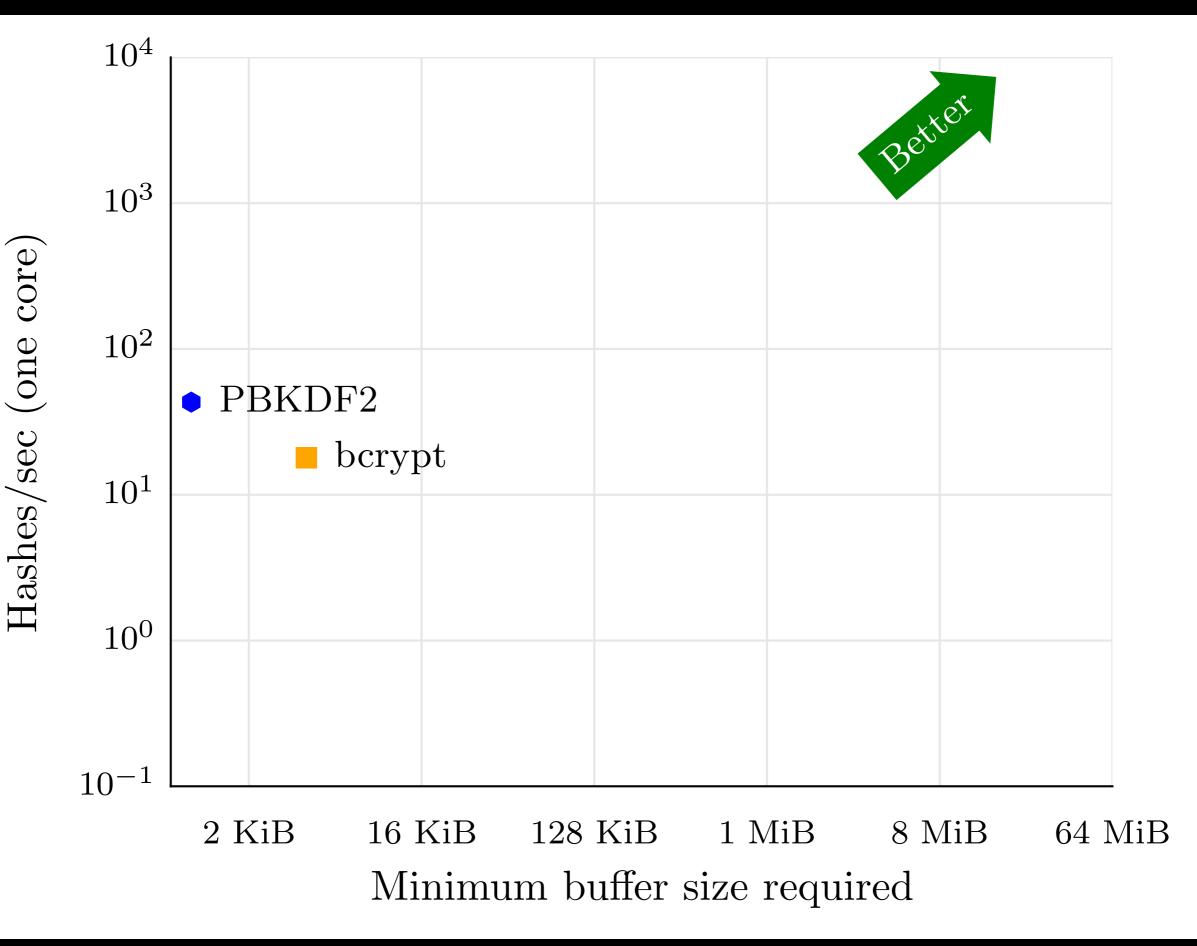
The proof works by inspecting the Balloon computation's datadependency graph.

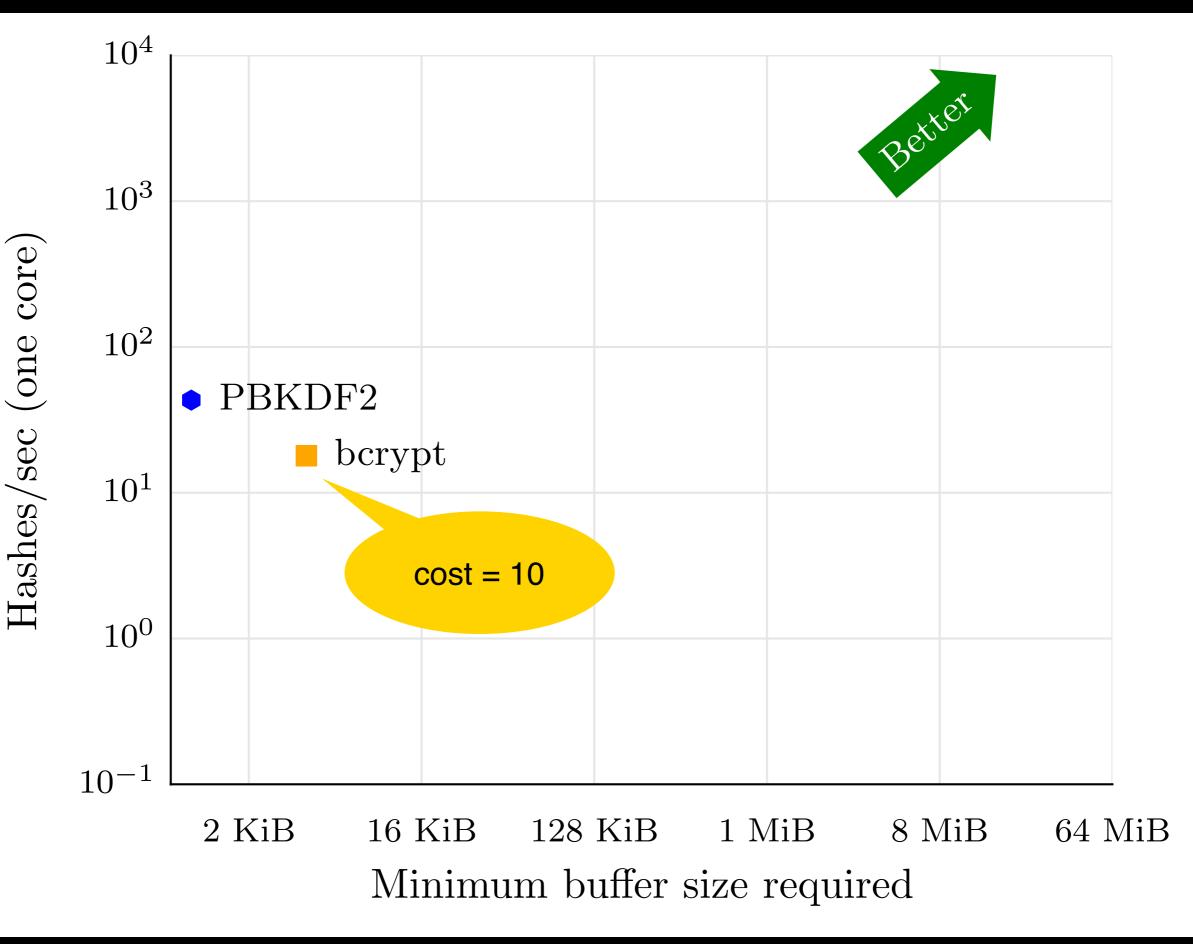
We draw heavily on prior work on pebbling arguments

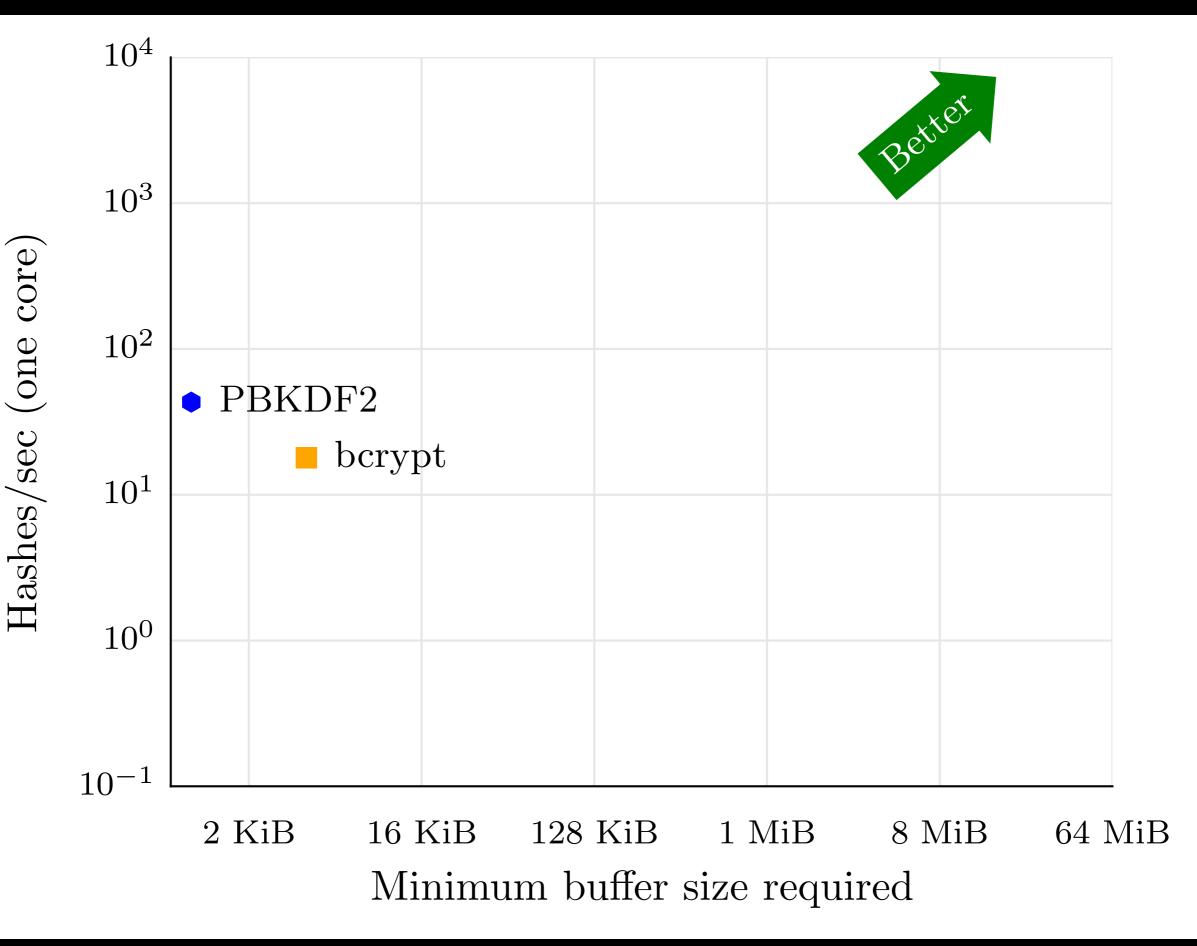
[Paterson & Hewitt 1970] [Paul & Tarjan 1978] [Dwork, Naor, Wee 2005] [Dziembowski, Kazana, Wichs 2011] [Alwen & Serbinenko 2015]

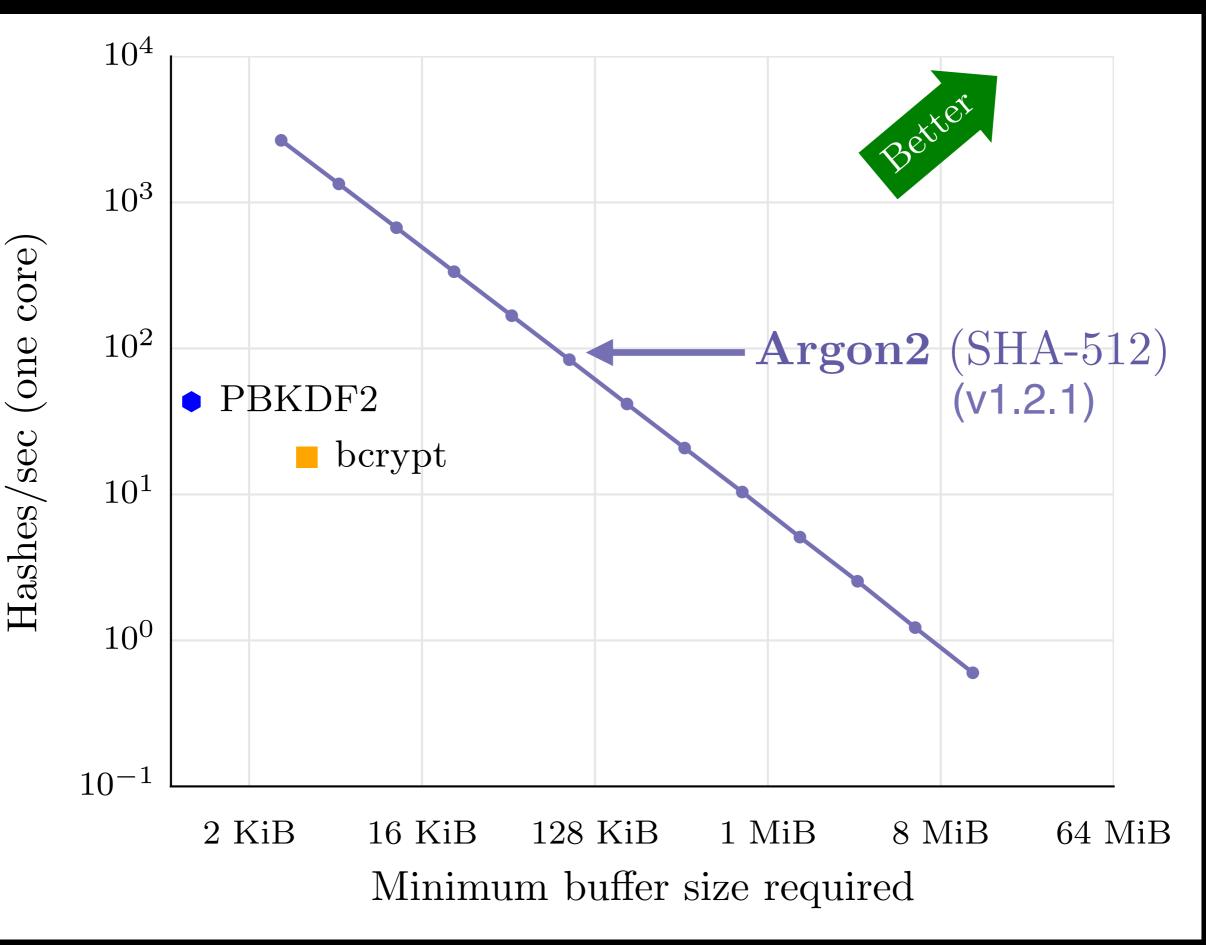




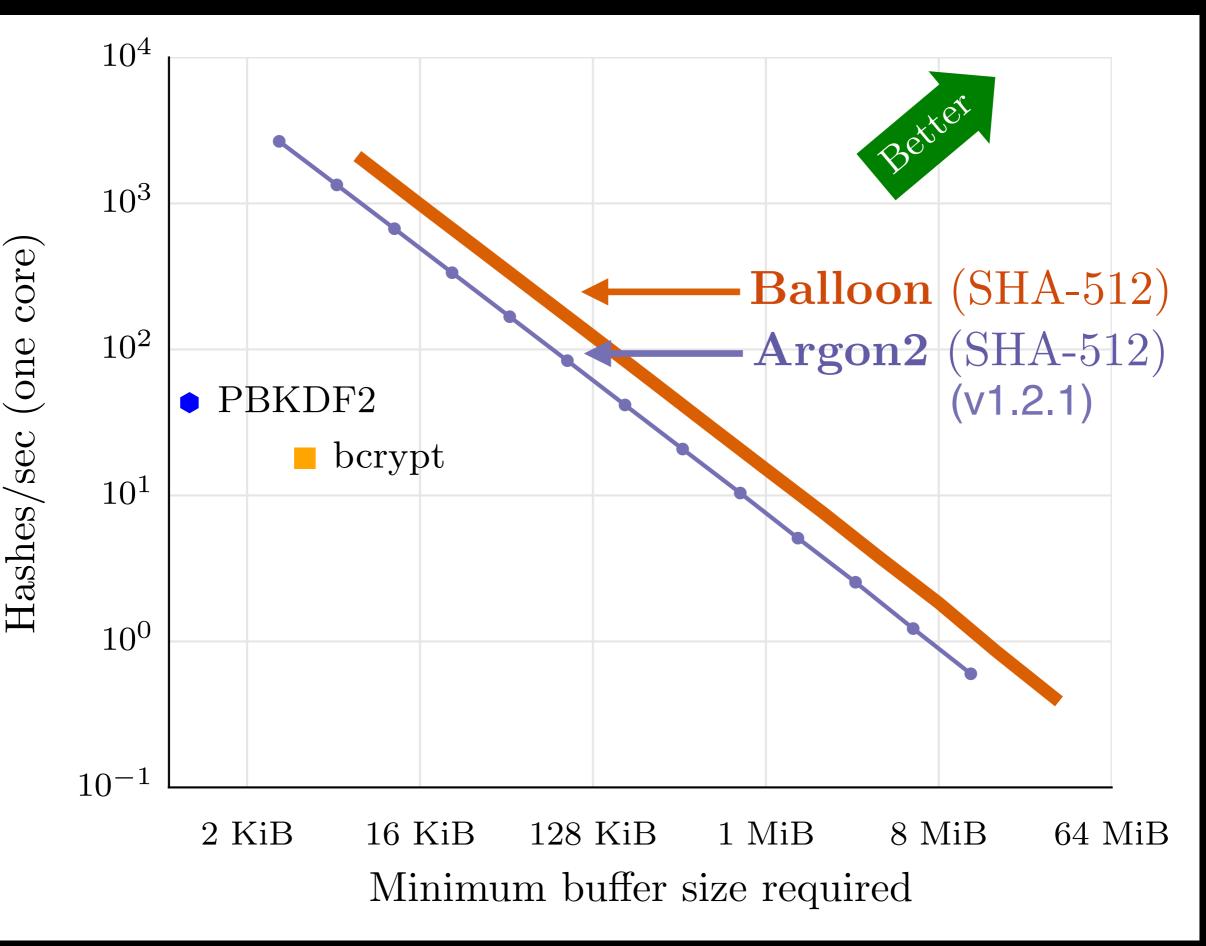




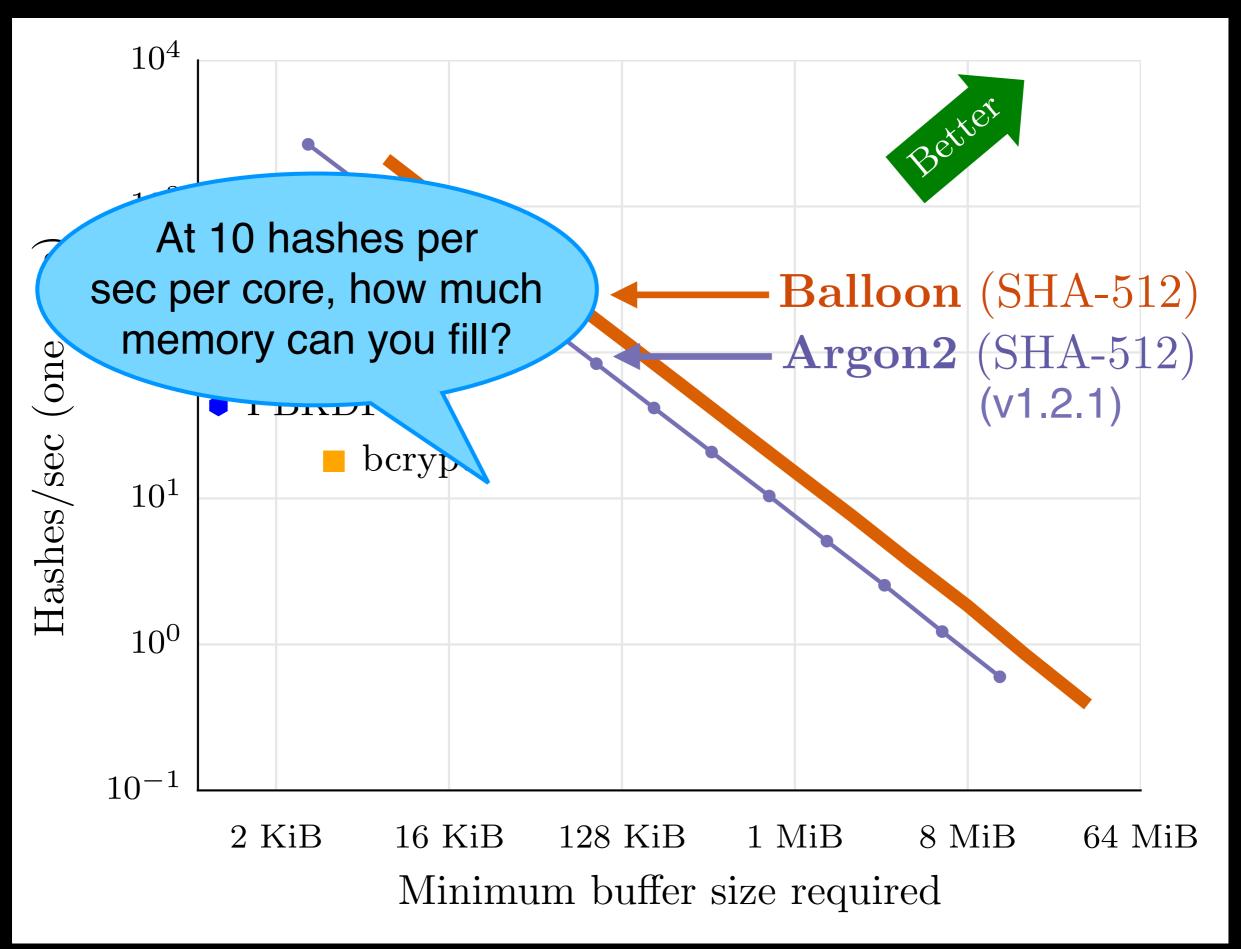


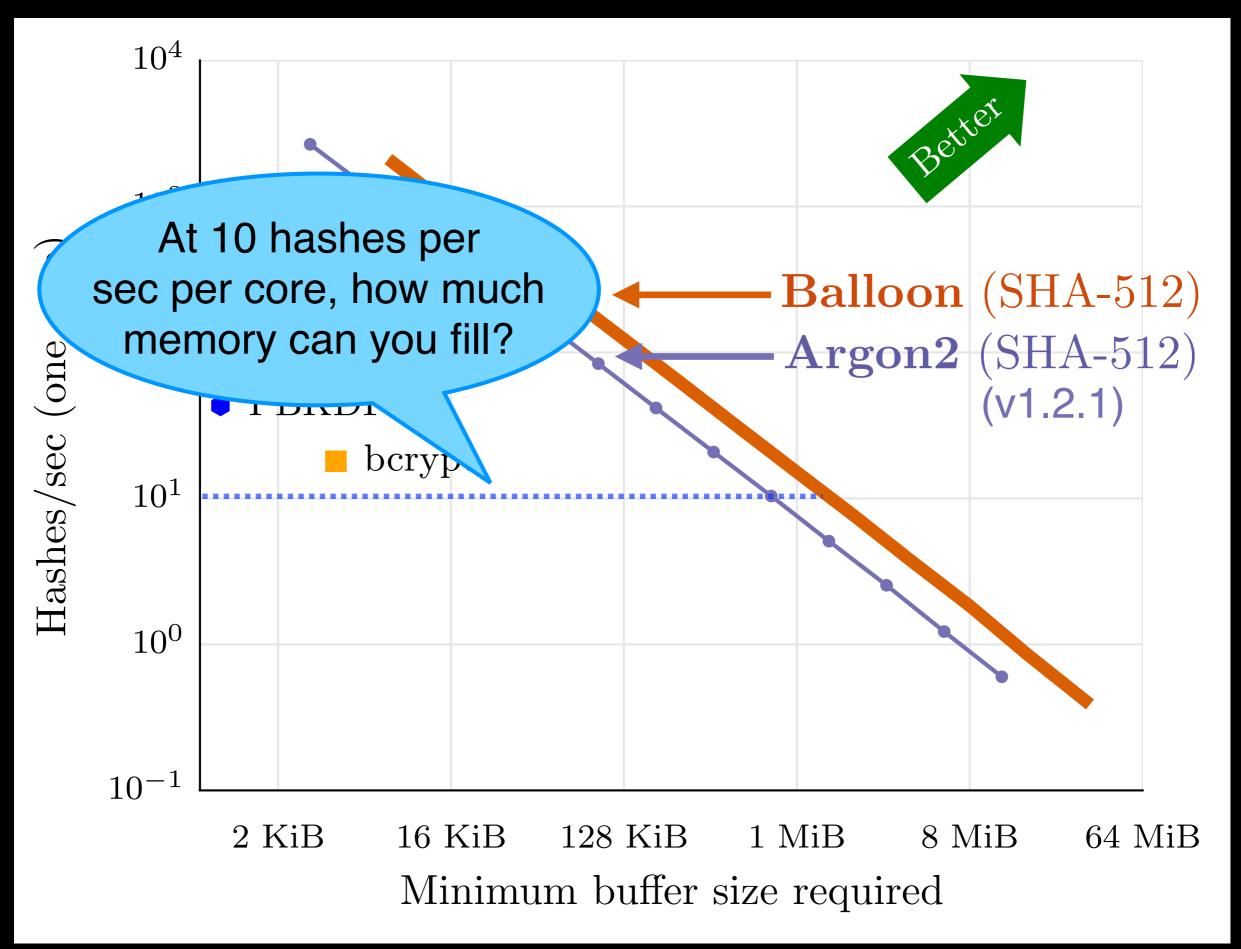


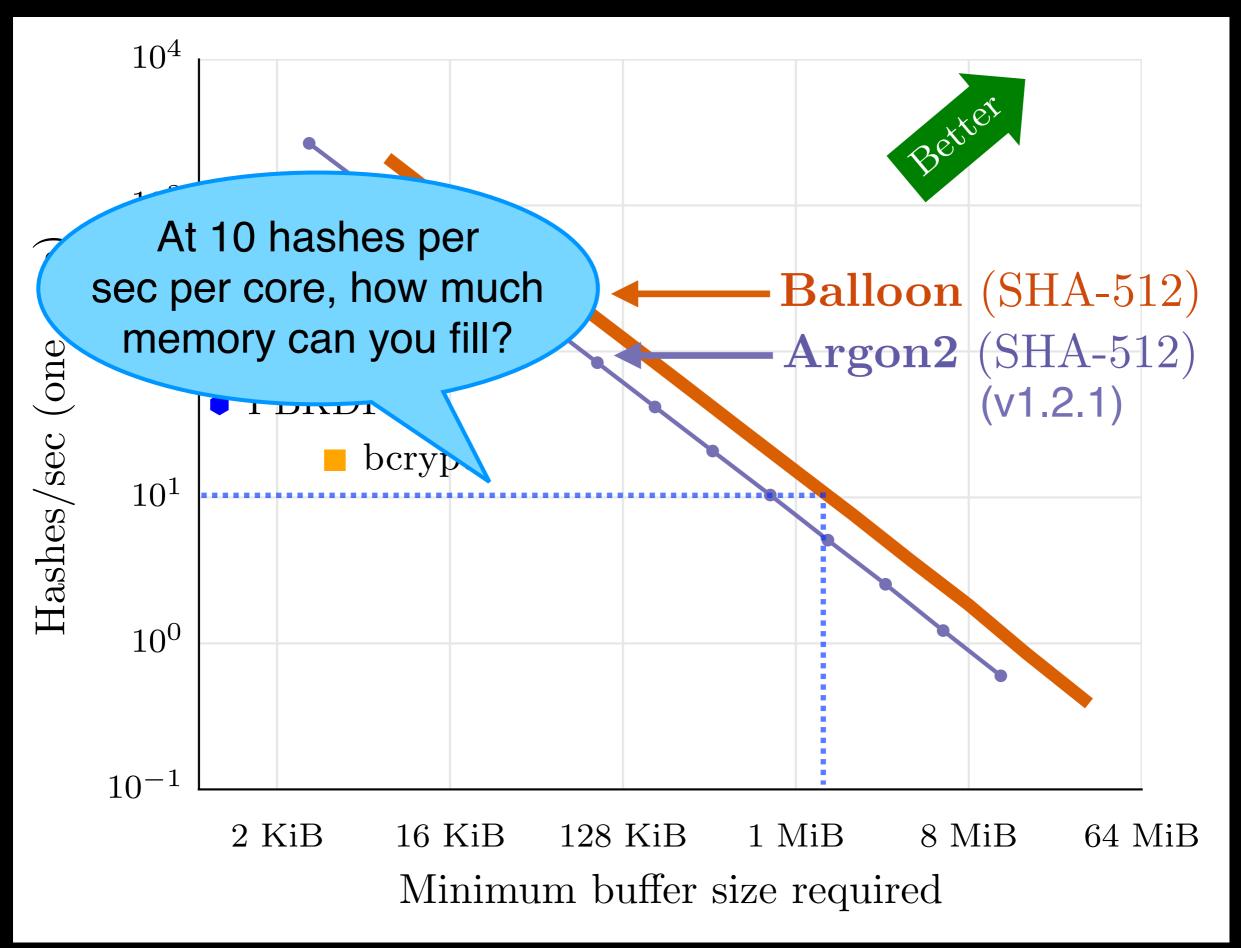
Using Balloon (δ =3). Both algorithms take four passes over memory.

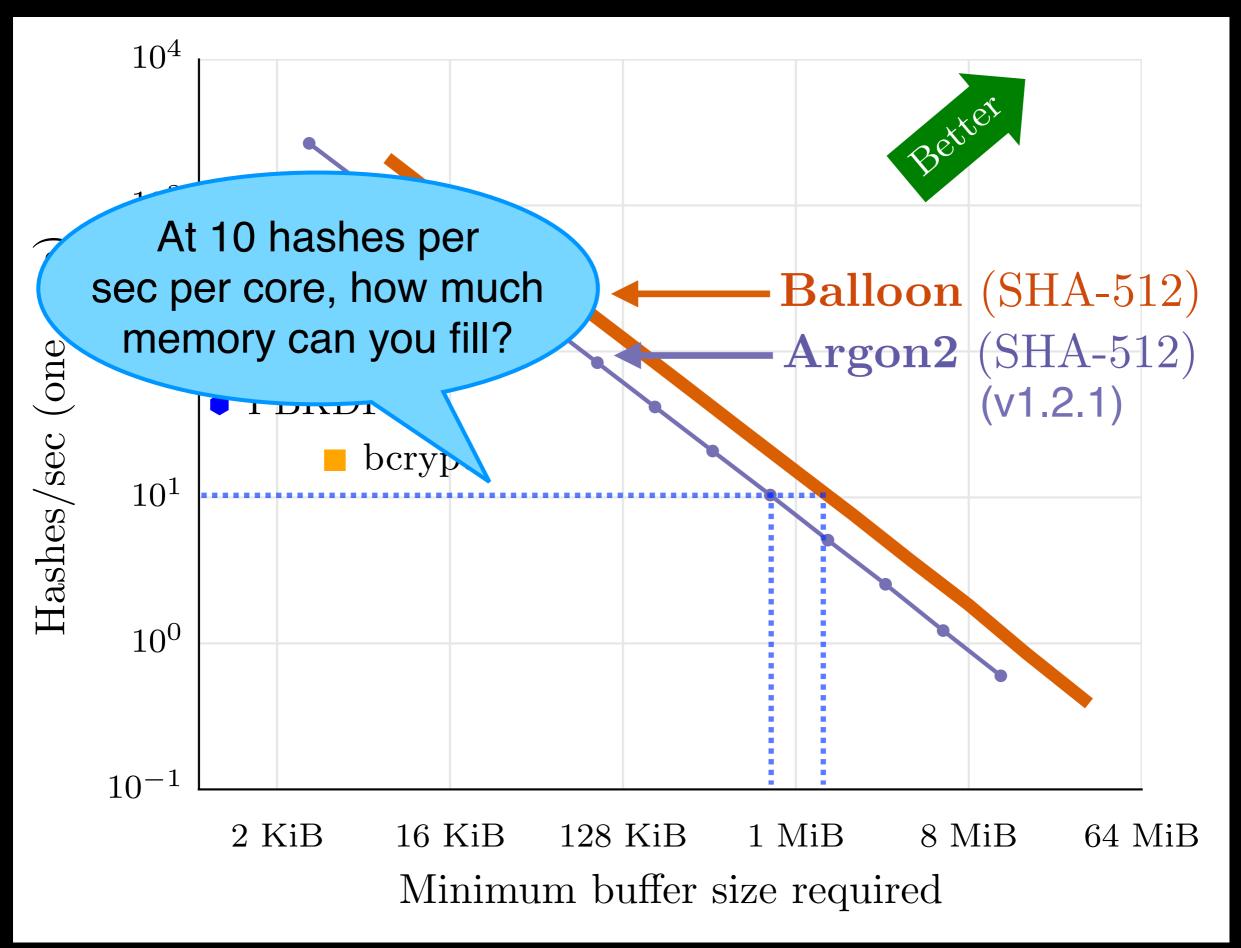


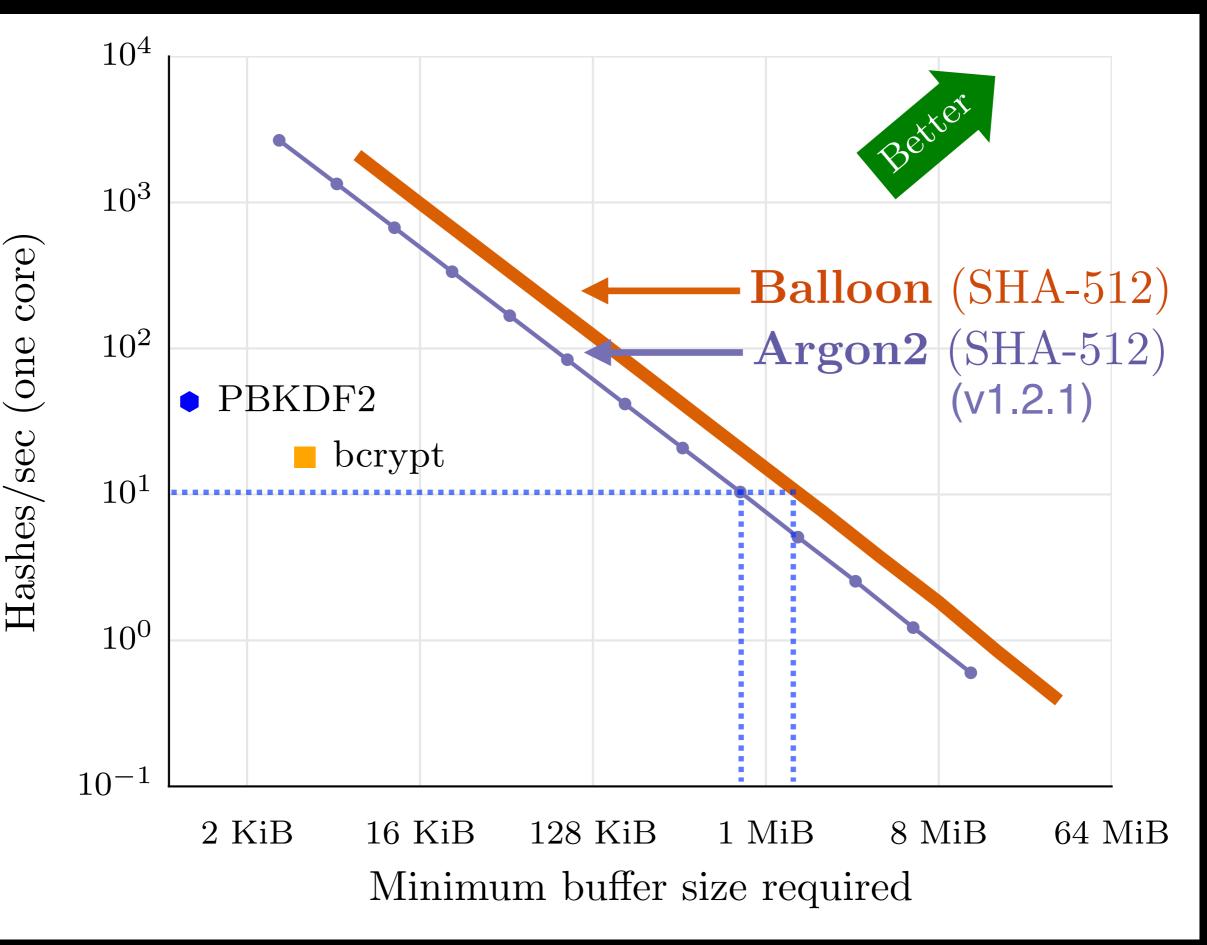
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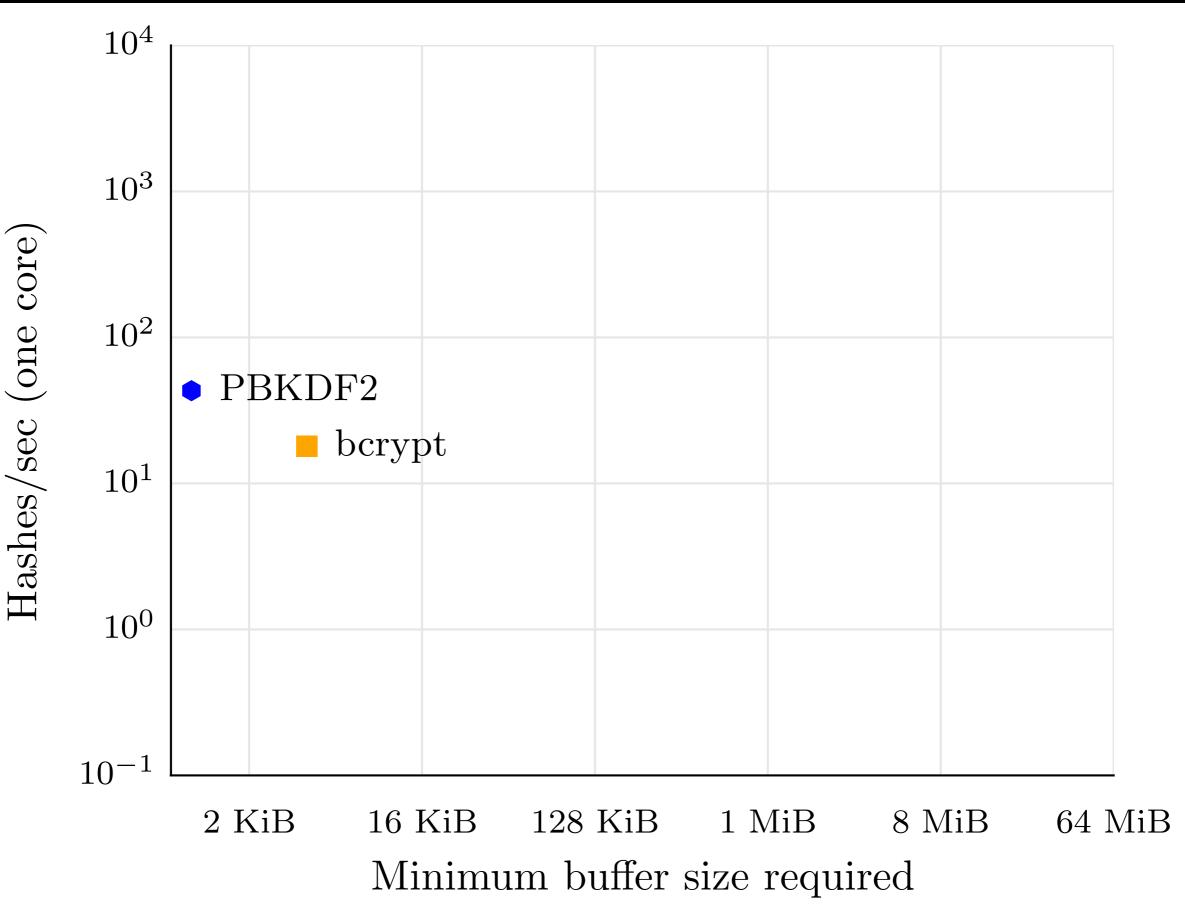


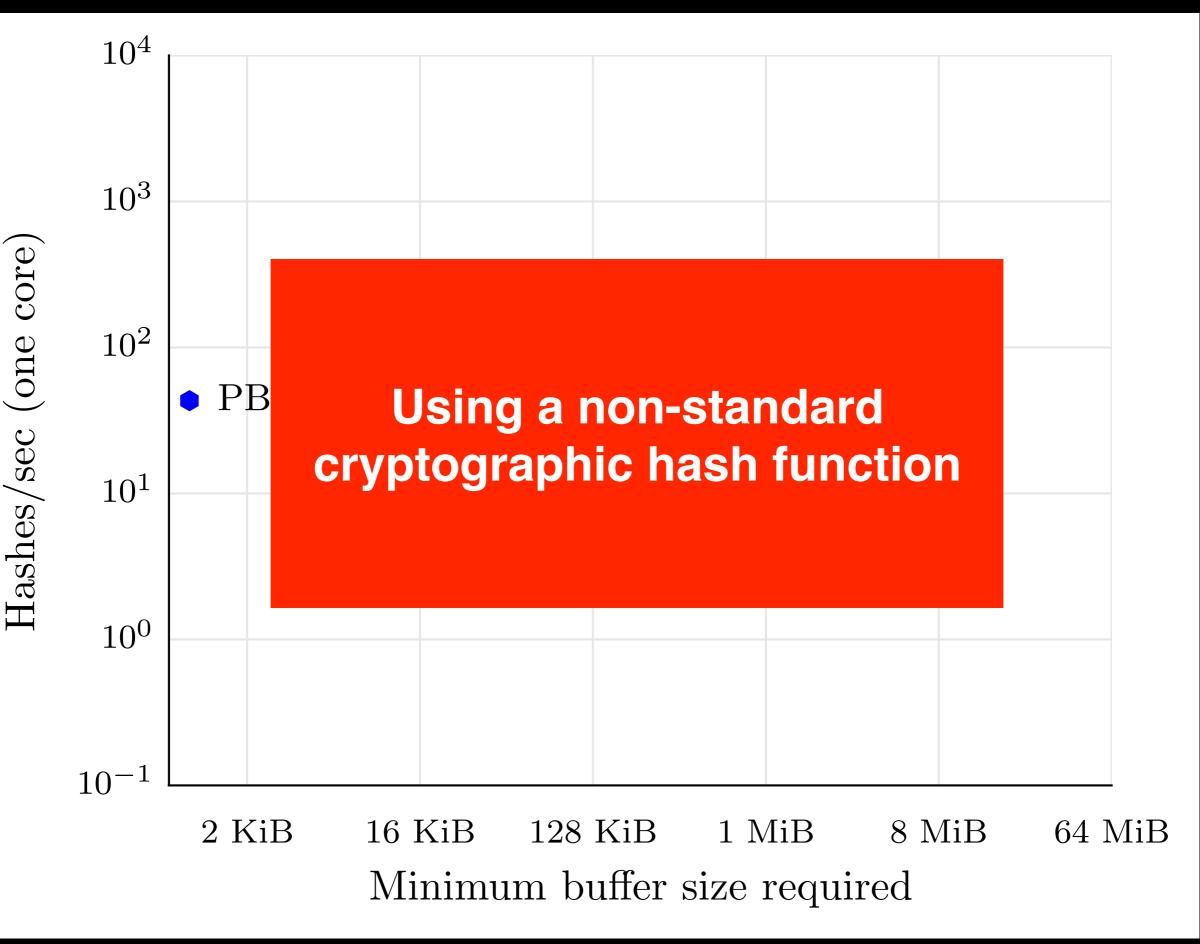


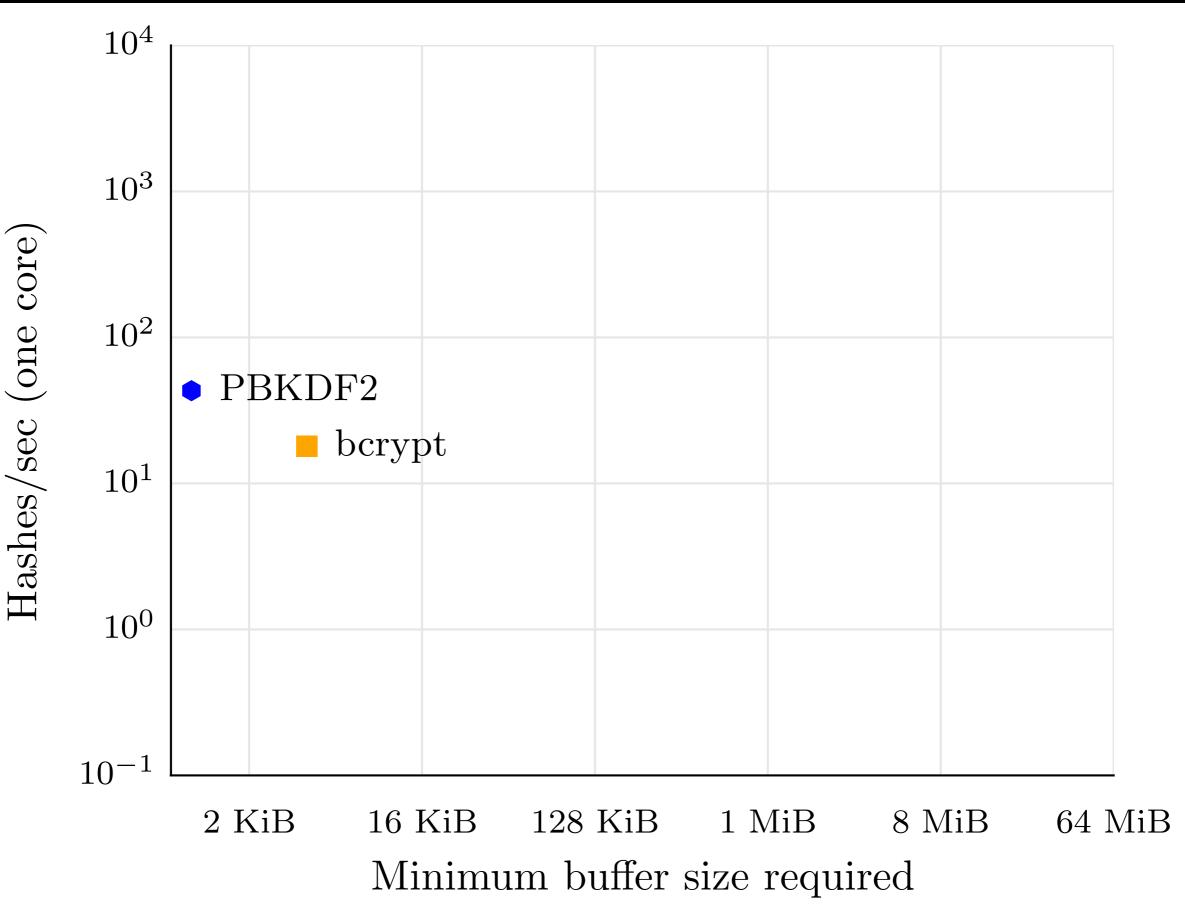


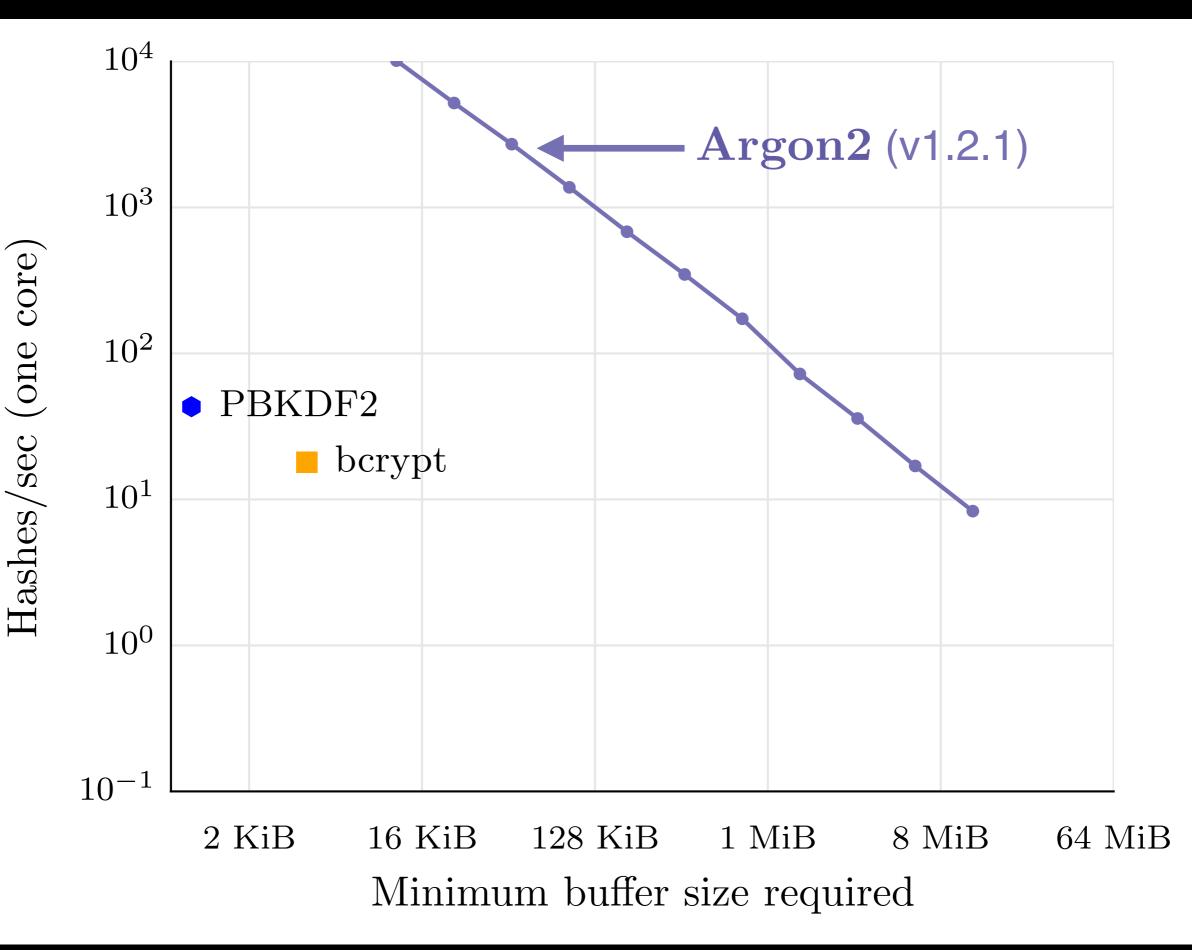


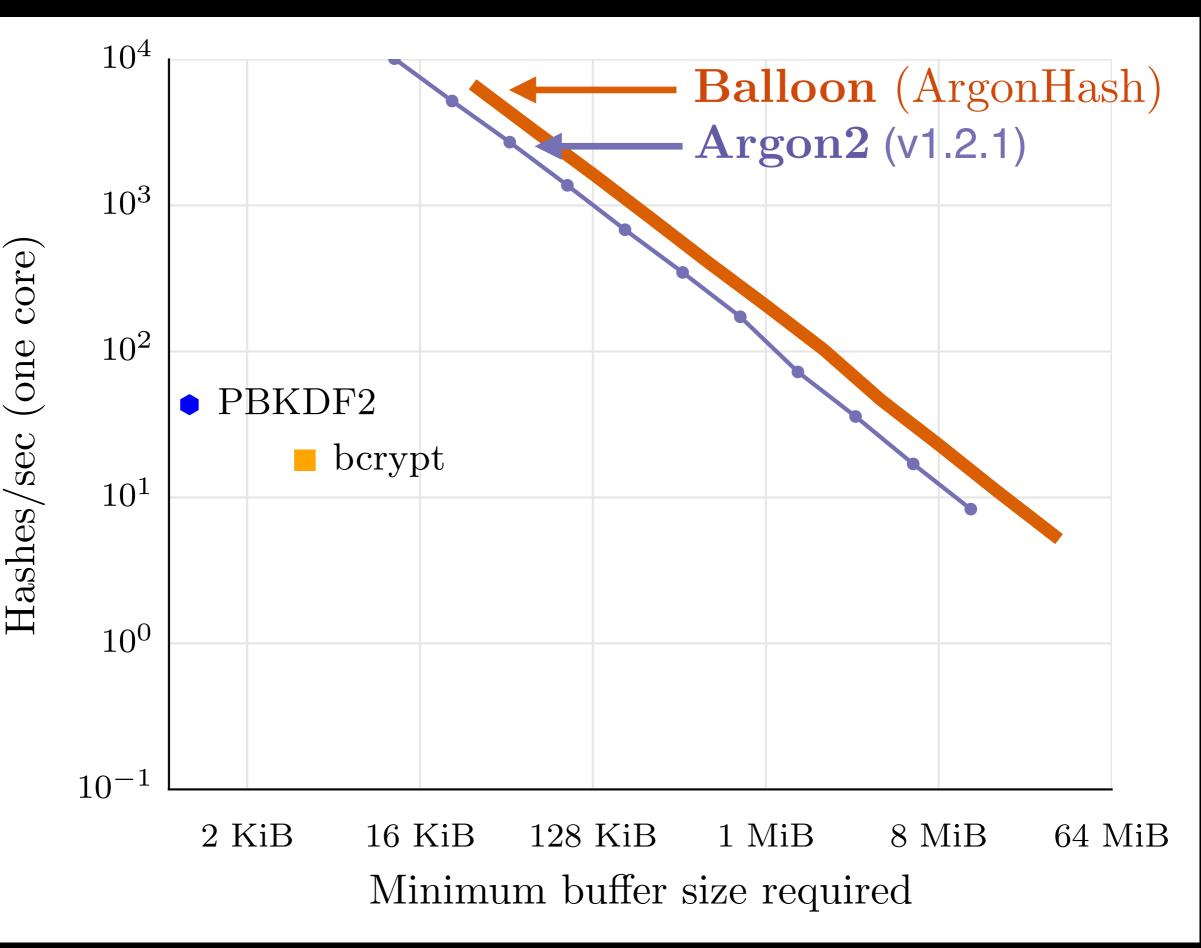


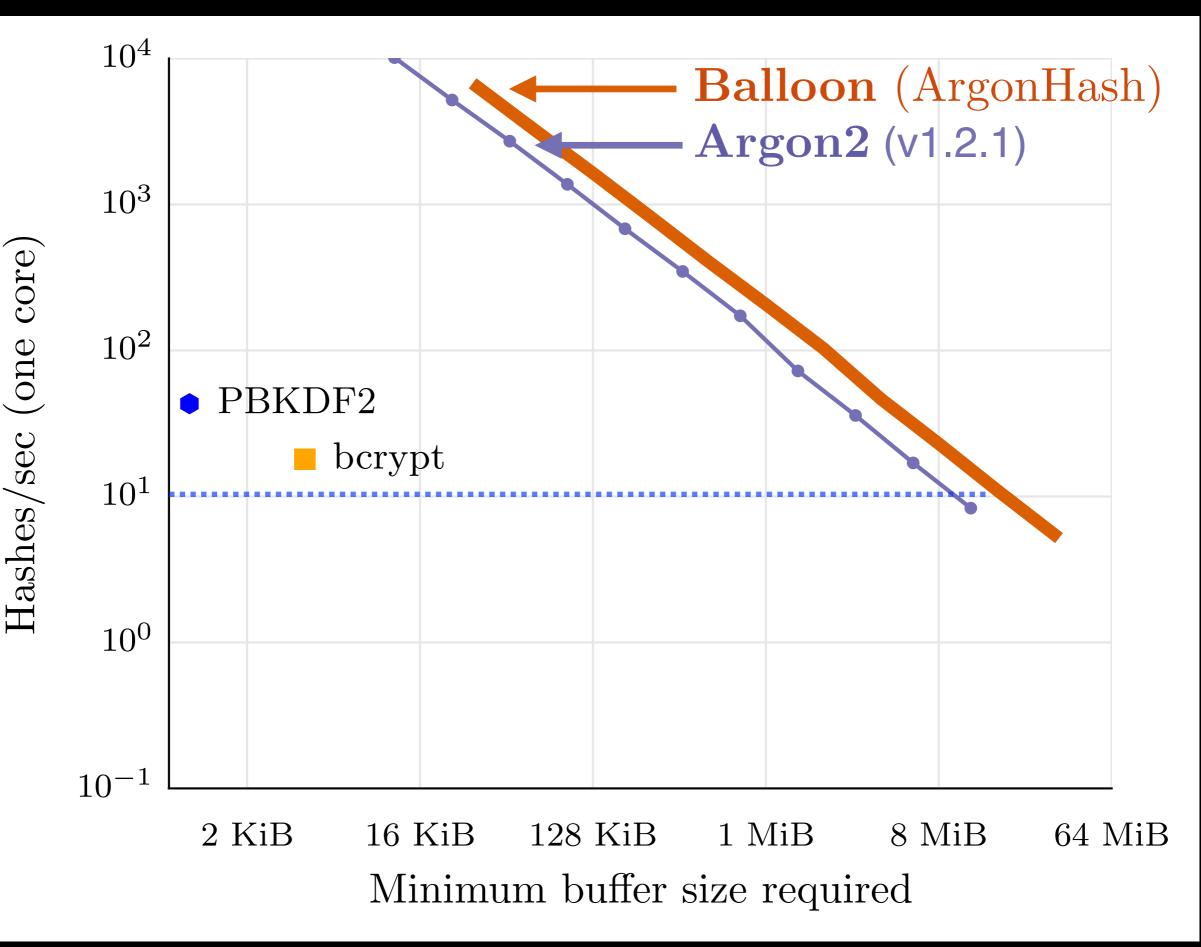


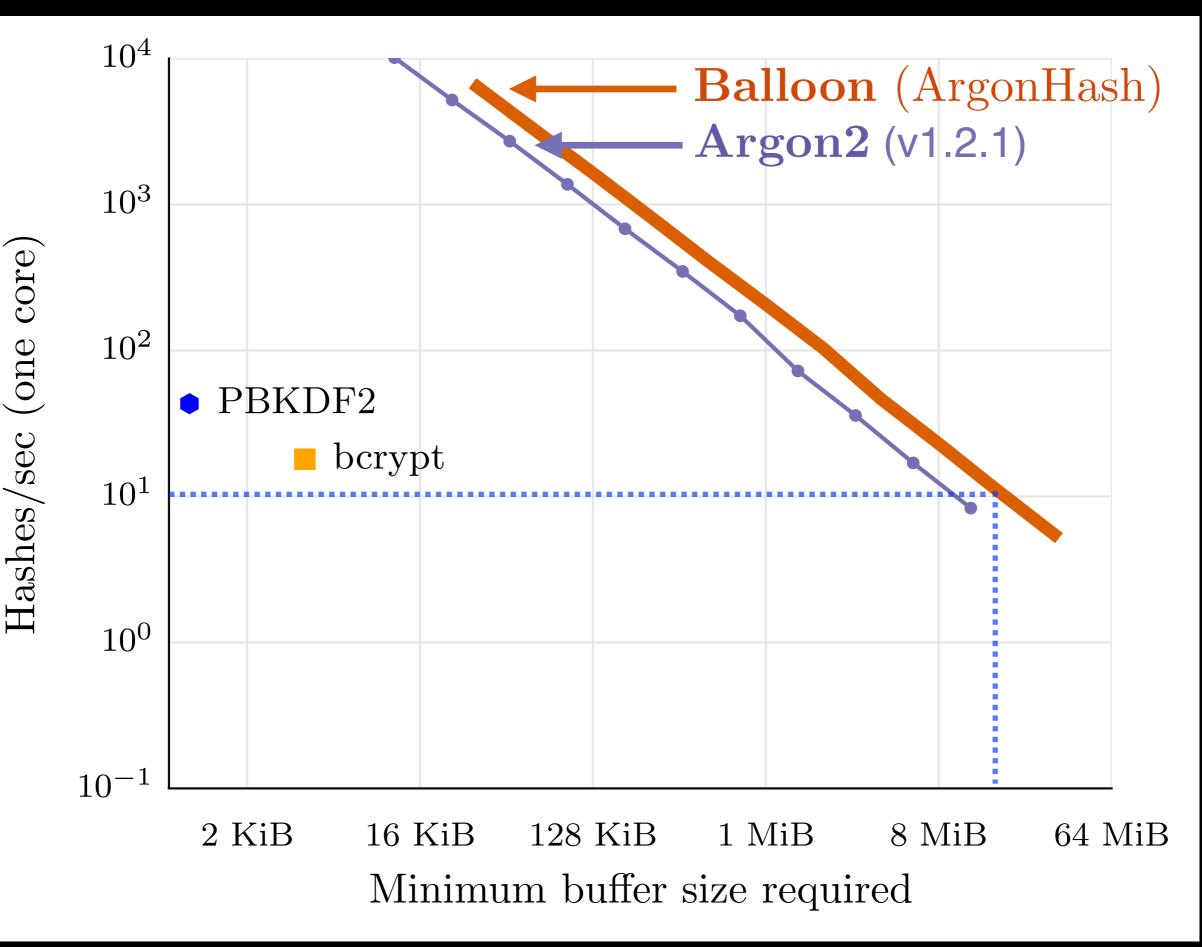


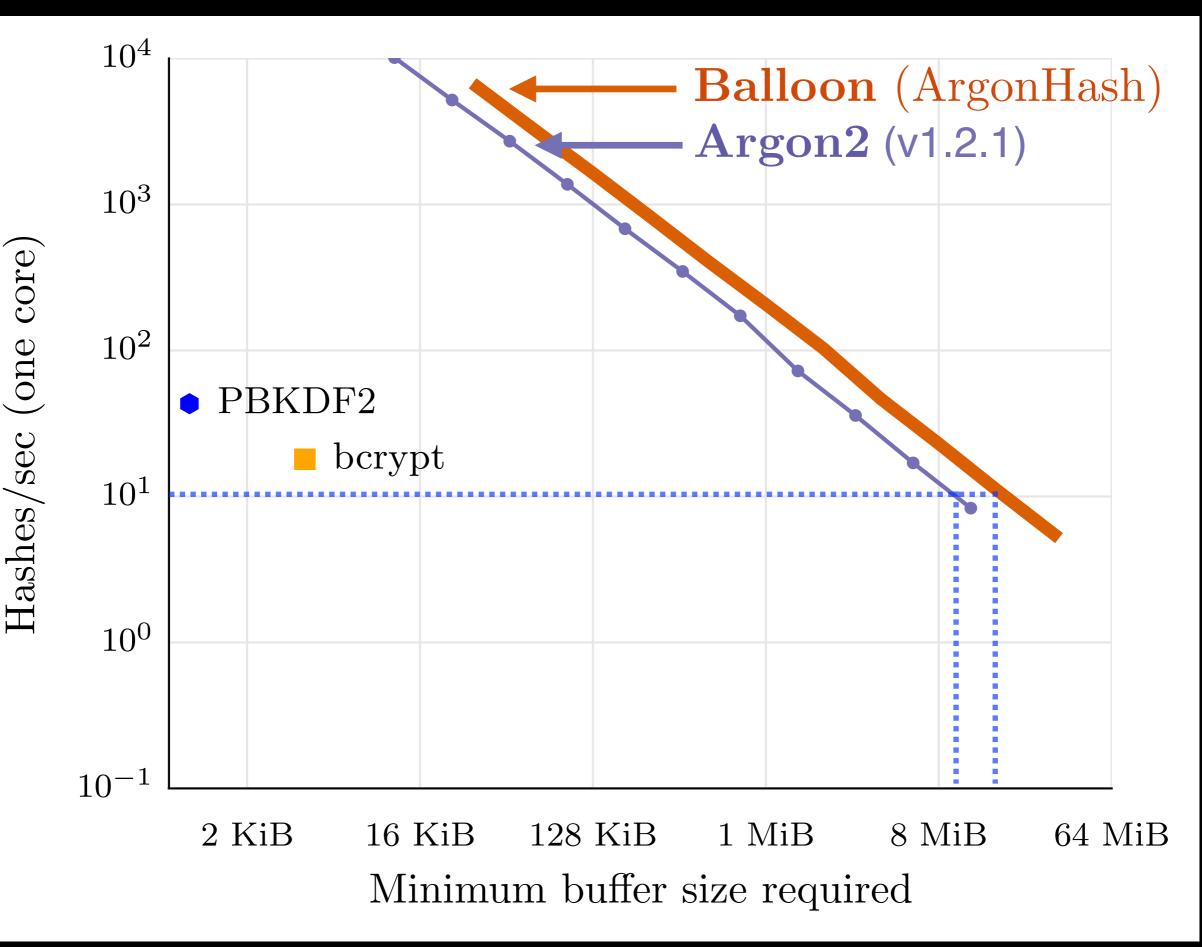












Plan

- I. Background on password hashing
- II. Goals

III. The Balloon algorithm

IV. Discussion

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- **IV. Discussion**

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- → Not yet clear whether these attacks are of practical concern.

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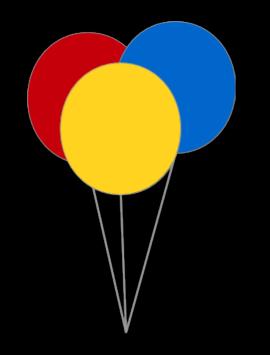
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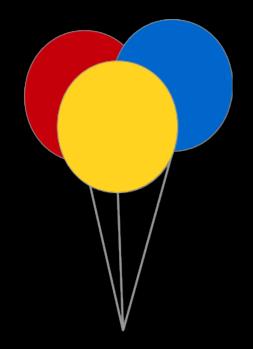
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- We prove that much better attacks are impossible
- → Balloon has stronger proven security properties than Argon2i. (In practice...)

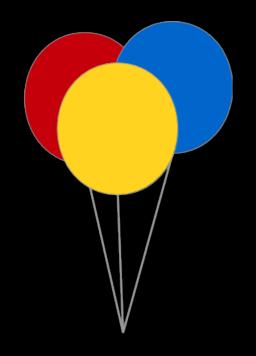


Henry Corrigan-Gibbs henrycg@stanford.edu



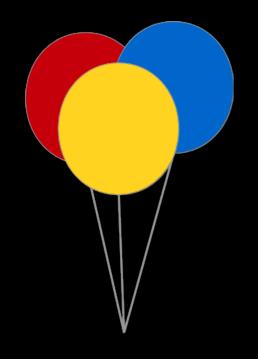
 Memory-hard password hashing functions increase the cost of offline dictionary attacks.

Henry Corrigan-Gibbs henrycg@stanford.edu



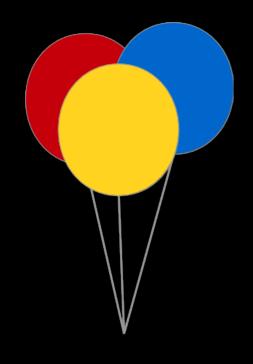
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- Balloon is a password hashing function that:
 - has proven memory-hardness properties against sequential attacks,
 - uses a password-indep. access pattern, and
 - is fast enough for real-world use.

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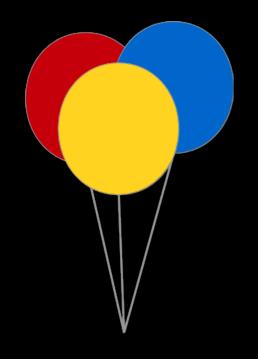
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An attacker who learns the memory access pattern of scrypt(passwd) can run a dictionary attack in very little space

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scrypt(passwd) 0x23AD 0x231F

0x2487

0x167A

0x1FD4

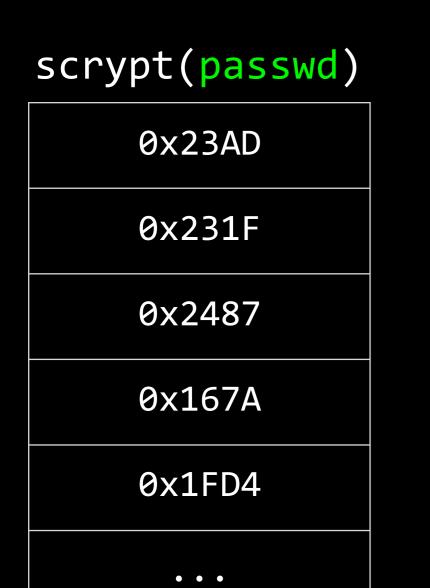
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scrypt("12345")

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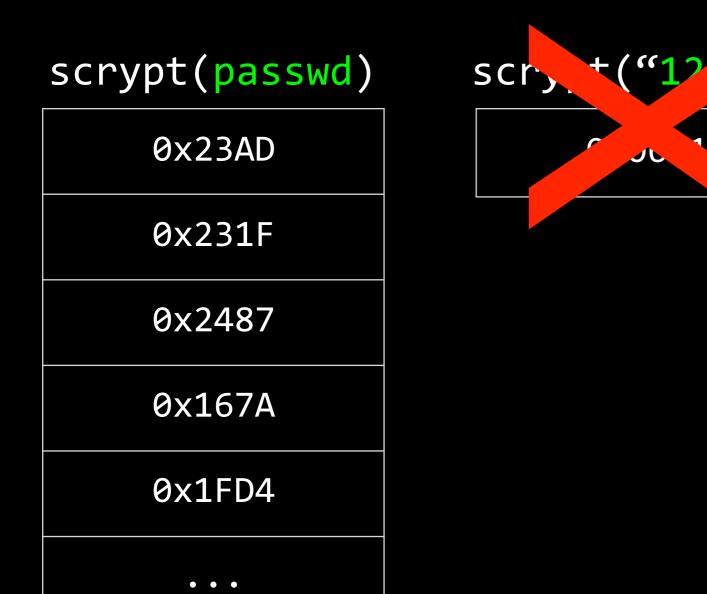


scrypt("12345")

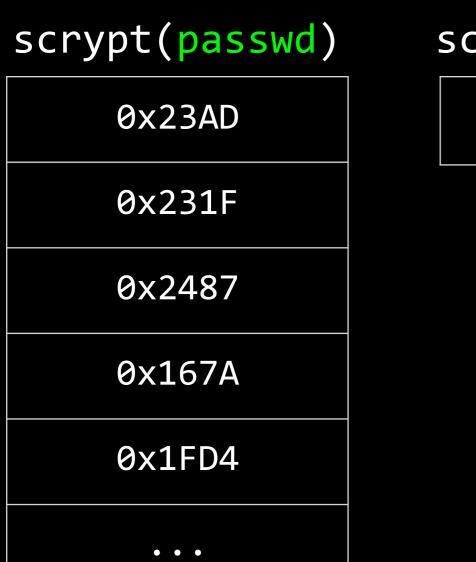
0x0631

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scrypt("abc123")

